

EE 610
09/07/17



$$-g_1 v_1 + 0 = i_{2a} = i_{3a} = -i_{3b} = i_{1b} = 0 - (-1g_2)v_2$$

$$g_1 v_1 = g_2 v_2 \Rightarrow v_2 = (g_1/g_2)v_1$$

$$i_{1a} = g_1 v_1 = g_1 v_2 \quad i_{2a} = -g_2 v_2$$

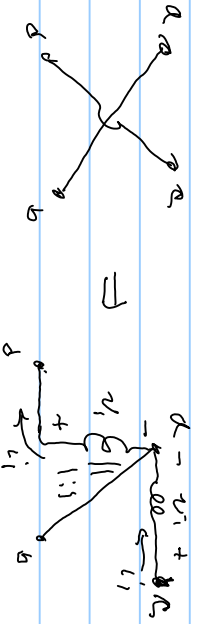
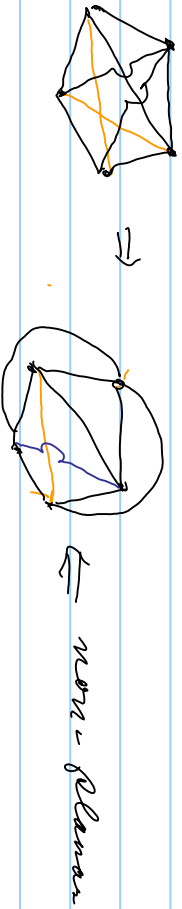
$$i_{1a} = i_{1b} = i_{2b} = -g_1/g_2 v_2$$

$$0 = i_{1a} = g_1 v_2$$

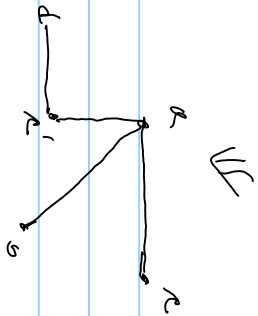
$$T = g_1/g_2$$

$$P_{in}(t) = v_1(t)i_1(t) + v_2(t)i_2(t) = v_1 \cdot i_1 + v_1 \left(\frac{g_1}{g_2} \right) \left(-\frac{1}{g_1/g_2} \right) i_1 = 0 \Rightarrow \text{Lossless}$$

Planar graph or non-planar



branch a-d has same v_i as before inter the transformer
 & branch a-b is unchanged



graph gets an extra branch.

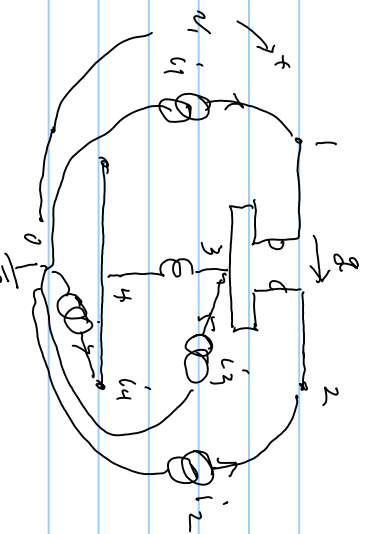
dual of graph $Y = \begin{bmatrix} 0 & 8 \\ -8 & 0 \end{bmatrix}$, $Z = Y = \begin{bmatrix} 0 & 11 \\ -11 & 0 \end{bmatrix}$

$$Z = Y^{-1} = +\frac{1}{8} \begin{bmatrix} 0 & -8 \\ +8 & 0 \end{bmatrix} \quad \text{check } ZY = I_2 = \begin{bmatrix} 0 & -11 \\ +11 & 0 \end{bmatrix} \begin{bmatrix} 0 & 8 \\ -8 & 0 \end{bmatrix} = \begin{bmatrix} +11 & 0 \\ 0 & +11 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 1/8 \\ -1/8 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 11 \\ -11 & 0 \end{bmatrix}, \quad V = 1/8$$

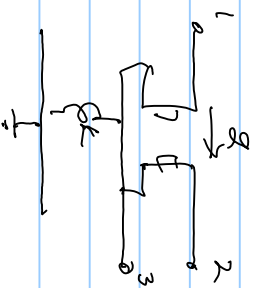
\therefore the dual of a graph is another graph $V = 1/8$

indefinite admittance matrix: Y_{ind}
 enters in a row add to zero & also in any column



$$\begin{bmatrix} i_1 \\ i_2 \\ i_3 \\ i_4 \end{bmatrix} = \underbrace{\begin{bmatrix} 0 & g & -g & 0 \\ -g & 0 & +g & 0 \\ +g & -g & 1/g & -1/g \\ 0 & 0 & -1/g & 1/g \end{bmatrix}}_{Y_{nod}} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{bmatrix}$$

more ground nodes present then $v_4 = 0 \Rightarrow$ can cross out last column, can ignore i_4 (as $= i_4$) \Rightarrow can cross out last row \Rightarrow gives a node by node admittance for all the nodes



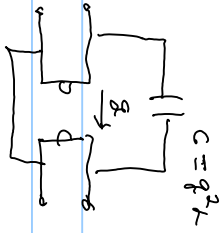
$$Y_{nod} = \begin{bmatrix} 0 & g & -g \\ -g & 0 & g \\ g & -g & 1/g \end{bmatrix}$$

I want the 2-row admittance for $\begin{matrix} l_1 \\ l_2 \end{matrix}$ + $\begin{matrix} g \\ g \end{matrix}$ + $\begin{matrix} l_2 \\ l_1 \end{matrix}$
 I desire to "eliminate" the 3 nodes $\begin{matrix} v_1 \\ v_2 \\ v_3 \end{matrix}$

$$\begin{bmatrix} l_1 \\ l_2 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 & g & -g \\ -g & 0 & g \\ g & -g & 0 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} \Rightarrow 0 = [g \ -g] \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} + [1/g] v_3$$

$$v_3 = g \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = [g \ g] \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$

$$\begin{bmatrix} l_1 \\ l_2 \end{bmatrix} = \begin{bmatrix} 0 & g \\ -g & 0 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} + \begin{bmatrix} -g \\ g \end{bmatrix} [g \ g] \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \\
 = \begin{bmatrix} +g^2 & g - g^2 \\ -g - g^2 & +g^2 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \Rightarrow \text{2 rows} = \begin{bmatrix} g^2 & g - g^2 \\ -g - g^2 & g^2 \end{bmatrix}$$



$$C \Rightarrow Y = Cx \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}$$