

ENEE 610 Fall 2017 – Homework 3 Due Th 09/28/17

1. (50 points; semistate realization)

The following semistate equations describe a 2-port characterized by its admittance matrix,  $y=Y(s)u$  where  $y=i$  and  $u=v$  are the port 2-vectors and  $x$  is a 3-vector semistate.

$$\begin{pmatrix} C & -C & 0 \\ -C & C & 0 \\ 0 & 0 & 0 \end{pmatrix} \cdot \frac{dx}{dt} := \begin{pmatrix} 1 & -1 & 1 \\ 1 & 0 & -1 \\ 0 & 1 & 0 \end{pmatrix} \cdot x + \begin{pmatrix} 0 & 0 \\ -1 & 0 \\ 0 & -1 \end{pmatrix} \cdot u$$

$$y := \begin{pmatrix} 0 & 0 & 1 \\ 0 & G & -1 \end{pmatrix} \cdot x$$

a) Transform the semistate  $x$  such that  $E$  is the direct sum of the  $1 \times 1$  (capacitor constant)  $C$  and a  $2 \times 2$  zero matrix.

b) Find the 2-port admittance matrix  $Y(s)$ .

2. (50 points; constant R circuit)

A constant R lattice has  $y_1(s)=sC+1/(sL)$  and  $R=(1/G)$ .

a) Give  $y_2(s)$  and  $v_o/v_i(s)$ .

b) Draw the resulting lattice circuit including source (with internal resistance  $R$ ) and load of resistance  $R$ .

c) Give the poles and zeros of  $v_o/v_i$  and determine  $G$ ,  $C$  &  $L$  for which they are real and double.

d) For a circuit of part c) with  $R=50\Omega$  do a Spice run and plot the amplitude and phase over an important range of frequencies.

e) Discuss the possibility of using two constant R circuits of smaller degree.