

Steel Bridge Design Handbook

Design Example 2A: Two-Span Continuous Straight Composite Steel I-Girder Bridge

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FOREWORD

This handbook covers a full range of topics and design examples intended to provide bridge engineers with the information needed to make knowledgeable decisions regarding the selection, design, fabrication, and construction of steel bridges. Upon completion of the latest update, the handbook is based on the Seventh Edition of the AASHTO LRFD Bridge Design Specifications. The hard and competent work of the National Steel Bridge Alliance (NSBA) and prime consultant, HDR, Inc., and their sub-consultants, in producing and maintaining this handbook is gratefully acknowledged.

The topics and design examples of the handbook are published separately for ease of use, and available for free download at the NSBA and FHWA websites: http://www.steelbridges.org, and http://www.fhwa.dot.gov/bridge, respectively.

The contributions and constructive review comments received during the preparation of the handbook from many bridge engineering processionals across the country are very much appreciated. In particular, I would like to recognize the contributions of Bryan Kulesza with ArcelorMittal, Jeff Carlson with NSBA, Shane Beabes with AECOM, Rob Connor with Purdue University, Ryan Wisch with DeLong's, Inc., Bob Cisneros with High Steel Structures, Inc., Mike Culmo with CME Associates, Inc., Mike Grubb with M.A. Grubb & Associates, LLC, Don White with Georgia Institute of Technology, Jamie Farris with Texas Department of Transportation, and Bill McEleney with NSBA.

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16. Abstract

The purpose of this example is to illustrate the use of the AASHTO LRFD Bridge Design for the design of a continuous two span steel I-girder bridge. The design process and corresponding calculations for steel I-girders are the focus of this example, with particular emphasis placed on illustration of the optional moment redistribution procedures. All aspects of the girder design are presented, including evaluation of the following: cross-section proportion limits, constructibility, serviceability, fatigue, and strength requirements. Additionally, the weld design for the web-to-flange joint of the plate girders is demonstrated along with all applicable components of the stiffener design and cross frame member design.

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1.0 INTRODUCTION

The purpose of this example is to illustrate the use of the Seventh Edition of the AASHTO LRFD Bridge Design Specifications [1], referred to herein as AASHTO LRFD (7th Edition, 2014) for the design of a continuous steel I-girder bridge. The design process and corresponding calculations for steel I-girders are the focus of this example, with particular emphasis placed on illustration of the optional moment redistribution procedures. All aspects of the girder design are presented, including evaluation of the following: cross-section proportion limits, constructibility, serviceability, fatigue, and strength requirements. Additionally, the weld design for the web-to-flange joint of the plate girders is demonstrated along with all applicable components of the stiffener design and cross-frame design.

The moment redistribution procedures allow for a limited degree of yielding at the interior supports of continuous-span girders. The subsequent redistribution of moment results in a decrease in the negative bending moments and a corresponding increase in positive bending moments. The current moment redistribution procedures utilize the same moment envelopes as used in a conventional elastic analysis and do not require the use of iterative procedures or simultaneous equations. The method is similar to the optional provisions in previous AASHTO specifications that permitted the peak negative bending moments to be decreased by 10% before performing strength checks of the girder. However, in the present method this empirical percentage is replaced by a calculated quantity, which is a function of geometric and material properties of the girder. Furthermore, the range of girders for which moment redistribution is applicable is expanded compared to previous editions of the specifications, in that girders with slender webs may now be considered. The result of the use of these procedures is considerable economical savings. Specifically, inelastic design procedures may offer cost savings by (1) requiring smaller girder sizes, (2) eliminating the need for cover plates (which have unfavorable fatigue characteristics) in rolled beams, and (3) reducing the number of flange transitions without increasing the amount of material required in plate girder designs, leading to both material and, more significantly, fabrication cost savings.

2.0 DESIGN PARAMETERS

The bridge cross-section for the tangent, two-span (90 ft - 90 ft) continuous bridge under consideration is given below in Figure 1. The example bridge has four plate girders spaced at 10.0 ft and 3.5 ft overhangs. The roadway width is 34.0 ft and is centered over the girders. The reinforced concrete deck is 8.5 inch thick, including a 0.5 inch integral wearing surface, and has a 2.0 inch haunch thickness.

The framing plan for this design example is shown in Figure 2. As will be demonstrated subsequently, the cross frame spacing is governed by constuctibility requirements in positive bending and by moment redistribution requirements in negative bending.

The structural steel is ASTM A709, Grade 50W, and the concrete is normal weight with a 28-day compressive strength, f'_c, of 4.0 ksi. The concrete slab is reinforced with nominal Grade 60 reinforcing steel.

The design specifications are the AASHTO LRFD (7th Edition, 2014) Bridge Design Specifications. Unless stated otherwise, the specific articles, sections, and equations referenced throughout this example are contained in these specifications.

The girder design presented herein is based on the premise of providing the same girder design for both the interior and exterior girders. Thus, the design satisfies the requirements for both interior and exterior girders. Additionally, the girders are designed assuming composite action with the concrete slab.

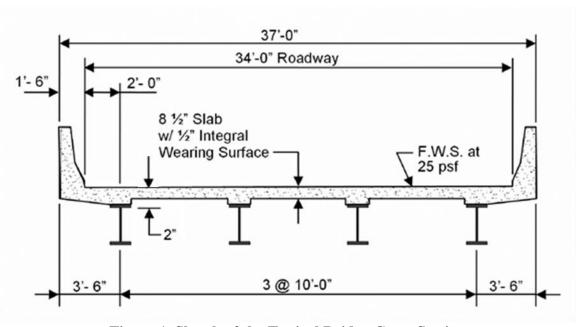


Figure 1 Sketch of the Typical Bridge Cross Section

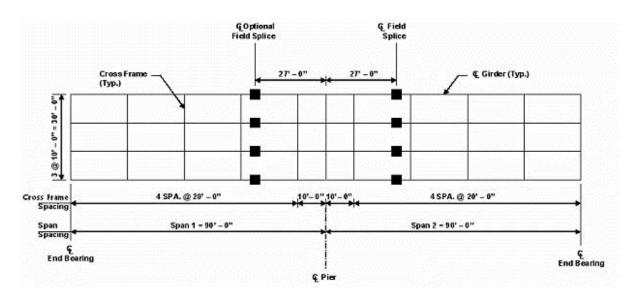


Figure 2 Sketch of the Superstructure Framing Plan

3.0 GIRDER GEOMETRY

The girder elevation is shown in Figure 3. As shown in Figure 3, section transitions are provided at 30% of the span length (27 feet) from the interior pier. The design of the girder from the abutment to 63 feet from the abutment is primarily based on positive bending moments; thus, this section of the girder is referred to as either the "positive bending region" or "Section 1" throughout this example. Alternatively, the girder geometry at the pier is controlled by negative bending moments; consequently the region of the girder extending from 0 to 27 feet on each side of the pier will be referred to as the "negative bending region" or "Section 2". The rationale used to develop the cross-sectional geometry of these sections and a demonstration that this geometry satisfies the cross-section proportion limits specified in Article 6.10.2 is presented herein.

3.1 Web Depth

Selection of appropriate web depth has a significant influence on girder geometry. Thus, initial consideration should be given to the most appropriate web depth. In the absence of other criteria the span-to-depth ratios given in Article 2.5.2.6.3 may be used as a starting point for selecting a web depth. As provided in Table 2.5.2.6.3-1, the minimum depth of the steel I-beam portion of a continuous-span composite section is 0.027L, where L is the span length. Thus, the minimum steel depth is computed as follows.

$$0.027(90 \text{ ft})(12 \text{ in./ft}) = 29.2 \text{ inches}$$

Preliminary designs were evaluated for five different web depths satisfying the above requirement. These web depths varied between 36 inches and 46 inches and in all cases girder weight decreased as web depth increased. However, the decrease in girder weight became much less significant for web depths greater than 42 inches.

