

## Non-linear equation

Although non-linear differential equations are in general very difficult to solve, there is one almost obvious case where the solution is easy: if the generation rate  $g(t)$  is very large and then shuts off, and if  $n \gg n_0 + p_0$ , the equation becomes  $\frac{dn}{dt} \approx -K(T) n^2$  or, with

$$K(T) = \frac{1}{(n_0 + p_0)\tau_0}, \quad \frac{dn}{dt} \approx -\frac{n^2}{(n_0 + p_0)\tau_0}. \quad \text{This is easily integrated to give}$$

$$\frac{1}{n(t)} - \frac{1}{n(0)} = \frac{t}{(n_0 + p_0)\tau_0}, \quad \text{or, re-arranging, } n(t) = \frac{n(0)(n_0 + p_0)\tau_0}{n(0)t + (n_0 + p_0)\tau_0} \text{ which, for}$$

large values of  $t$ , decreases linearly with  $t$ .