

## Introduction to Cryptology ENEE459E/CMSC498R: Homework 11

Due by beginning of class on 5/7/2015.

1. Describe in detail a man-in-the-middle attack on the Diffie-Hellman key-exchange protocol whereby the adversary ends up sharing a key  $k_A$  with Alice and a different key  $k_B$  with Bob, and Alice and Bob cannot detect that anything has gone wrong.

What happens if Alice and Bob try to detect the presence of a man-in-the-middle adversary by sending each other (encrypted) questions that only the other party would know how to answer?

2. Consider the following key-exchange protocol:

- (a) Alice chooses  $k, r \leftarrow \{0, 1\}^n$  at random, and sends  $s := k \oplus r$  to Bob.
- (b) Bob chooses  $t \leftarrow \{0, 1\}^n$  at random and sends  $u := s \oplus t$  to Alice.
- (c) Alice computes  $w := u \oplus r$  and sends  $w$  to Bob.
- (d) Alice outputs  $k$  and Bob outputs  $w \oplus t$ .

Show that Alice and Bob output the same key. Analyze the security of the scheme (i.e., either prove its security or show a concrete attack).

3. Consider the following key-exchange protocol:

Common input: The security parameter  $1^n$ .

- (a) Alice runs  $\mathcal{G}(1^n)$  to obtain  $(G, q, g)$ .
- (b) Alice chooses  $x_1, x_2 \leftarrow Z_q$  and sends  $\alpha = x_1 + x_2$  to Bob.
- (c) Bob chooses  $x_3 \leftarrow Z_q$  and sends  $h_2 = g^{x_3}$  to Alice.
- (d) Alice sends  $h_3 = g^{x_2 \cdot x_3}$  to Bob.
- (e) Alice outputs  $h_2^{x_1}$ . Bob outputs  $(g^\alpha)^{x_3} \cdot (h_3)^{-1}$ .

Show that Alice and Bob output the same key. Analyze the security of the scheme (i.e., either prove its security or show a concrete attack).

4. Show that any 2-round key-exchange protocol (that is, where each party sends a single message) can be converted into a CPA-secure public-key encryption scheme.
5. Fix an RSA public key  $\langle N, e \rangle$  and assume we have an algorithm  $A$  that always correctly computes  $lsb(x)$  given  $[x^e \bmod N]$ . Write full pseudocode for an algorithm  $A'$  that computes  $x$  from  $[x^e \bmod N]$ .