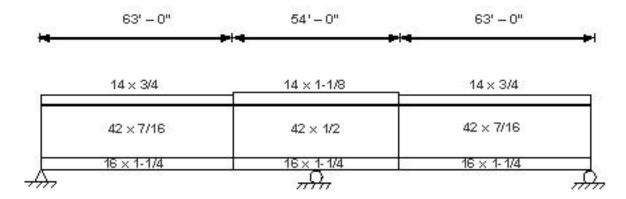


Figure 3 Sketch of the Girder Elevation

3.2 Web Thickness

The thickness of the web was selected to satisfy shear requirements at the strength limit state without the need for transverse stiffeners. This resulted in a required web thickness of 0.5 inch at

the pier and 0.4375 inch at the abutments. The designer may also want to examine the economy of using a constant 0.5 inch web throughout.

In developing the preliminary cross-section it should also be verified that the selected dimensions satisfy the cross-section proportion limits required in Article 6.10.2. The required web proportions are given in Article 6.10.2.1 where, for webs without longitudinal stiffeners, the web slenderness is limited to a maximum value of 150.

$$\frac{D}{t_{w}} \le 150$$
 Eq. (6.10.2.1.1-1)

Thus, the following calculations demonstrate that Eq. 6.10.2.1.1-1 is satisfied for both the positive and negative moment regions of the girder, respectively.

$$\frac{D}{t_{w}} = \frac{42}{0.4375} = 96 \le 150$$
 (satisfied)

$$\frac{D}{t_{yy}} = \frac{42}{0.5} = 84 \le 150$$
 (satisfied)

3.3 Flange Geometries

The width of the compression flange in the positive bending region was controlled by constructibility requirements as the flange lateral bending stresses are directly related to the section modulus of the flange about the y-axis of the girder as well as the cross-frame spacing. Various cross-frame distances were investigated and the corresponding flange width required to satisfy constructibility requirements for each case was determined. Based on these efforts it was determined that a minimum flange width of 14 in. was needed to avoid the use of additional cross-frames. Thus, this minimum width was used for the top flanges.

All other plate sizes were iteratively selected to satisfy all applicable requirements while producing the most economical girder design possible. The resulting girder dimensions are illustrated in Figure 3.

Article 6.10.2.2 specifies four flange proportions limits that must be satisfied. The first of these is intended to prevent the flange from excessively distorting when welded to the web of the girder during fabrication.

$$\frac{b_f}{2t_f} \le 12.0$$
 Eq. (6.10.2.2-1)

Evaluation of Eq. 6.10.2.2-1 for each of the three flange sizes used in the example girder is demonstrated below.

$$\frac{b_f}{2t_f} = \frac{14}{2(0.75)} = 9.33 \le 12.0$$
 (satisfied)

$$\frac{b_f}{2t_f} = \frac{14}{2(1.125)} = 6.22 \le 12.0$$
 (satisfied)

$$\frac{b_f}{2t_f} = \frac{14}{2(1.25)} = 5.6 \le 12.0$$
 (satisfied)

The second flange proportion limit that must be satisfied corresponds to the relationship between the flange width and the web depth. The ratio of the web depth to the flange width significantly influences the flexural capacity of the member and is limited to a maximum of 6, which is the maximum value for which the moment capacity prediction equations for steel I-girders are proven to be valid.

$$b_f \ge \frac{D}{6} = \frac{42}{6} = 7.0$$
 Eq. (6.10.2.2-2)

It is shown below that Eq. 6.10.2.2-2 is satisfied for both flange widths utilized in this design example.

$$b_f = 14.0 \text{ inch}$$
 (satisfied)
 $b_f = 16.0 \text{ inch}$ (satisfied)

Equation 3 of Article 6.10.2.2 limits the thickness of the flange to a minimum of 1.1 times the web thickness. This requirement is necessary to ensure that some web shear buckling restraint is provided by the flanges, and that the boundary conditions at the web-flange junction assumed in the development of the web-bend buckling and flange local buckling resistance equations are sufficiently accurate.

$$t_f \ge 1.1 t_w$$
 Eq. (6.10.2.2-3)

Evaluation of Eq. 6.10.2.2-3 for the minimum flange thickness used in combination with each of the web thicknesses utilized in the example girder is demonstrated below.

$$t_f = t_{f,min} = 0.75 \ge 1.1(0.4375) = 0.48$$
 (satisfied)

$$t_f = t_{f-min} = 1.125 \ge 1.1(0.5) = 0.55$$
 (satisfied)

Equation 6.10.2.2-4 sets limits for designed sections similar to the previsions of previous specifications. This provision prevents the use of extremely mono-symmetric sections ensuring more efficient flange proportions and a girder section that is suitable for handling during erection.

$$0.1 \le \frac{I_{yc}}{I_{vt}} \le 10$$
 Eq. (6.10.2.2-4)

where: I_{yc} = moment of inertia of the compression flange of the steel section about the vertical axis in the plane of the web (in.⁴)

 I_{yt} = moment of inertia of the tension flange of the steel section about the vertical axis in the plane of the web (in. 4)

Computing the ratio between the top and bottom flanges for the positive and negative bending regions, respectively, shows that this requirement is satisfied for the design girder.

$$0.1 \le \frac{(0.75)(14)^3/12}{(1.25)(16)^3/12} = \frac{171.5}{426.7} = 0.40 \le 10$$
 (satisfied)

$$0.1 \le \frac{(1.125)(14)^3/12}{(1.25)(16)^3/12} = \frac{257.25}{426.7} = 0.60 \le 10$$
 (satisfied)

4.0 LOADS

This example considers all applicable loads acting on the superstructure including dead loads, live loads, and wind loads as discussed below. In determining the effects of each of these loads, the approximate methods of analysis specified in Article 4.6.2 are implemented.

4.1 Dead Loads

The dead load, according to Article 3.5.1, is to include the weight of all components of the structure, appurtenances and utilities, earth cover, wearing surface, future overlays, and planned widening. Dead loads are divided into two categories: dead load of structural components and non-structural attachments (DC) and the dead load of wearing surface and utilities (DW). Alternative load factors are specified for each of these categories of dead load depending on the load combination under consideration.

4.1.1 Component Dead Load (DC)

For composite girders consideration is given to the fact that not all dead loads are applied to the composite section and the DC dead load is separated into two parts: the dead load acting on the section before the concrete deck is hardened or made composite (DC1), and the dead load acting on the composite section (DC2). DC1 is assumed to be carried by the steel section alone. DC2 is assumed to be carried by the long-term composite section. In the positive bending region the long-term composite section is comprised of the steel girder and an effective width of the concrete slab. Formulas are given in the specifications to determine the effective slab width over which a uniform stress distribution may be assumed. The effective width of the concrete slab is transformed into an equivalent area of steel by dividing the width by the ratio between the steel modulus and one-third the concrete modulus, or a modular ratio of 3n. The reduced concrete modulus is intended to account for the effects of concrete creep. In the negative bending region at the strength limit state, the composite section is comprised of the steel section and the longitudinal steel reinforcing within the effective width of the slab. At the fatigue and service limit states, the concrete deck may be considered effective in both negative and positive bending for loads applied to the composite section if certain conditions are met.

