

ACM CCS'15, Denver, Colorado, Oct 15 2015

Based on slides from:

# Introduction to Cryptocurrencies

a tutorial

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With some added and  
removed material



**INNOVATIVE ECONOMY**  
NATIONAL COHESION STRATEGY



*Foundation for Polish Science*

**EUROPEAN UNION**  
EUROPEAN REGIONAL  
DEVELOPMENT FUND



# Announcements

- Midterm Upcoming on 3/13
  - Review sheet and practice exam posted on course webpage/Canvas
  - Solutions and Cheat Sheet posted soon on Canvas



An extended abstract of this tutorial (including the references) is available at:

[www.crypto.edu.pl/Dziembowski/talks/bitcointutorial.pdf](http://www.crypto.edu.pl/Dziembowski/talks/bitcointutorial.pdf).

These slides are available at

[www.crypto.edu.pl/Dziembowski/talks](http://www.crypto.edu.pl/Dziembowski/talks).

# Outline

1. Introduction to Bitcoin
2. Bitcoin mining pools
3. Security of Bitcoin
4. Smart contracts
5. Other cryptocurrencies
6. Conclusion

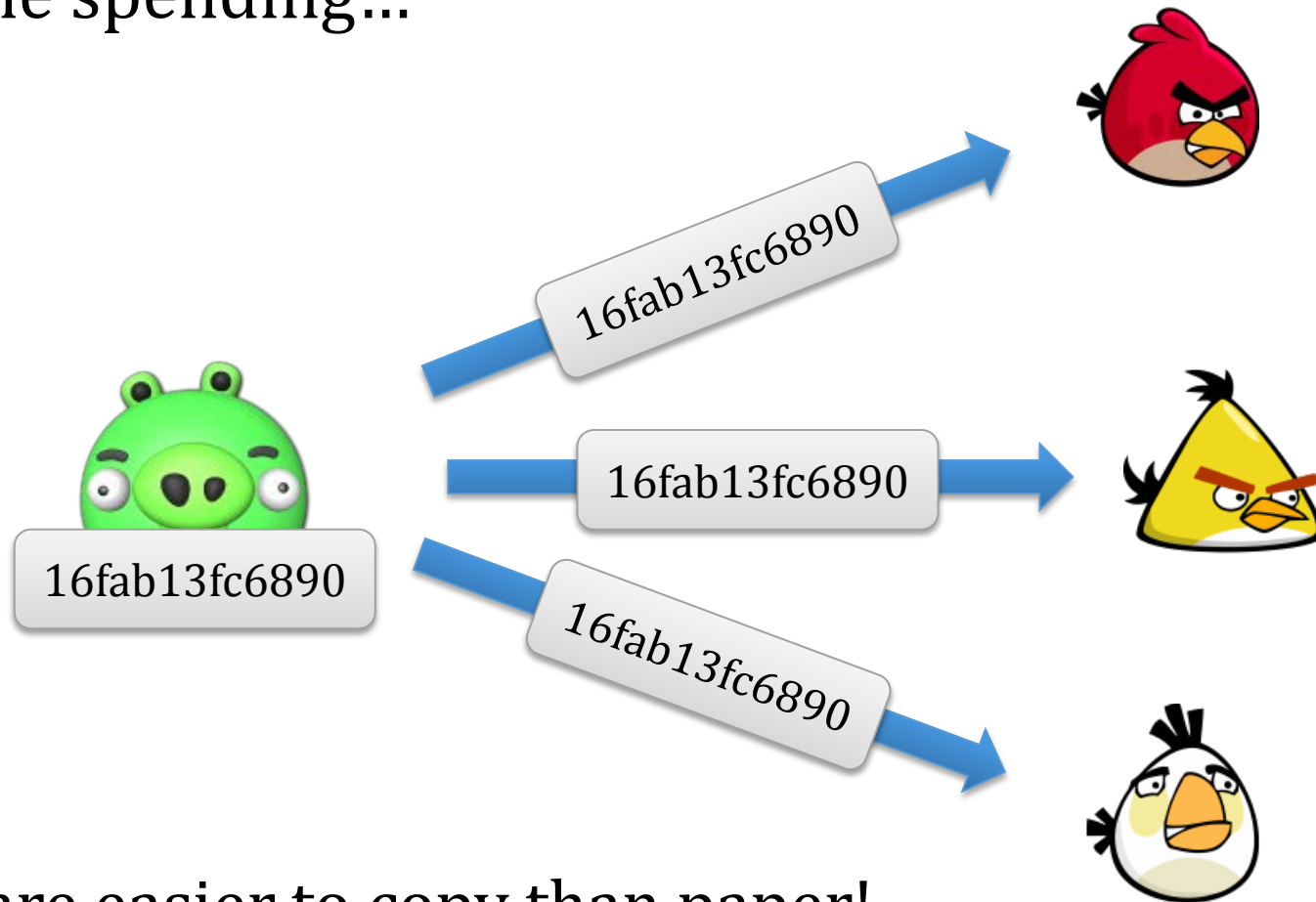
# Part I

Introduction to Bitcoin

# Main design principles

# Main problem with the digital money

Double spending...



Bits are easier to copy than paper!

# Bitcoin idea (simplified):

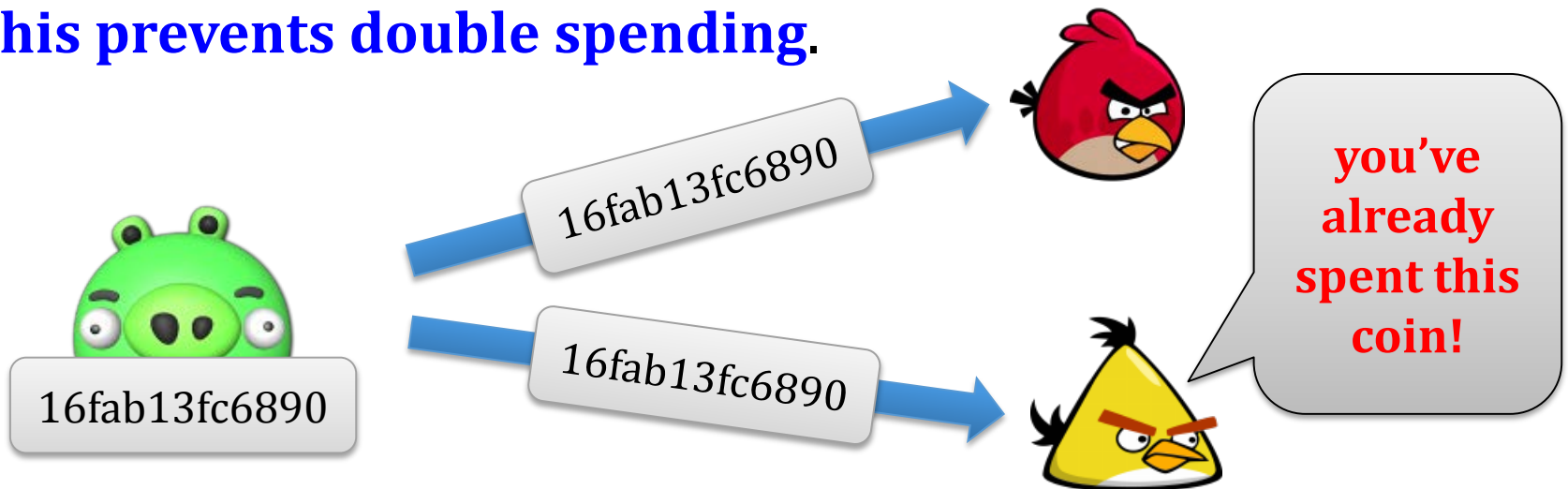
The users emulate a **public trusted bulletin-board** containing a list of transactions.