DC1 includes the girder self-weight, weight of the concrete slab (including the haunch and deck overhang taper if present), deck forms, cross-frames, and stiffeners. The unit weight for steel (0.490 k/ft³) used in this example is taken from Table 3.5.1-1, which provides approximate unit weights of various materials. Table 3.5.1-1 also lists the unit weight of normal weight concrete as 0.145 k/ft³; the concrete unit weight is increased to 0.150 k/ft³ in this example to account for the additional weight of the steel reinforcement within the concrete. The dead load of the stay-in-place forms is assumed to be 15 psf. To account for the dead load of the cross-frames, stiffeners and other miscellaneous steel details, a dead load of 0.015 k/ft is assumed. It is also assumed that these dead loads are equally distributed to all girders as permitted by Article 4.6.2.2.1 for the line-girder type of analysis implemented herein. Thus, the total DC1 loads used in this design are as computed below.

Slab = $(8.5/12) \times (37) \times (0.150)/4$	= 0.983 k/ft
Haunch (average wt/length)	= 0.017 k/ft
Overhang taper = $2 \times (1/2) \times [3.5 - (7/12)] \times (2/12) \times 0.150/4$	= 0.018 k/ft
Girder (average wt/length)	= 0.174 k/ft
Cross-frames and misc. steel	= 0.015 k/ft
Stay-in-place forms = $0.015 \text{ x } (30-3 \text{ x } (12/12))/4$	= 0.101 k/ft
Total DC1	=1.308 k/ft

DC2 is composed of the weight from the barriers, medians, and sidewalks. No sidewalks or medians are present in this example and thus the DC2 weight is equal to the barrier weight alone. The barrier weight is assumed to be equal to 520 lb/ft. Article 4.6.2.2.1 specifies that when approximate methods of analysis are applied DC2 may be equally distributed to all girders, or a larger proportion of the concrete barriers may be applied to the exterior girder which represents a more realistic distribution of these loads acting out on the deck overhangs. In this example, the barrier weight is equally distributed to all girders, resulting in the DC2 loads computed below.

Barriers =
$$(0.520 \text{ x } 2)/4 = 0.260 \text{ k/ft}$$

DC2 = 0.260 k/ft

4.1.2 Wearing Surface Dead Load (DW)

Similar to the DC2 loads, the dead load of the future wearing surface is applied to the long-term composite section and is assumed to be equally distributed to each girder. A future wearing surface with a dead load of 25 psf is assumed. Multiplying this unit weight by the roadway width and dividing by the number of girders gives the following.

Wearing surface =
$$(0.025) \times (34)/4 = 0.213 \text{ k/ft}$$

DW = 0.213 k/ft

4.2 Vehicular Live Loads

The AASHTO LRFD (7th Edition, 2014) Specifications consider live loads to consist of gravity loads, wheel load impact (dynamic load allowance), braking forces, centrifugal forces, and vehicular collision forces. Live loads are applied to the short-term composite section. In positive bending regions, the short-term composite section is comprised of the steel girder and the effective width of the concrete slab, which is converted into an equivalent area of steel by dividing the width by the modular ratio, or the ratio of the elastic moduli of the steel and the concrete. In other words, a modular ratio of n is used for short-term loads where creep effects are

not relevant. In negative bending regions at the strength limit state, the short-term composite section consists of the steel girder and the longitudinal reinforcing steel, At the fatigue and service limit states, the concrete deck may be considered effective in both negative and positive bending if certain conditions are met.

4.2.1 General Vehicular Live Load (Article 3.6.1.2)

The AASHTO LRFD (7th Edition, 2014) vehicular live loading is designated as the HL-93 loading and is a combination of the design truck or tandem plus the design lane load. The design truck, specified in Article 3.6.1.2.2, is composed of an 8-kip lead axle spaced 14 feet from the closer of two 32-kip rear axles, which have a variable axle spacing of 14 feet to 30 feet. The transverse spacing of the wheels is 6 feet. The design truck occupies a 10 feet lane width and is positioned within the design lane to produce the maximum force effects, but may be no closer than 2 feet from the edge of the design lane, except for the design of the deck overhang.

The design tandem, specified in Article 3.6.1.2.3, is composed of a pair of 25-kip axles spaced 4 feet apart. The transverse spacing of the wheels is 6 feet.

The design lane load is discussed in Article 3.6.1.2.4 and has a magnitude of 0.64 klf uniformly distributed in the longitudinal direction. In the transverse direction, the load occupies a 10 foot width. The lane load is positioned to produce extreme force effects, and therefore, need not be applied continuously.

For both negative moments between points of contraflexure and interior pier reactions a special loading is used. The loading consists of two design trucks (as described above but with the magnitude of 90% the axle weights) in addition to 90% of the lane loading. The trucks must have a minimum headway of 50 feet between the two loads. The live load moments between the points of dead load contraflexure are to be taken as the larger of the moments caused by the HL-93 loading or the special loading.

Live load shears are to be calculated only from the HL-93 loading, except for interior pier reactions, which are to be taken as the larger of the reactions due to the HL-93 loading or the special loading.

The dynamic load allowance, which accounts for the dynamic effects of force amplification, is only applied to the truck portion of the live loading, and not the lane load. For the strength and service limit states, the dynamic load allowance is taken as 33 percent, and for the fatigue limit state, the dynamic load allowance is taken as 15 percent.

4.2.2 Optional Live Load Deflection Load (Article 3.6.1.3.2)

The loading for the optional live load deflection criterion consists of the greater of the design truck, or 25 percent of the design truck plus the lane load. A dynamic load allowance of 33 percent applies to the truck portions (axle weights) of these load cases. During this check, all design lanes are to be loaded, and the assumption is made for straight-girder bridges that all components deflect equally.

4.2.3 Fatigue Load (Article 3.6.1.4)

For checking the fatigue limit state, a single design truck with a constant rear axle spacing of 30 feet is applied.

4.3 Wind Loads

Article 3.8.1.2 discusses the design horizontal wind pressure, P_D , which is used to determine the wind load on the structure. The wind pressure is computed as follows:

$$P_D = P_B \frac{V_{DZ}^2}{10,000}$$
 Eq. (3.8.1.2.1-1)

where:

 P_B = base wind pressure of 0.050 ksf for beams (Table 3.8.1.2.1-1)

 V_{DZ} = design wind velocity at design elevation, Z (mph)

In this example it is assumed the superstructure is less than 30 feet above the ground, at which the wind velocity is prescribed to equal 100 mph, which is designated as the base wind velocity, V_B . With V_{DZ} equal to the base wind velocity of 100 in Eq. 3.8.1.2.1-1 the horizontal wind pressure, P_D , is determined as follows.

$$P_D = 0.050 \frac{100^2}{10,000} = 0.050 \,\mathrm{ksf}$$

4.4 Load Combinations

The specifications define four limit states: the service limit state, the fatigue and fracture limit state, the strength limit state, and the extreme event limit state. The subsequent sections discuss each limit state in more detail; however for all limit states the following general equation from Article 1.3.2.1 must be satisfied, where different combinations of loads (i.e., dead load, wind load) are specified for each limit state.

$$\eta_D \eta_R \eta_I \Sigma \gamma_i Q_i \leq \varphi R_n = R_r$$

where:

 η_D = Ductility factor (Article 1.3.3)

 η_R = Redundancy factor (Article 1.3.4)

 η_I = Operational importance factor (Article 1.3.5)

 γ_i = Load factor

 Q_i = Force effect

 φ = Resistance factor

 $R_n = \text{Nominal resistance}$

 R_r = Factored resistance

The factors relating to ductility and redundancy are related to the configuration of the structure, while the operational importance factor is related to the consequence of the bridge being out of service. The product of the three factors results in the load modifier, η , and is limited to the range between 0.95 and 1.00. In this example, the ductility, redundancy, and operational importance factors are each assigned a value equal to one. The load factors are given in Tables 3.4.1-1 and 3.4.1-2 of the specifications and the resistance factors for the design of steel members are given in Article 6.5.4.2.