A transaction is of a form:



“User  $P_1$  transfers a coin #16fab13fc6890 to user  $P_2$ ”

**This prevents double spending.**



# What needs to be discussed

1. How is the **trusted bulletin-board** maintained?
2. How are the users identified?
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# The Merkle-Damgård Transform = Blockchain

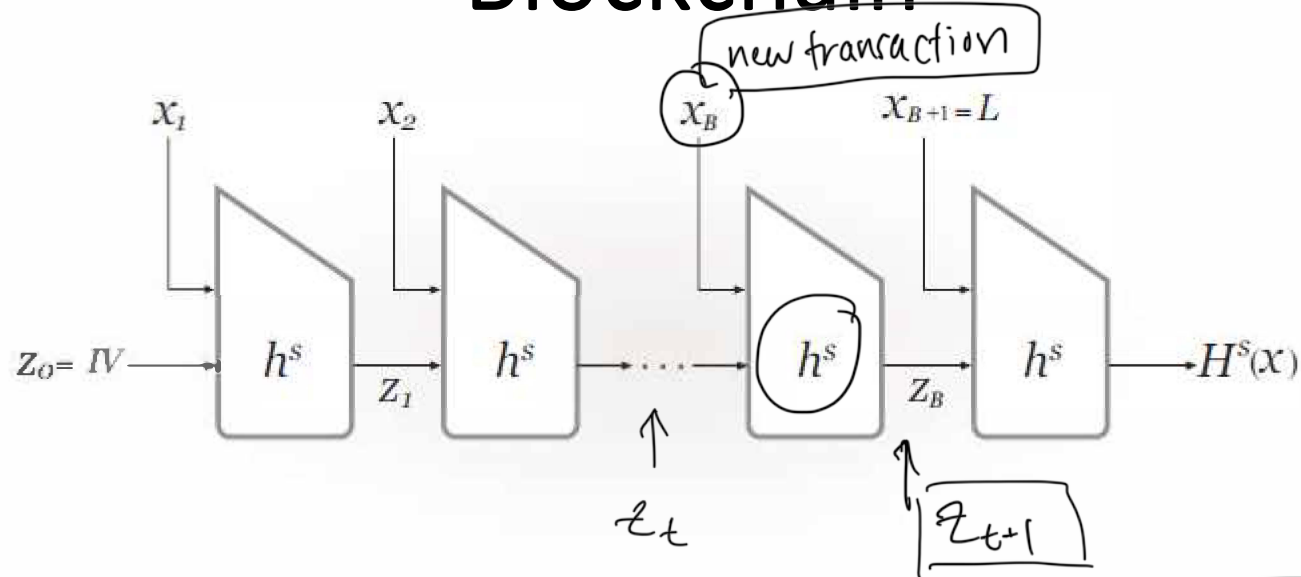


FIGURE 5.1: The Merkle-Damgård transform.

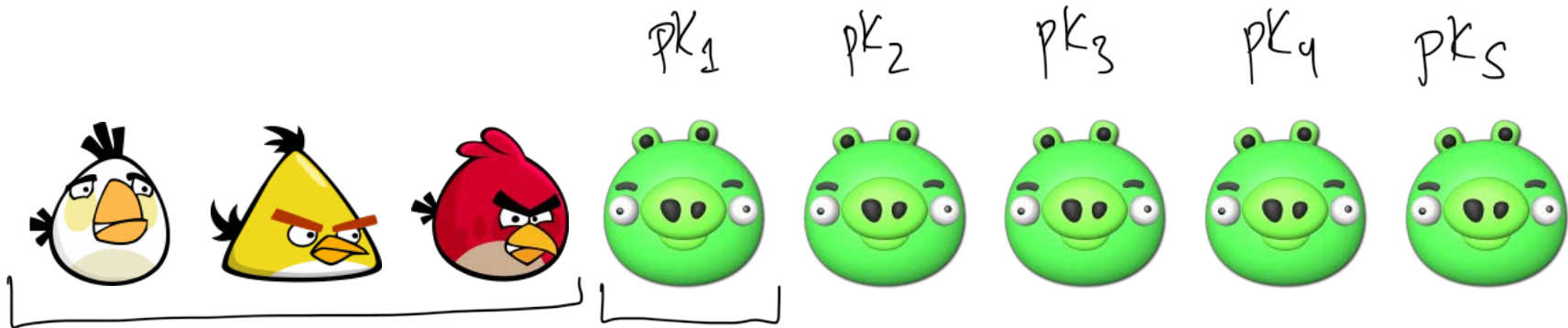
$Z'_{t+1}$

Problem: How to reach consensus on the correct final  $Z$  which fixes the **entire history**?

First attempt: Majority vote!

# Problem

How to define “**majority**” in  
a situation where  
**everybody can join the network?**



# The Bitcoin solution

Define the “majority” as

**the majority of the computing power**

*Assume  
majority of computing  
power  
honest*

Now creating multiple identities does not help!



# How is this enforced?

Main idea:

- use **Proofs of Work**
- **incentivize** honest users to constantly participate in the process

The honest users can use their **idle CPU cycles**.

Nowadays: often done on **dedicated hardware**.

# Proofs of work

Introduced by **Dwork and Naor** [Crypto 1992] as a countermeasure against spam.