When evaluating the strength of the structure during construction, the load factor for construction loads, for equipment and for dynamic effects (i.e. temporary dead and/or live loads that act on the structure during construction) is not to be taken less than 1.5 in the Strength I load combination (Article 3.4.2). Also, the load factor for any non-integral wearing surface and utility loads may be reduced from 1.5 to 1.25 when evaluating the construction condition. The load factor for wind may be reduced to not less than 1.25 when checking the Strength III load combination during construction (Article 3.4.2). Also, for evaluating the construction condition, the load factor for temporary dead loads that act on the structure during construction is not to be taken less than 1.25 and the load factor for any non-integral wearing surface and utility loads may be reduced from 1.5 to 1.25.

Article 3.4.2.1 further states that unless otherwise specified by the Owner, primary steel superstructure components are to be investigated for maximum force effects during construction for an additional load combination consisting of the applicable DC loads and any construction loads that are applied to the fully erected steelwork. For this additional load combination, the load factor for DC and construction loads including dynamic effects (if applicable) is not to be taken less than 1.4. For steel superstructures, the use of higher-strength steels, composite construction, and limit-states design approaches in which smaller factors are applied to dead load force effects than in previous service-load design approaches, have generally resulted in lighter members overall. To ensure adequate stability and strength of primary steel superstructure components during construction, an additional strength limit state load combination is specified for the investigation of loads applied to the fully erected steelwork (i.e., for investigation of the deck placement sequence and deck overhang effects).

5.0 STRUCTURAL ANALYSIS

The AASHTO LRFD (7th Edition, 2014) specifications allow the designer to use either approximate (e.g., line girder) or refined (e.g., grid or finite element) analysis methods to determine force effects; the acceptable methods of analysis are detailed in Section 4 of the specifications. In this design example, the line girder approach is employed to determine the girder moment and shear envelopes. Using the line girder approach, vehicular live load force effects are determined by first computing the force effects due to a single truck or loaded lane and then by multiplying these forces by multiple presence factors, live-load distribution factors, and dynamic load allowance factors as detailed below.

5.1 Multiple Presence Factors (Article 3.6.1.1.2)

Multiple presence factors account for the probability of multiple lanes on the bridge being loaded simultaneously. These factors are specified for various numbers of loaded lanes in Table 3.6.1.1.2-1 of the specifications. There are two exceptions when multiple presence factors are not to be applied. These are when (1) distribution factors are calculated using the tabulated empirical equations given in Article 4.6.2.2 as these equations are already adjusted to account for multiple presence effects and (2) when determining fatigue truck moments, since the fatigue analysis is only specified for a single truck. Thus, for the present example, the multiple presence factors are only applicable when distribution factors are computed using the lever rule or the special analysis for the exterior girders at the strength and service limit states as demonstrated below.

5.2 Live-Load Distribution Factors (Article 4.6.2.2)

The distribution factors approximate the amount of live load (i.e., percentage of a truck or lane load) distributed to a given girder. These factors are computed based on a combination of empirical equations and simplified analysis procedures. Empirical equations are provided in Article 4.6.2.2.1 of the specifications and are specifically developed based on the location of the girder (i.e. interior or exterior), the force effect considered (i.e., moment or shear), and the bridge type. These equations are valid only if specific parameters of the bridge are within the ranges specified in the tables given in Article 4.6.2.2.1. If the limits are not satisfied, a more refined analysis must be performed. This design example satisfies all limits for use of the empirical distribution factors, and therefore, the analysis using the approximate equations follows.

Distribution factors are a function of the girder spacing, slab thickness, span length, and the stiffness of the girder, which depends on the proportions of the section. Since the factor depends on girder proportions that are not initially known, the stiffness term may be assumed to be equal to one for preliminary design. In this section, calculation of the distribution factors is presented based on the girder proportions previously shown in Figure 3.

5.2.1 Live-Load Lateral Distribution Factors – Positive Flexure

In positive bending regions, the stiffness parameter required for the distribution factor equations, K_g , is determined based on the cross section in Figure 4.

$$K_g = n(I + Ae_g^2)$$
 Eq. (4.6.2.2.1-1)

where:

n = modular ratio

I = moment of inertia of the steel girder

A = area of the steel girder

e_g = distance between the centroid of the girder and centroid of the slab

The required section properties of the girder (in addition to other section properties that will be relevant for subsequent calculations) are determined as follows.

$$e_g = 8.0 / 2 + 2.0 + 26.01 - 0.75 = 31.26$$
 in.

n = 8

$$K_g = n(I + Ae_g^2) = 8(15,969 + 48.88(31.26)^2) = 509,871 \text{ in.}^4$$

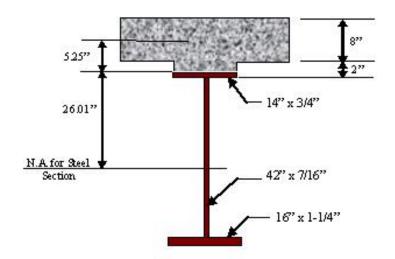


Figure 4 Sketch of Section 1, Positive Bending Region

Table 1 Section 1 Steel Only Section Properties

Component	A	D	Ad	Ad^2	Io	I
Top Flange 14" x ¾"	10.50	21.38	224.5	4797	0.49	4798
Web 42" x ⁷ / ₁₆ "	18.38				2701	2701
Bottom Flange 16" x 1-1/4"	20.00	-21.63	-432.5	9353	2.60	9356
	48.88		-208.0			16,855
				-4.2	26(208)=	<u>-886</u>
					$I_{NA} =$	15,969 in ⁴
$d_{8} = \frac{-208.0}{48.88} = -4.26 \text{ in.}$						
$d_{\text{TOP OF STEEL}} = 21.75 + 4.26 = 26.01 \text{ in.}$ $S_{\text{TOP OF STEEL}} = \frac{15,969}{26.01} = 614.0 \text{ in.}^3$						
$d_{BOT OF STEEL} = 22.25 - 4.26 = 17.99 \text{ in}$ $S_{BOT OF STEEL} = \frac{15,969}{19.99} = 887.7 \text{ in.}^3$						

5.2.1.1 Interior Girder – Strength and Service Limit States

For interior girders, computation of the distribution factors for the strength and service limit states is based on the empirical equations given in Article 4.6.2.2.2 as described below.

5.2.1.1.1 Bending Moment

The empirical equations for distribution of live load moment at the strength and service limit states are given in Table 4.6.2.2.2b-1. Alternative expressions are given for one loaded lane and multiple loaded lanes, where the maximum of the two equations governs as shown below. It is noted that the maximum number of lanes possible for the 34 feet roadway width considered in this example is two lanes.