## **Basic idea:**

Force users to do some computational work:

    solve a **moderately difficult** “puzzle”

    (checking correctness of the solution has to be fast)

# A simple hash-based PoW

$h^s$

**H**-- a hash function whose computation takes time **TIME(H)**  
*previous hash of*  
*↓ BC + new trans*



**Prover**

finds **s** such that **H(s,x)** starts with **n** zeros (in binary)



takes time  **$2^n \cdot \text{TIME(H)}$**

**Verifier**

checks if **H(s,x)** starts with **n** zeros

60

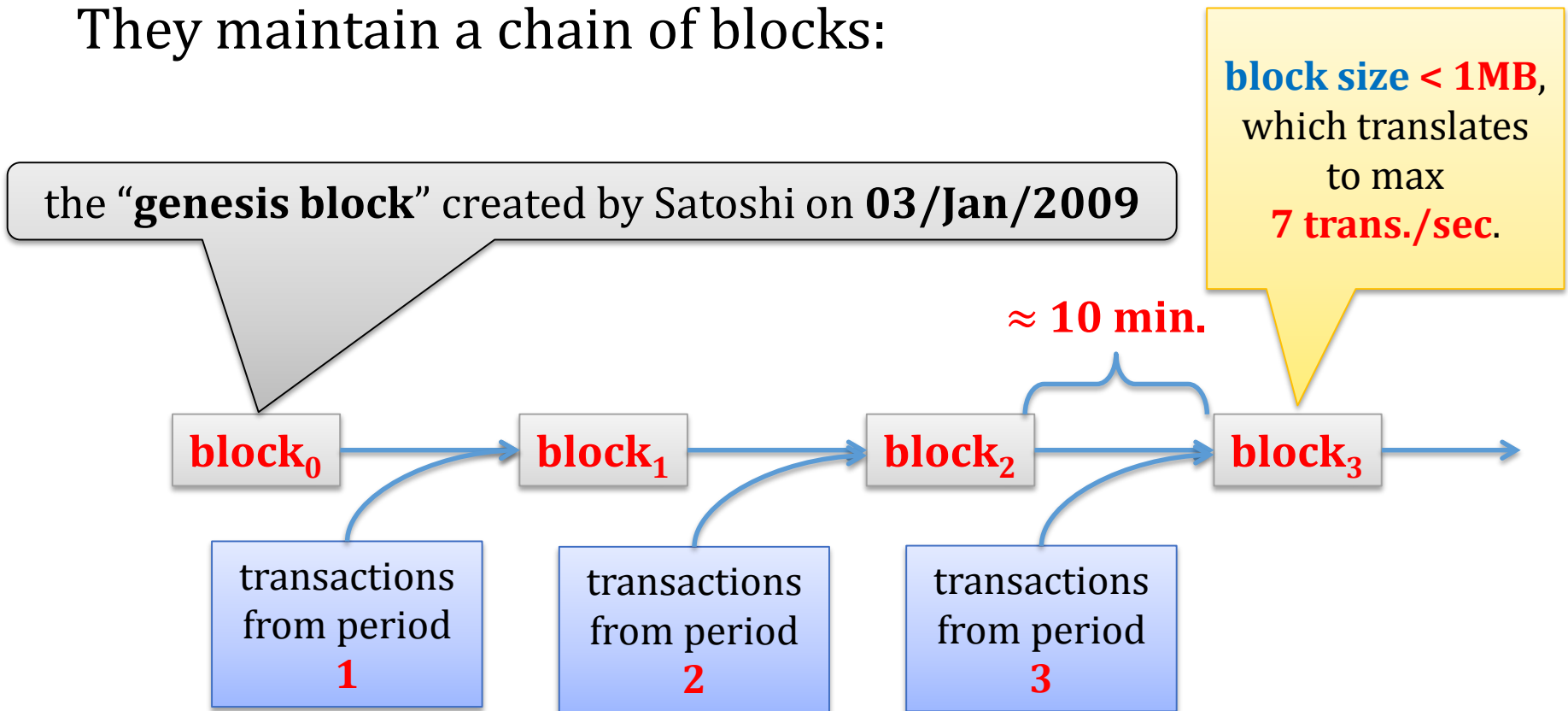
takes time **TIME(H)**

# Main idea

The users participating in the scheme are called the “miners”.

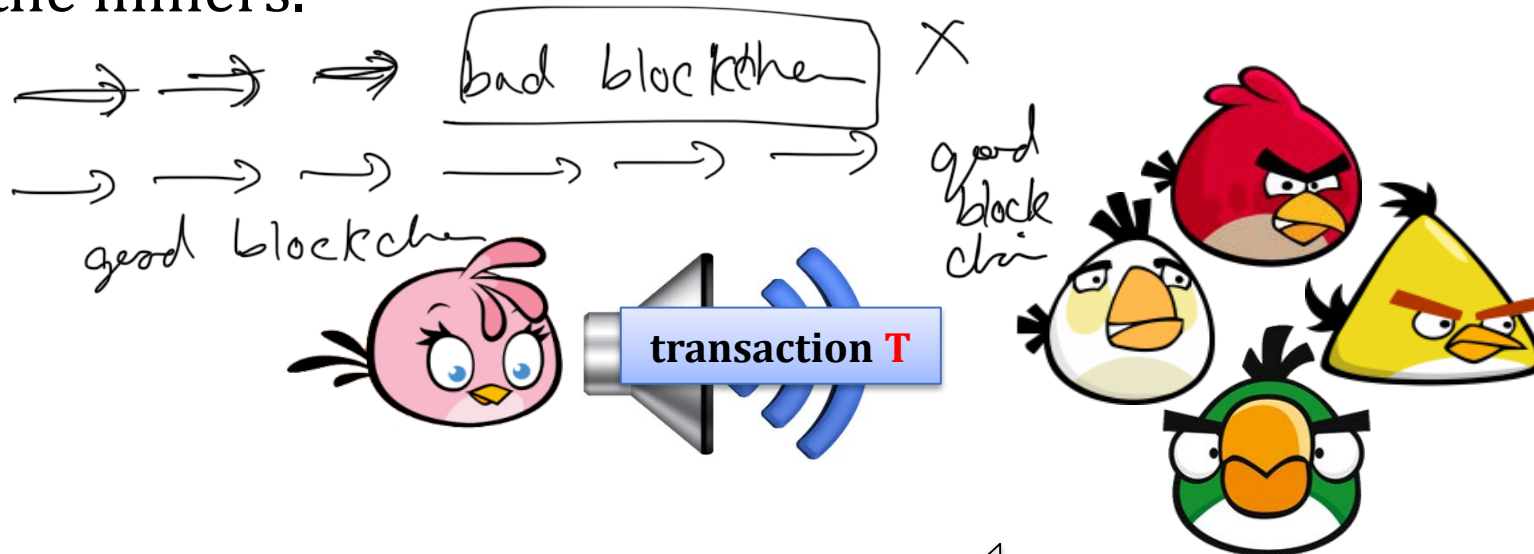


They maintain a chain of blocks:



# How to post on the board

Just broadcast (over the internet) your transaction to the miners.



And hope they will **add it to the next block**.

the miners are incentivized to do it.

**Important:**  
They **never add an invalid transaction** (e.g. double spending)

a chain with an invalid transaction is **itself not valid**, so no rational miner would do it.




# Main principles

1. It is **computationally hard** to extend the chain.

2. Once a miner finds an extension he **broadcasts it to everybody**.

3. The users will always accept "**the longest chain**" as the valid one.

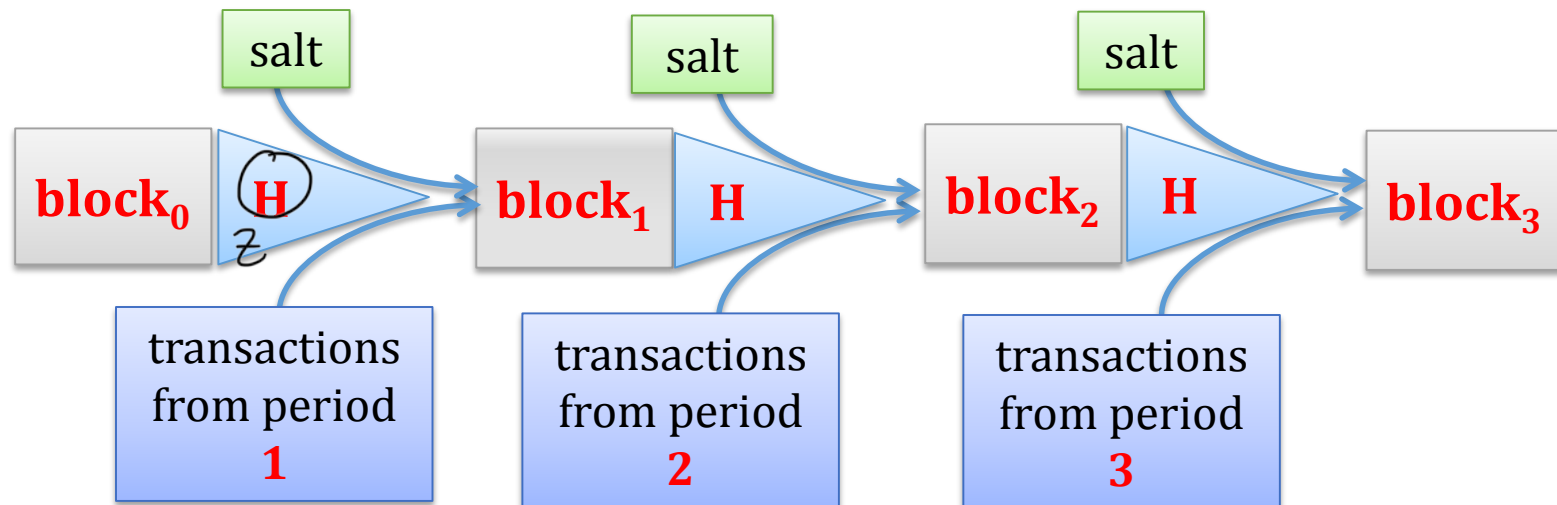


the system  
incentivizes  
them to do it

# How are the PoWs used?

**H** - hash function

more concretely in Bitcoin: **H** is **SHA256**.



**Main idea:** to extend the chain one needs to find **salt** such that

**$H(\text{salt}, H(\text{block}_i), \text{transactions})$**  starts with some number **n** of zeros

“hardness parameter”

# “Hashrate” = number of hashes computed per second

total hashrate over the last 2 years:



**Note:**

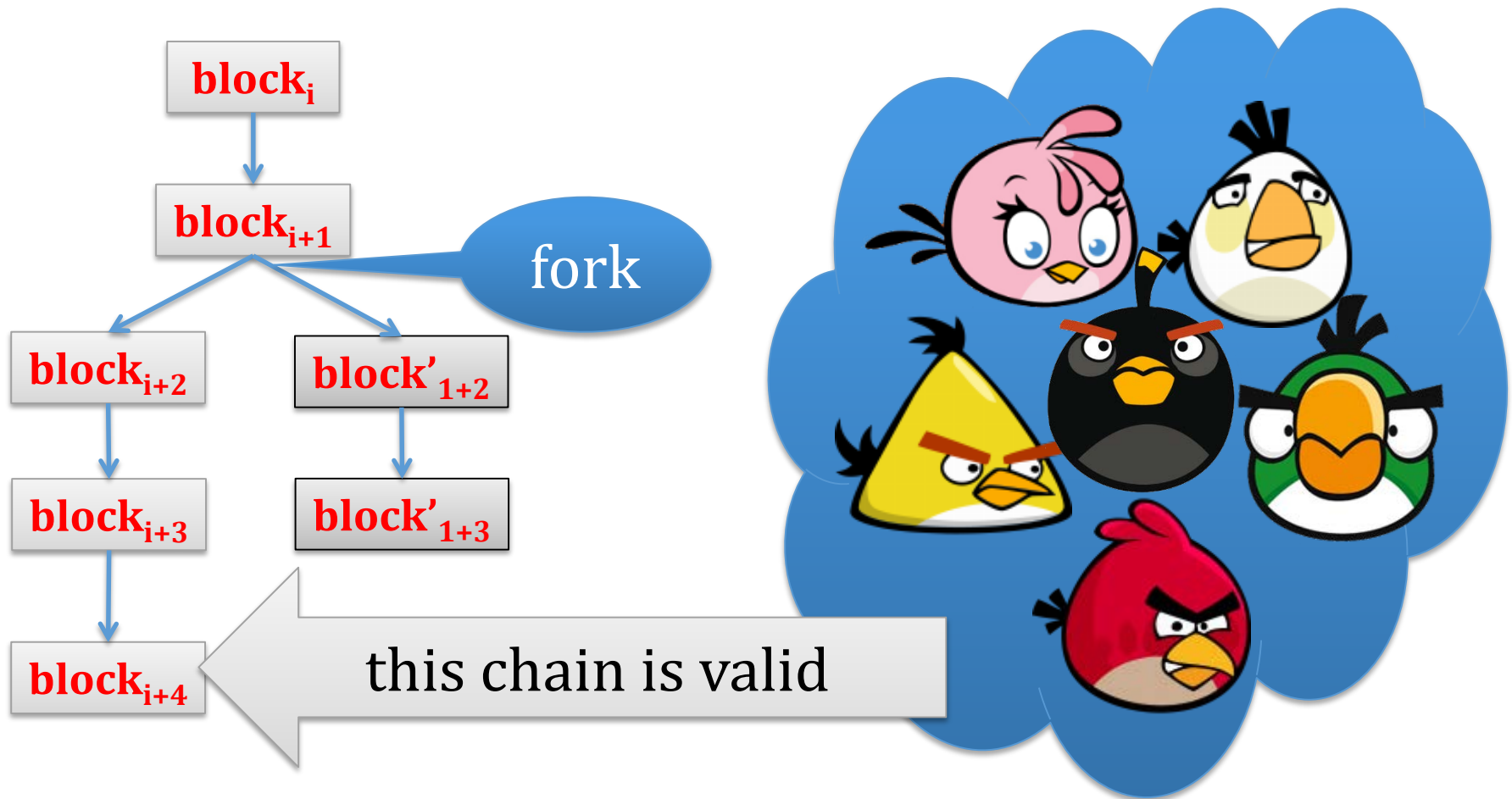
Sep 17 2013 : 990,986 GH/s  
Sep 17 2014 : 280,257,530 GH/s  
Sep 17 2015 : 385,067,688 GH/s