DF =
$$0.06 + \left(\frac{S}{14}\right)^{0.4} \left(\frac{S}{L}\right)^{0.3} \left(\frac{K_g}{12.0Lt_s^3}\right)^{0.1}$$
 for one-lane loaded

where:

 $\begin{array}{lll} S & = & girder \ spacing \\ L & = & span \ length \\ t_s & = & slab \ thickness \\ K_g & = & stiffness \ term \end{array}$

DF =
$$0.06 + \left(\frac{10.0}{14}\right)^{0.4} \left(\frac{10.0}{90}\right)^{0.3} \left(\frac{509871}{12.0(90)(8.0)^3}\right)^{0.1} = 0.508 \text{ lanes}$$

DF =
$$0.075 + \left(\frac{S}{9.5}\right)^{0.6} \left(\frac{S}{L}\right)^{0.2} \left(\frac{K_g}{12.0Lt^3}\right)^{0.1}$$
 for two or more lanes loaded

DF = $0.075 + \left(\frac{10.0}{9.5}\right)^{0.6} \left(\frac{10.0}{90}\right)^{0.2} \left(\frac{509871}{12.0(90)(8.0)^3}\right)^{0.1} = 0.734 \text{ lanes}$ (governs)

Thus, the controlling distribution factor for moment of an interior girder in the positive moment region at the strength or service limit state is 0.734 lanes.

5.2.1.1.2 Shear

The empirical equations for distribution of live load shear in an interior girder at the strength and service limit states are given in Table 4.6.2.2.3a-1. Similar to the equations for moment given above, alternative expressions are given based on the number of loaded lanes.

DF =
$$0.36 + \frac{S}{25.0}$$
 for one lane loaded

DF =
$$0.36 + \frac{10.0}{25.0} = 0.760$$
 lanes

DF =
$$0.2 + \frac{S}{12} - \left(\frac{S}{35}\right)^2$$
 for two or more lanes loaded

DF =
$$0.2 + \frac{10.0}{12} - \left(\frac{10.0}{35}\right)^2 = 0.952$$
 lanes (governs)

5.2.1.2 Exterior Girder – Strength and Service Limit States

The live load distribution factors for an exterior girder for checking the strength limit state are determined as the governing factors calculated using a combination of the lever rule, approximate formulas, and a special analysis assuming that the entire cross section deflects and rotates as a rigid cross-section. Each method is illustrated below.

5.2.1.2.1 Bending Moment

Lever Rule:

As specified in Table 4.6.2.2.2d-1, the lever rule is one method used to determine the distribution factor for the exterior girder for the case of one-lane loaded. The lever rule assumes the deck is hinged at the interior girder, and statics is employed to determine the percentage of the truck weight resisted by the exterior girder, i.e., the distribution factor. It is specified that the truck is to be placed such that the closest wheel is two feet from the barrier or curb, which results in the truck position shown in Figure 5 for the present example. The calculated reaction of the exterior

girder is multiplied by the multiple presence factor for one lane loaded, m_1 , to determine the distribution factor.

$$DF = \left(0.5 + 0.5 \left(\frac{10 - 6}{10}\right)\right) m_{1}$$

 $m_1 = 1.20$ (from Table 3.6.1.1.2-1)

$$DF = 0.7 \times 1.2 = 0.840$$
 lanes

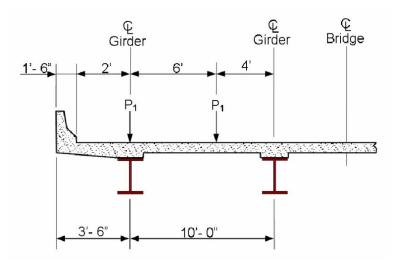


Figure 5 Sketch of the Truck Location for the Lever Rule

Modified Interior Girder Distribution Factor:

For the case of two or more lanes loaded, a modification factor, e, to be applied to the distribution factor for the interior girder is found in Table 4.6.2.2.2d-1 and is given below.

$$e = 0.77 + \frac{d_e}{9.1}$$

In the above equation d_e is the distance between the center of the exterior girder and the interior face of the barrier or curb in feet. Thus, for the present example d_e is equal to 2.

$$e = 0.77 + \frac{2.0}{9.1} = 0.990$$

Modifying the interior girder distribution factor for moment for the case of two or more lanes loaded by the factor, e, gives the following:

$$DF = 0.990(0.734) = 0.727$$
 lanes

Special Analysis:

The special analysis assumes the entire bridge cross-section behaves as a rigid cross-section rotating about the transverse centerline of the structure and is discussed in the commentary of Article 4.6.2.2.2d. The reaction on the exterior beam is calculated from the following equation:

$$R = \frac{N_L}{N_b} + \frac{X_{ext} \sum_{b}^{N_L} e}{\sum_{b}^{N_b} x^2}$$
 Eq. (C4.6.2.2.2d-1)

where:

 N_L = number of lanes loaded

 N_b = number of beams or girders

 X_{ext} = horizontal distance from center of gravity of the pattern of girders to the exterior girder (ft.)

e = eccentricity of a design truck or a design lane load from the center of gravity of the pattern of girders (ft.)

x = horizontal distance from the center of gravity of the pattern of girders to each girder (ft.)

Figure 6 shows the truck locations for the special analysis. Here it is shown that the maximum number of trucks that may be placed on half of the cross-section is two. Thus, the calculation of the distribution factors using the special analysis procedure for one loaded lane and two loaded lanes proceeds as follows (the appropriate multiple presence factors, MPF, that are applied in each case are shown):

DF = 1.2
$$\left(\frac{1}{4} + \frac{(15)(12)}{2((15)^2 + (5)^2)}\right) = 0.732$$
 for one lane loaded (Note, MPF = 1.2)

DF =
$$1.0 \left(\frac{2}{4} + \frac{(15)(12+0)}{2((15)^2 + (5)^2)} \right) = 0.860$$
 for two lanes loaded (Note, MPF = 1.0)

DF = 0.860 governs

Based on the computations for the exterior girder distribution factors for moment in the positive bending region shown above, it is determined that the controlling factor for this case is equal to 0.860 lanes, which is based on the special analysis with two lanes loaded. Compared to the interior girder distribution factor for moment in the positive bending region, which was computed to be 0.734 lanes, it is shown that the exterior girder distribution factor is larger, and

therefore controls the bending strength design at the strength and service limit states in the positive bending region.

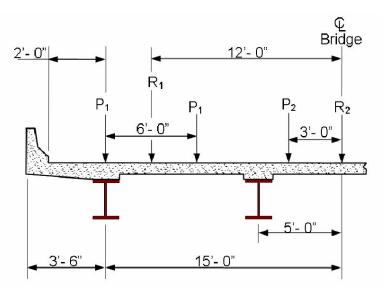


Figure 6 Sketch of the Truck Locations for the Special Analysis

5.2.1.2.2 Shear

The distribution factors computed above using the lever rule, approximate formulas, and special analysis are also applicable to the distribution of shear.

Lever Rule:

The above computations demonstrate that for the case of one-lane loaded the distribution factor is equal to 0.840 lanes based on the lever rule.

$$DF = 0.840$$
 lanes

Modified Interior Girder Distribution Factor:

For the case of two or more lanes loaded, the shear modification factor is computed using the following formula, Table 4.6.2.2.3b-1:

$$e = 0.60 + \frac{d_e}{10.0}$$

$$e = 0.60 + \frac{2}{10.0} = 0.800$$
 lanes

Applying this modification factor to the previously computed interior girder distribution factor for shear for two or more lanes loaded gives the following:

$$DF = 0.800(0.952) = 0.762$$
 lanes

Special Analysis:

It was demonstrated above that the special analysis yields the following distribution factors for one lane and two or more lanes loaded, respectively:

DF = 0.732 lanes

DF = 0.860 lanes (governs)

Thus, the controlling distribution factor for shear in the positive bending region of the exterior girder is 0.860 lanes, which is less than that of the interior girder. Thus, the interior girder distribution factor of 0.952 lanes controls the shear design in the positive bending region.

5.2.1.3 Fatigue Limit State

As stated in Article 3.6.1.1.2, the fatigue distribution factor is based on one lane loaded, and does not include the multiple presence factor, since the fatigue loading is specified as a single truck load. Because the distribution factors calculated from the tabulated empirical equations incorporate the multiple presence factors, the fatigue distribution factors are equal to the strength distribution factors divided by the multiple presence factor for one lane loaded, as described subsequently.

5.2.1.3.1 Bending Moment

Upon reviewing the moment distribution factors for one lane loaded computed above, it is determined that the maximum distribution factor results from the lever rule calculations. Dividing this distribution factor of 0.840 lanes by the multiple presence factor for one lane loaded results in the following distribution factor for fatigue moment in the positive bending region.

Exterior Girder, DF = 0.840 / 1.20 = 0.700 lanes

Interior Girder, DF = 0.508 / 1.20 = 0.423 lanes

5.2.1.3.2 Shear

Similarly, based on the above distribution factors for shear due to one lane loaded, the controlling distribution factor is calculated by again dividing the lever rule distribution factor by the multiple presence factor.

Exterior Girder, DF = 0.840 / 1.20 = 0.700 lanes

Interior Girder, DF = 0.760 / 1.20 = 0.633 lanes

5.2.1.4 Distribution Factor for Live-Load Deflection

Article 2.5.2.6.2 states that all design lanes must be loaded when determining the live load deflection of the structure. In the absence of a refined analysis, for straight-girder bridges, an approximation of the live load deflection can be obtained by using a distribution factor computed assuming that all girders deflect equally with the appropriate multiple presence factor applied. The controlling case occurs when two lanes are loaded, and the calculation of the corresponding distribution factor is shown below.

DF =
$$m \left(\frac{N_L}{N_h} \right) = 1.0 \left(\frac{2}{4} \right) = 0.500 \text{ lanes}$$

Table 2 summarizes the governing distribution factors for the positive bending region.

Table 2 Positive Bending Region Distribution Factors (lanes)

	Interior Girder	Exterior Girder
Bending Moment	0.734	0.860
Shear	0.952	0.860
Fatigue (Bending Moment)	0.423	0.700
Fatigue (Shear)	0.633	0.700
Deflection	0.500	0.500

5.2.2 Live-Load Lateral Distribution Factors – Negative Flexure

Many of the distribution factors are the same in both the positive and negative bending regions. This section demonstrates the computation of the distribution factors that are unique to the negative bending region. Specifically, the distribution factor for bending moment in the interior girder at the strength and service limit states is directly influenced by to the girder proportions. As in the above calculations for the positive moment region, this process begins with determining the stiffness parameter, K_g , of the section. The cross section for the negative bending region is shown in Figure 7. The section properties of the girder are determined as follows.

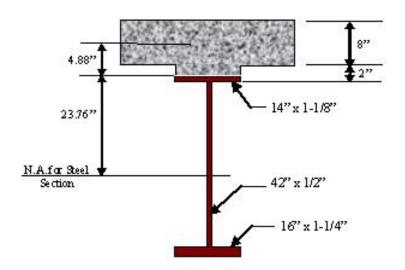


Figure 7 Sketch of Section 2, Negative Bending Region

Table 3 Section 2 Steel Only Section Properties

Component	Α	D	Ad	Ad^2	I _o	I
Top Flange 14" x 1-1/8"	15.75	21.56	340	7323	1.66	7325
Web 42" x 1/2"	21.00				3087	3087
Bottom Flange 16" x 1-1/4"	20.00	-21.63	-432.5	9352	2.60	9355
	56.75		-92.5			19,767
				-1.	63(92.5)=	<u>-151</u>
					$I_{NA} =$	19,616 in ⁴
$\underline{d}_{s} = \frac{-92.5}{56.75} = -1.63 \text{ in.}$						
$\underline{\text{d}_{\text{TOP OF STEEL}}} = 22.125 + 1.63 = 23.76 \text{ in.}$ $S_{\text{TOP OF STEEL}} = \frac{19,616}{23.76} = 825.6 \text{ in.}^3$						
$d_{\text{BOT OF STEEL}} = 22.25 - 1.63 = 20.62 \text{ in.}$ $S_{\text{BOT OF STEEL}} = \frac{19,616}{20.62} = 951.3 \text{ in.}^3$						

$$e_g = 8.0 \ / \ 2 + 2.0 + 23.76 - 1.125 = 28.64$$
 in.
$$n = 8$$

$$K_g = n(I + Ae_g^2) = 8(19,616 + 56.75(28.64)^2) = 529,321 \text{ in.}^4$$

As discussed above, the distribution factors for bending moment in interior girders at the strength and service limit states are computed based on the tabulated empirical equations given in Article 4.6.2.2.2.

The applicable equations for moment distribution factors from Table 4.6.2.2.2b-1 are as shown below.

DF =
$$0.06 + \left(\frac{S}{14}\right)^{0.4} \left(\frac{S}{L}\right)^{0.3} \left(\frac{K_g}{12.0Lt_s^3}\right)^{0.1}$$
 for one lane loaded

DF =
$$0.06 + \left(\frac{10.0}{14}\right)^{0.4} \left(\frac{10.0}{90.0}\right)^{0.3} \left(\frac{529,321}{12.0(90.0)(8.0)^3}\right)^{0.1} = 0.510 \text{ lanes}$$

DF =
$$0.075 + \left(\frac{S}{9.5}\right)^{0.6} \left(\frac{S}{L}\right)^{0.2} \left(\frac{K_g}{12.0 Lt_s^3}\right)^{0.1}$$
 for two or more lanes loaded

DF = 0.075+
$$\left(\frac{10.0}{9.5}\right)^{0.6} \left(\frac{10.0}{90.0}\right)^{0.2} \left(\frac{529,321}{12.0(90.0)(8.0)^3}\right)^{0.1} = 0.737 \text{ lanes}$$

Table 4 summarizes the distribution factors for the negative bending region, where it is shown that the exterior girder controls all aspects of the design except for shear at the strength and service limit states.

	Interior Girder	Exterior Girder
Bending Moment	0.737	0.860
Shear	0.952	0.860
Fatigue (Bending Moment)	0.425	0.700
Fatigue (Shear)	0.633	0.700
Deflection	0.500	0.500

Table 4 Negative Bending Region Distribution Factors

5.2.3 Dynamic Load Allowance

The dynamic effects of the truck loading are taken into consideration by the dynamic load allowance, IM. The dynamic load allowance, which is discussed in Article 3.6.2 of the specifications, accounts for the hammering effect of the wheel assembly and the dynamic response of the bridge. IM is only applied to the design truck or tandem, not the lane loading. Table 3.6.2.1-1 specifies IM equal to 1.33 for the strength, service, and live load deflection evaluations, while IM of 1.15 is specified for the fatigue limit state.

6.0 ANALYSIS RESULTS

6.1 Moment and Shear Envelopes

Figures 8 through 11 show the moment and shear envelopes for this design example, which are based on the data presented in Tables 5 through 11. These figures show distributed moments for the exterior girder and distributed shears for an interior girder, which are the controlling girders for each force effect, based on the distribution factors computed above. For loads applied to the composite section, the envelopes shown are determined based on the composite section properties assuming the concrete deck to be effective over the entire span length.

As previously mentioned, the live load in the positive bending region between the points of dead load contraflexure is the result of the HL-93 loading. In the negative bending region between the points of dead load contraflexure, the moments are the larger of the moments due to the HL-93 loading and the special negative-moment loading, which is composed of 90 percent of both the truck-train moment and lane loading moment.