$2^{69}$  hash/second

$\approx 2^{58}$  hash / second

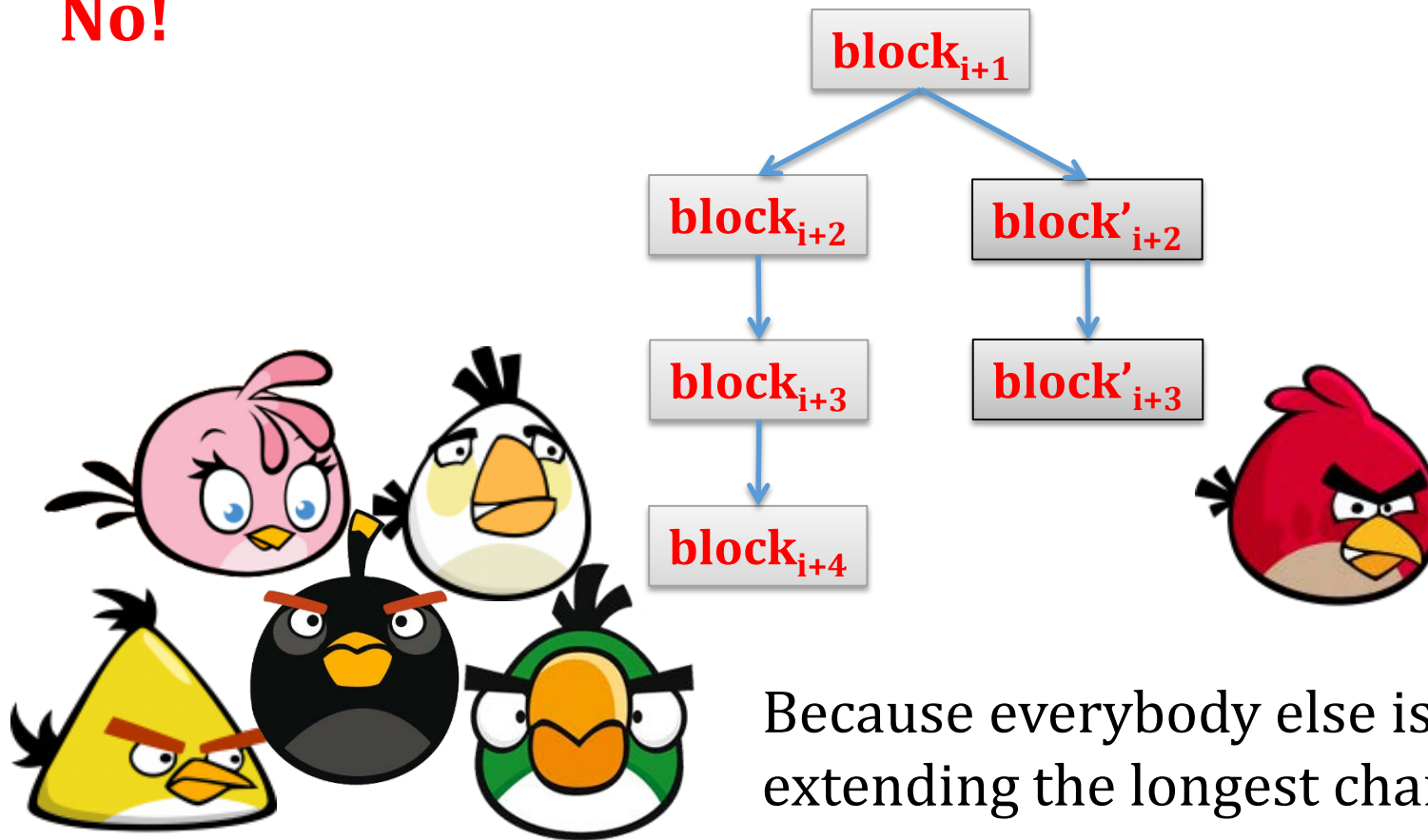
# What if there is a “fork”?

For a moment let's say: the “**longest**” chain counts.



# Does it make sense to “work” on a shorter chain?

**No!**



Because everybody else is working on extending the longest chain.

**Recall:** we assumed that the majority follows the protocol.

# How are the miners incentivized to participate in this game?

**Short answer:** they are paid (in Bitcoins) for this.  
We will discuss it in detail later...



# An important feature

Suppose everybody behaves according to the protocol  
then:

every miner  $P_i$  whose **computing power is an  $\alpha_i$ -fraction** of the total computing power **mines an  $\alpha_i$ -fraction of the blocks**.



**Intuitively** this is because:

$P_i$ 's chances of winning are **proportional to**  
the number of times  $P_i$  can compute  $H$  in a given time frame.

# Freshness of the genesis block



I didn't know the genesis block before Bitcoin was launched (**Jan 3, 2009**)

Here is a heuristic “proof”:


**Block<sub>0</sub>** contained a hash of a title from a front page of the London Times on **Jan 3, 2009**

Chancellor on brink of second bailout for banks

A recent paper that shows how to generate the genesis block in a distributed way: **[Andrychowicz, D., CRYPTO'15]**.