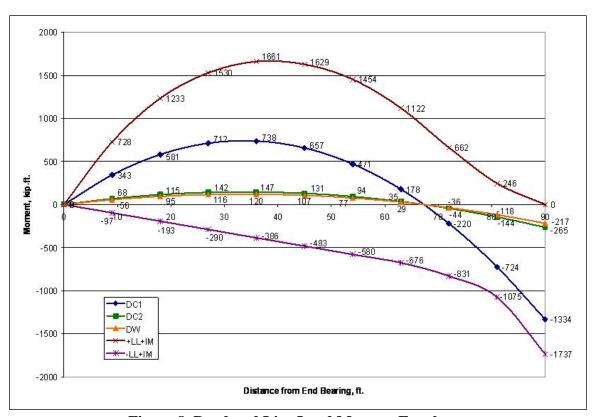


Figure 8 Dead and Live Load Moment Envelopes

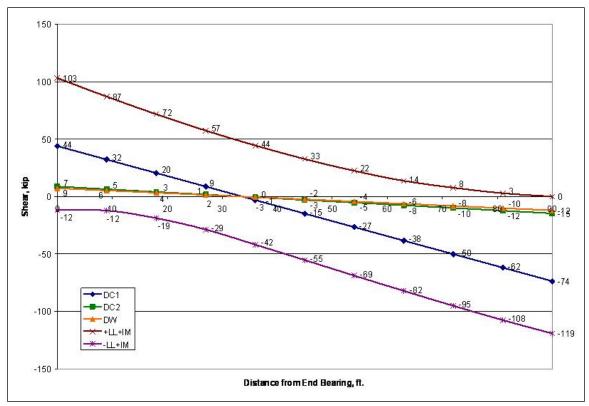


Figure 9 Dead and Live Load Shear Envelopes

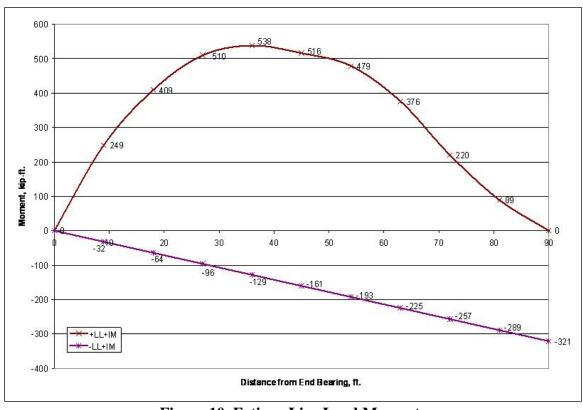


Figure 10 Fatigue Live Load Moments

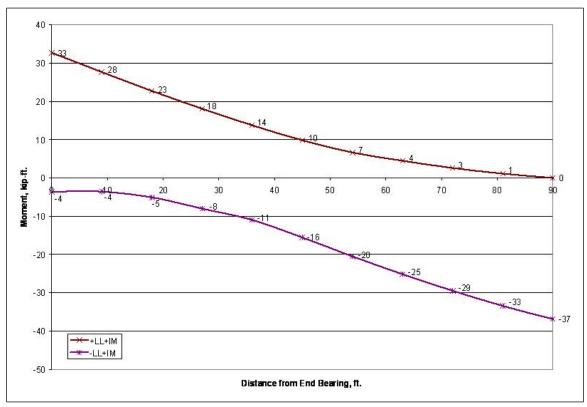


Figure 11 Fatigue Live Load Shears

Table 5 Unfactored and Undistributed Moments (kip-ft)

	Non-Com. Dead	Com. Dead	Wearing Surf.	Truck Load		Truck Load Lane Load		Tandem		Double Truck		Double Tandem	
Span 1	DC1	DC2	DW	pos.	neg.	pos.	neg.	pos.	neg.	pos.	neg.	pos.	neg.
0.00	0	0	0	0	0	0	0	0	0	0	0	0	0
0.10	343	68	56	485	-60	201	-33	381	-44	0	0	0	0
0.20	581	115	95	816	-120	349	-65	652	-87	0	0	0	0
0.30	712	142	116	1002	-180	446	-98	817	-131	0	0	0	0
0.40	738	147	120	1083	-240	491	-131	883	-174	0	0	0	0
0.50	657	131	107	1059	-300	485	-163	866	-218	0	0	0	0
0.60	471	94	77	951	-359	426	-196	779	-261	0	0	0	0
0.70	178	35	29	743	-419	316	-229	625	-305	0	0	0	0
0.80	-220	-44	-36	463	-479	154	-261	423	-348	0	-479	0	-611
0.90	-724	-144	-118	148	-539	30	-385	192	-392	0	-755	0	-687
1.00	-1334	-265	-217	0	-599	0	-653	0	-436	0	-1196	0	-764

Table 6 Unfactored and Undistributed Live Load Moments (kip-ft)

	vehicle		special	standard	1.33 Vehicle +			
Span 1	positive	negative	negative	negative	Lane positive	Distribution Factors	Positive	Negative
0.00	0	0	0	0	0	0.86	0	0
0.10	485	-60	-29	-112	846	0.86	728	-97
0.20	816	-120	-59	-225	1434	0.86	1233	-193
0.30	1002	-180	-88	-337	1779	0.86	1530	-290
0.40	1083	-240	-118	-449	1932	0.86	1661	-386
0.50	1059	-300	-147	-562	1894	0.86	1629	-483
0.60	951	-359	-176	-674	1691	0.86	1454	-580
0.70	743	-419	-206	-786	1304	0.86	1122	-676
0.80	463	-479	-967	-899	770	0.86	662	-831
0.90	192	-539	-1250	-1102	285	0.86	246	-1075
1.00	0	-599	-2020	-1450	0	0.86	0	-1737

Table 7 Strength I Load Combination Moments (kip-ft)

Tuble / Strongth I Loud Compiliation (170ments (mp 10)										
				1.75 (LL+IM)		Stre	ngth I			
Span 1	1.25 DC1	1.25 DC2	1.5 DW	positive	negative	positive	negative			
0.00	0	0	0	0	0	0	0			
0.10	429	85	84	1273	-169	1871	429			
0.20	726	144	142	2158	-338	3170	674			
0.30	890	177	174	2677	-507	3918	734			
0.40	922	183	180	2907	-676	4192	609			
0.50	821	163	161	2850	-845	3995	300			
0.60	588	117	115	2545	-1014	3365	-194			
0.70	223	44	44	1963	-1183	2274	-873			
0.80	-275	-55	-54	1159	-1455	775	-1838			
0.90	-905	-180	-177	430	-1882	-833	-3144			
1.00	-1668	-332	-326	0	-3039	-2326	-5365			

Table 8 Service II Load Combination Moments (kip-ft)

				1.3 (LL+IM)		Sen	vice II
Span 1	1.0 DC1	1.0 DC2	1.0 DW	positive	negative	positive	negative
0.00	0	0	0	0	0	0	0
0.10	343	68	56	946	-126	1413	342
0.20	581	115	95	1603	-251	2394	540
0.30	712	142	116	1989	-377	2959	593
0.40	738	147	120	2160	-502	3164	502
0.50	657	131	107	2117	-628	3012	267
0.60	471	94	77	1890	-753	2531	-113
0.60	471	94	77	1890	-753	2531	-113
0.70	178	35	29	1458	-879	1701	-636
0.80	-220	-44	-36	861	-1081	561	-1380
0.90	-724	-144	-118	319	-1398	-667	-2384

Table 9 Unfactored and Undistributed Shears (kip)