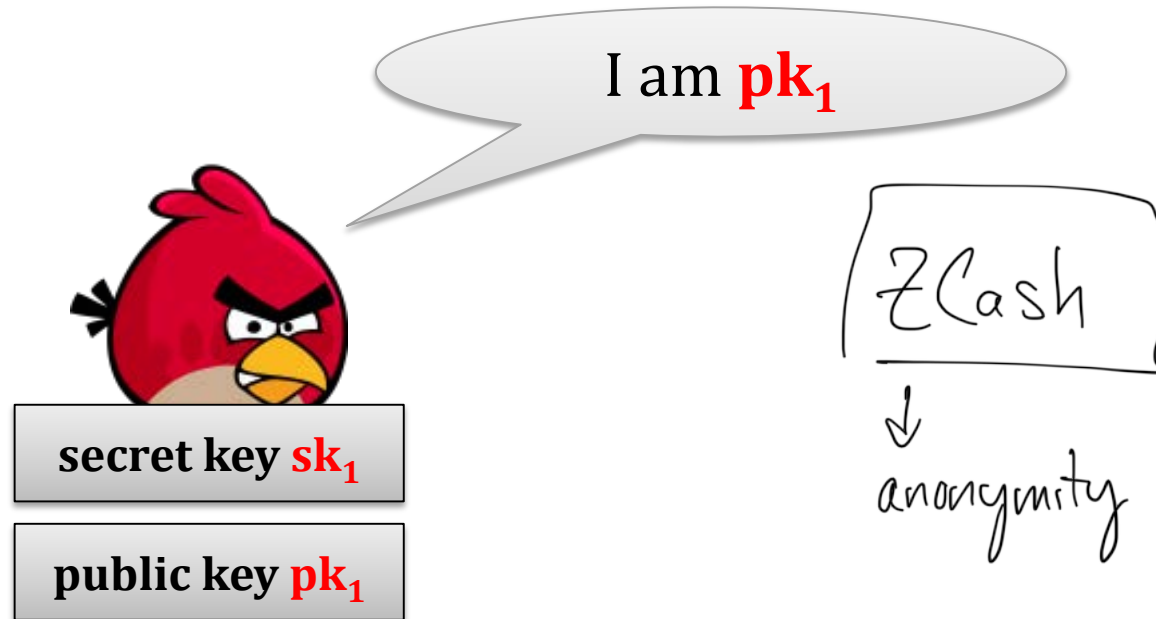


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# User identification

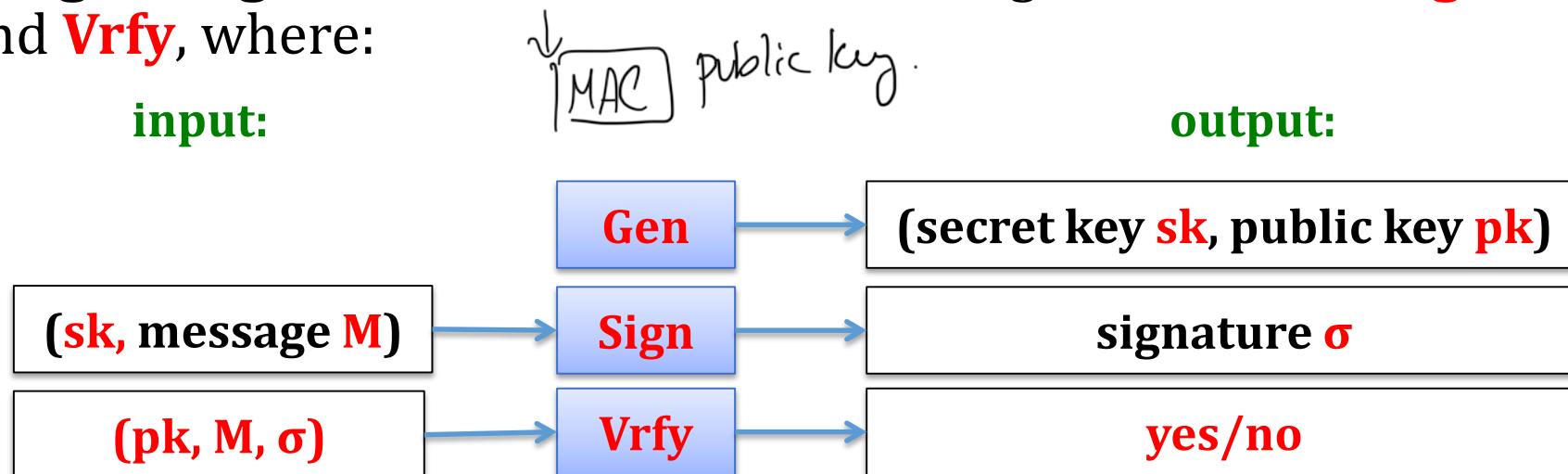
We use the digital signature schemes.



The users are identified by their public keys.

# Digital signature schemes

A **digital signature scheme** consists of algorithms **Gen**, **Sign** and **Vrfy**, where:




## Correctness:

for every  $(sk, pk) := \text{Gen}()$  and every  $M$  we have  
 $\text{Vrfy}(pk, M, \text{Sign}(sk, M)) = \text{yes}$

## Security:

“without knowing  $sk$  it is infeasible to compute  $\sigma$  such that  
 $\text{Vrfy}(pk, M, \sigma) = \text{yes}$ ”

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# Where does the money come from?

A miner who finds a new block gets a “reward” in **BTC**:

**$\approx 4$  years**

- for the first **210,000** blocks: **50 BTC**
  - for the next **210,000** blocks: **25 BTC**
  - for the next **210,000** blocks: **12.5 BTC**,
- and so on...



current reward

Note:  **$210,000 \cdot (50 + 25 + 12.5 + \dots) \rightarrow 21,000,000$**

# More details

Each block contains a transaction that **transfers the reward** to the miner.

## Advantages:

1. It provides **incentives** to be a miner.
2. It also makes the miners interested in **broadcasting new block** asap.

this view was challenged in a recent paper:

**Ittay Eyal, Emin Gun Sirer**

**Majority is not Enough: Bitcoin Mining is Vulnerable**

(we will discuss it later)

# What needs to be discussed

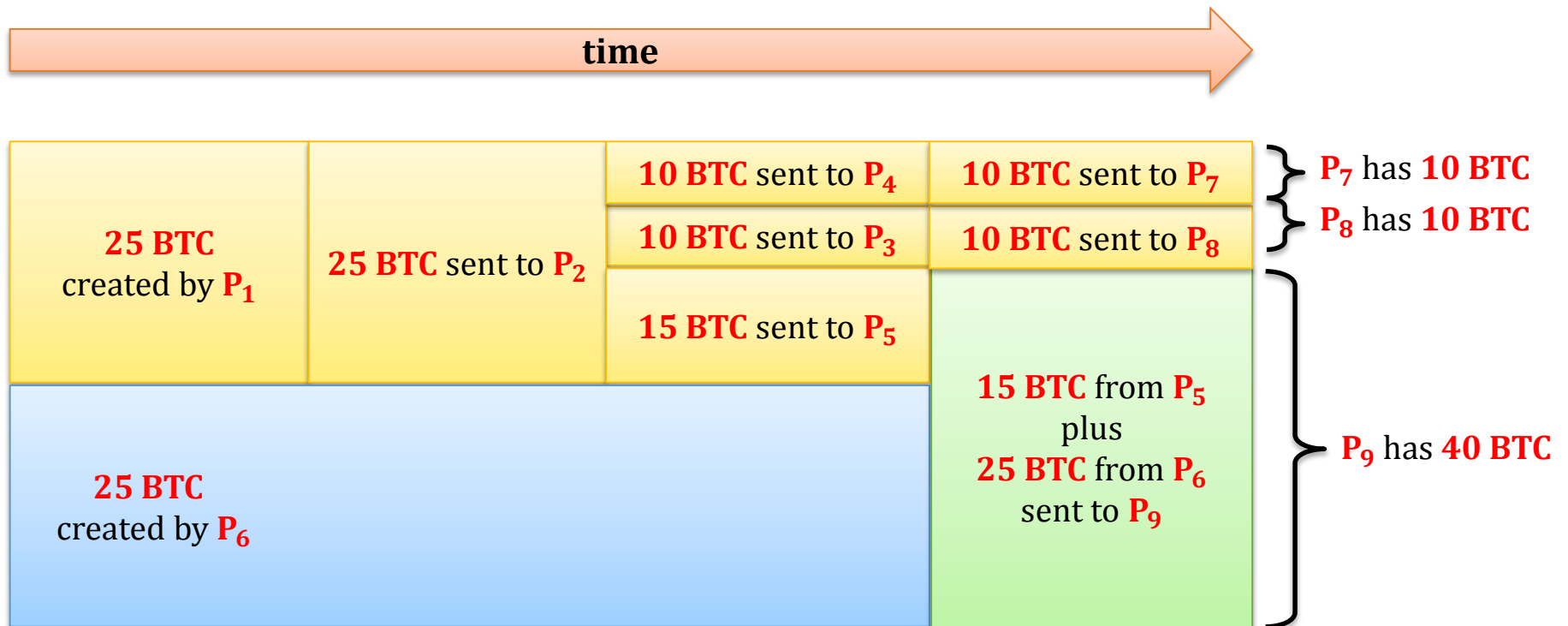
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# Bitcoin's money mechanics

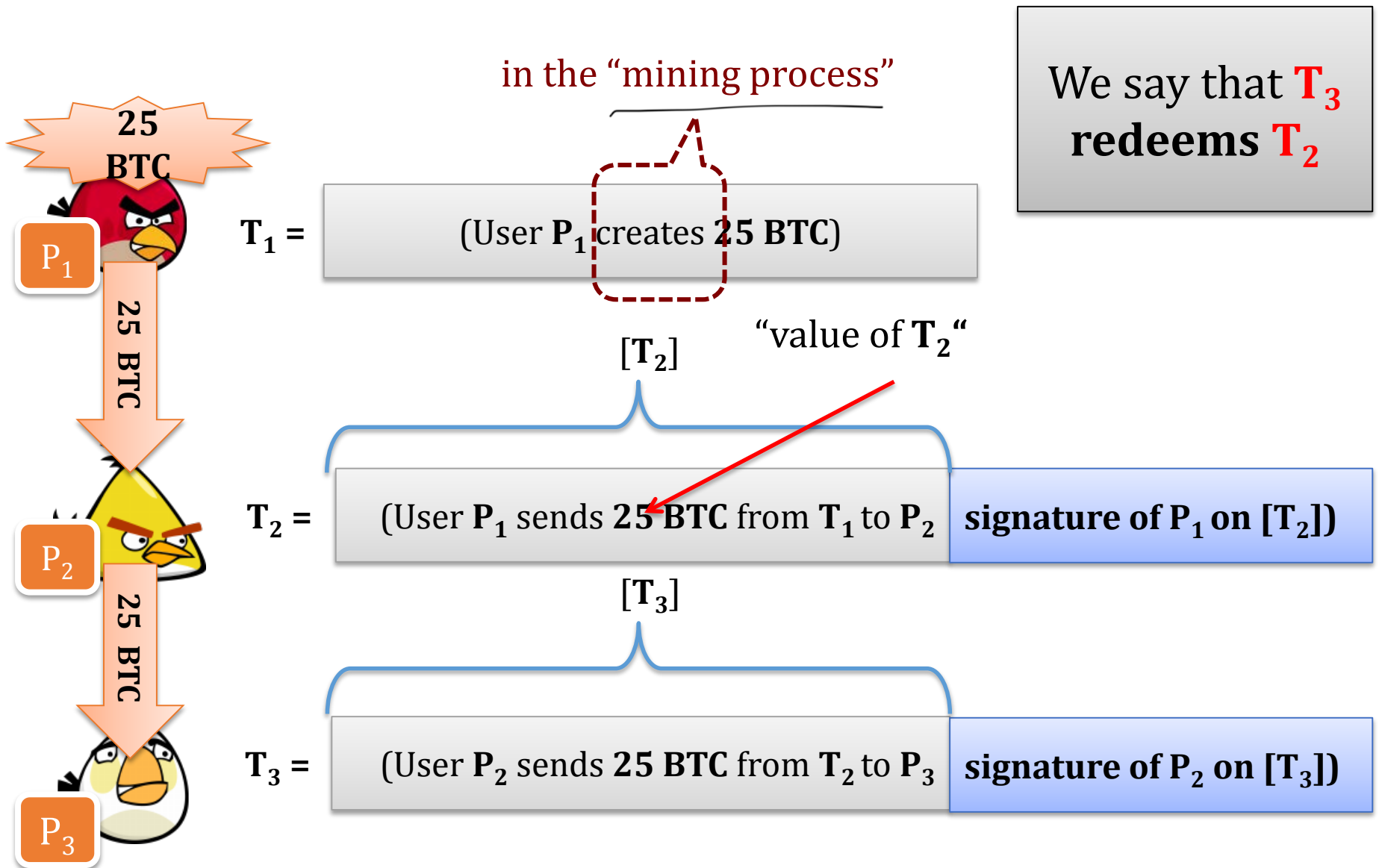
Bitcoin is “transaction based”.

Technically: there is no notion of a “coin” in Bitcoin.

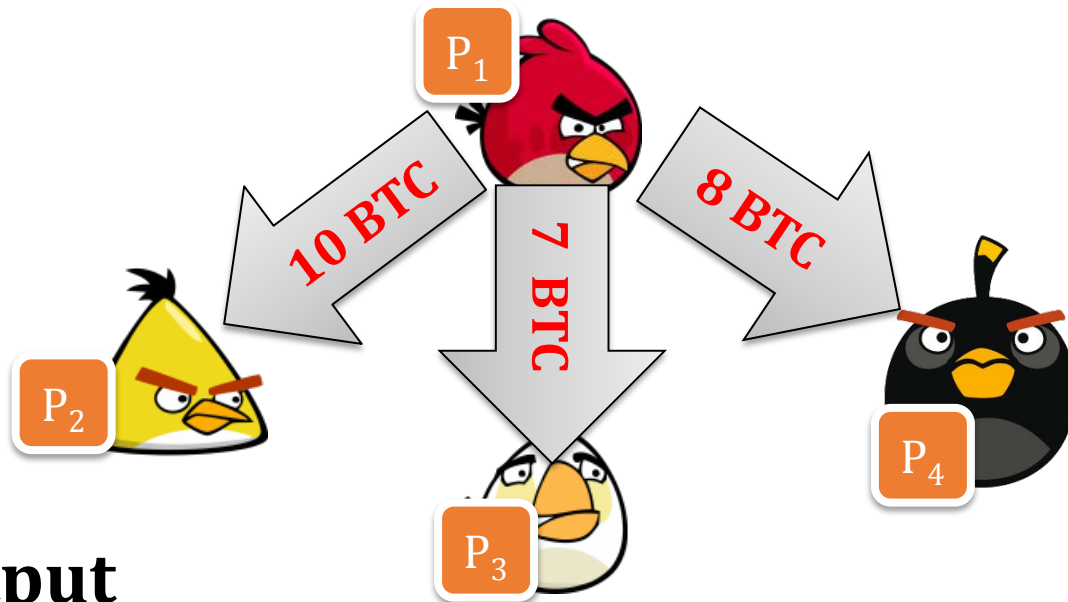




# Transaction syntax – simplified view



# How to “divide money”?



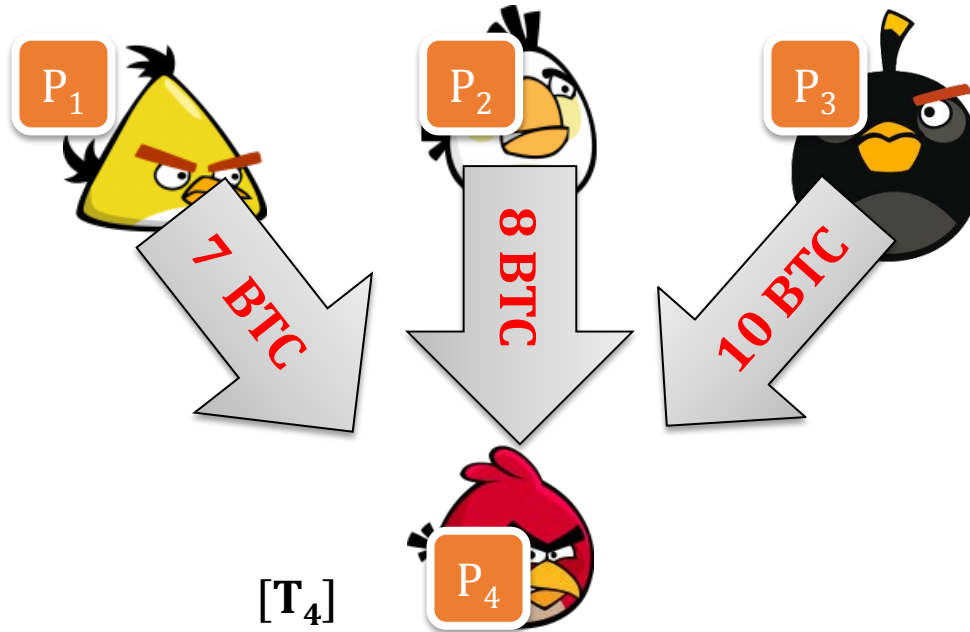
**Multi-output**  
transactions:

$[T_2]$

$T_2 =$  (User  $P_1$  sends 10 BTC from  $T_1$  to user  $P_2$ ,  
User  $P_1$  sends 7 BTC from  $T_1$  to user  $P_3$ ,  
User  $P_1$  sends 8 BTC from  $T_1$  to user  $P_4$

signature of  $P_1$  on  
 $[T_2]$ )

# Multiple inputs



$T_4 =$

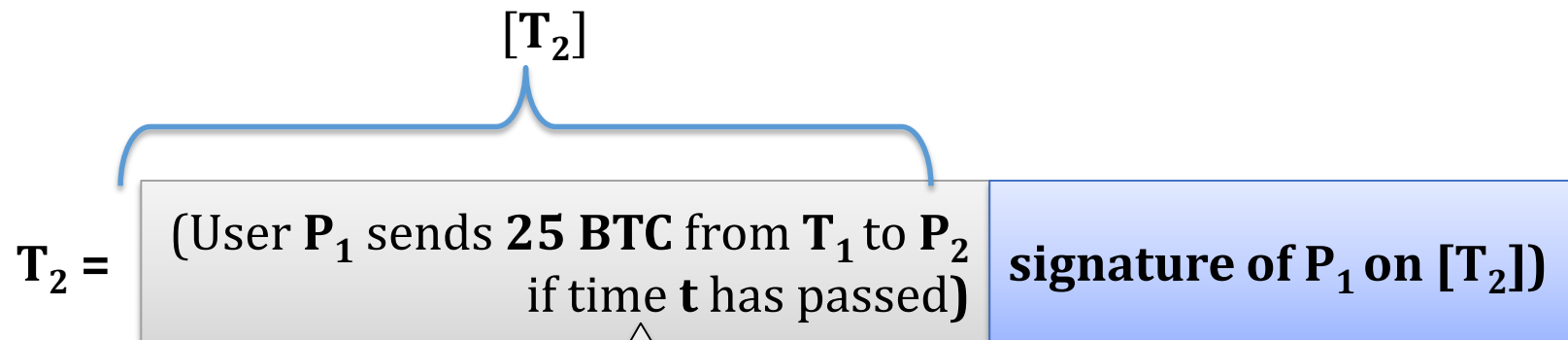
(User  $P_1$  sends 10 BTC from  $T_1$  to user  $P_4$ ,  
User  $P_2$  sends 7 BTC from  $T_2$  to user  $P_4$ ,  
User  $P_3$  sends 8 BTC from  $T_3$  to user  $P_4$ )

signature of  $P_1$  on  $[T_4]$ ,  
signature of  $P_2$  on  $[T_4]$ ,  
signature of  $P_3$  on  $[T_4]$ )

all signatures need to be valid!

# Time-locks

It is also possible to specify time **t** when a transaction becomes valid.



measured in:

- **real time**, or
- **blocks**.