	Non-Com. Dead	Com. Dead	Wearing Surf.	Truck Load		Lane	Load	Tandem	
Span 1	DC1	DC2	DW	positive	negative	positive	negative	positive	negative
0.00	44	9	7	63	-7	25	-4	49	-5
0.10	32	6	5	54	-7	20	-4	42	-5
0.20	20	4	3	45	-10	15	-5	36	-11
0.30	9	2	1	37	-18	11	-7	30	-17
0.40	-3	-1	0	29	-26	8	-9	25	-23
0.50	-15	-3	-2	22	-34	5	-12	19	-29
0.60	-27	-5	-4	15	-42	3	-16	14	-34
0.70	-38	-8	-6	10	-50	2	-20	10	-38
0.80	-50	-10	-8	5	-56	1	-25	6	-43
0.90	-62	-12	-10	2	-62	0	-30	2	-46
1.00	-74	-15	-12	0	-67	0	-36	0	-49

Table 10 Unfactored and Undistributed Live Load Shears (kip)

	vel	nicle	(1.33 V Vehi	cle + V.Lane)		Live	Load
Span 1	positive	negative	positive	negative	Distribution	Positive	Negative
0.00	63	-7	108	-12	0.952	103	-12
0.10	54	-7	91	-13	0.952	87	-12
0.20	45	-11	75	-20	0.952	72	-19
0.30	37	-18	60	-30	0.952	57	-29
0.40	29	-26	47	-44	0.952	44	-42
0.50	22	-34	34	-58	0.952	33	-55
0.60	15	-42	24	-72	0.952	22	-69
0.70	10	-50	14	-86	0.952	14	-82
0.80	6	-56	8	-100	0.952	8	-95
0.90	2	-62	3	-113	0.952	3	-108
1.00	0	-67	12	-108	0.952	12	-103

Table 11 Strength I Load Combination Shear (kip)

				1.75 (LL+IM)		Strei	ngth I
Span 1	1.25 DC1	1.25 DC2	1.5 DW	positive	negative	positive	negative
0.00	55	11	11	181	-21	257	56
0.10	40	8	8	152	-21	209	35
0.20	26	5	5	126	-33	161	3
0.30	11	2	2	101	-50	116	-35
0.40	-4	-1	-1	78	-73	72	-79
0.50	-19	-4	-4	57	-97	31	-123
0.60	-33	-7	-6	39	-120	-7	-167
0.70	-48	-10	-9	24	-144	-43	-211
0.80	-63	-12	-12	13	-167	-74	-254
0.90	-77	-15	-15	5	-188	-103	-296
1.00	-92	-18	-18	0	-209	-128	-337

6.2 Live Load Deflection

As indicated in Article 3.6.1.3.2, control of live-load deflection is optional. Evaluation of this criterion is based on the flexural rigidity of the short-term composite section and consists of two load cases: deflection due to the design truck, and deflection due to the design lane plus 25 percent of the design truck. The dynamic load allowance of 33 percent is applied to the design truck load only for both loading conditions. For this example, the live load is distributed using a distribution factor of 0.500 lanes calculated earlier.

The maximum deflection due to the design truck is 0.917 inches. Applying the impact and distribution factors gives the following.

$$\Delta_{\text{LL+IM}} = 0.500 \text{ x } 1.33 \text{ x } 0.917 = 0.610 \text{ in.}$$
 (governs)

The maximum deflection due to lane load only is 0.475 inches. Therefore, the deflection due to 25% of the design truck plus the lane loading is equal to the following:

$$\Delta_{\text{LL+IM}} = 0.500 \text{ (1.33 x 0.25 x 0.917 + 0.475)} = 0.390 \text{ in.}$$

Thus the governing deflection equal to 0.610 inch will be used to assess the girder design based on the live-load deflection criterion.

7.0 LIMIT STATES

As discussed previously, there are four limit states applicable to the design of steel I-girders. Each of these limit states is described below.

7.1 Service Limit State (Articles 1.3.2.2 and 6.5.2)

The intent of the Service Limit State is to ensure the satisfactory performance and rideability of the bridge structure by preventing localized yielding. For steel members, these objectives are intended to be satisfied by limiting the maximum levels of stress that are permissible. The optional live-load deflection criterion is also included in the service limit state and is intended to ensure user comfort.

7.2 Fatigue and Fracture Limit State (Article 1.3.2.3 and 6.5.3)

The intent of the Fatigue and Fracture Limit State is to control crack growth under cyclic loading. This is accomplished by limiting the stress range to which steel members are subjected. The permissible stress range varies for various design details and member types. The fatigue limit state also restricts the out-of-plane flexing of the web. Additionally, fracture toughness requirements are stated in Article 6.6.2 of the specifications and are dependent on the temperature zone.

7.3 Strength Limit State (Articles 1.3.2.4 and 6.5.4)

The strength limit state ensures the design is stable and has adequate strength when subjected to the highest load combinations considered. The bridge structure may experience structural damage (e.g., permanent deformations) at the strength limit state, but the integrity of the structure is preserved.

The suitability of the design must also be investigated to ensure adequate strength and stability during each construction phase. The deck casting sequence has a significant influence on the distribution of stresses within the structure. Therefore, the deck casting sequence should be considered in the design and specified on the plans to ensure uniformity between predicted and actual stresses. In addition, lateral flange bending stresses resulting from forces applied to the overhang brackets during construction should also be considered during the constructibility evaluation.

7.4 Extreme Event Limit State (Articles 1.3.2.5 and 6.5.5)

The extreme event limit state is to ensure the structure can survive a collision, earthquake, or flood. The collisions investigated under this limit state include the bridge being struck by a vehicle, vessel, or ice flow. This limit state is not addressed in this design example.

8.0 SAMPLE CALCULATIONS

This example presents sample calculations for the design of positive and negative bending sections of the girders for the strength, fatigue and fracture, and service limit states. In addition, calculations evaluating the constructibility of the bridge system are included and the optional provisions for moment redistribution are presented. Also presented are the cross-frame design, stiffener design, and weld design. The moment and shear envelopes provided in Figs. 8 through 11 are referenced in the following calculations.

8.1 Section Properties

The section properties for Section 1 and Section 2 are first calculated and will be routinely used in the subsequent evaluations of the various code checks. The structural slab thickness is taken as the slab thickness minus the thickness of the integral wearing surface (8 inches) and the modular ratio (n) is taken to be 8 in these calculations.

8.1.1 Section 1 – Positive Bending Region

Section 1 represents the positive bending region and was previously shown in Figure 4. The longitudinal reinforcement is neglected in the computation of these section properties.

8.1.1.1 Effective Flange Width (Article 4.6.2.6)

Article 4.6.2.6 of the AASHTO LRFD (7th Edition, 2014) Specifications governs the determination of the effective flange width of the concrete slab when designing composite sections.

For the interior girders of this example, b_{eff} in the positive bending region is determined as one-half the distance to the adjacent girder on each side of the girder being analyzed.

$$b_{\text{eff}} = \frac{120}{2} + \frac{120}{2} = 120.0 \text{in}.$$

For the exterior girders of this example, b_{eff} in the positive bending region is determined as one-half the distance to the adjacent girder plus the full overhang width.

$$b_{eff} = \frac{120}{2} + 42 = 102.0in.$$

The exterior girder has both a smaller effective width and a larger live load distribution factor than the interior girder; therefore the moment design of the positive bending region is controlled by the exterior girder.

8.1.1.2 Elastic Section Properties: Section 1

As discussed above, the section properties considered in the analysis of the girder vary based on the loading conditions. Specifically, live loads are applied to the short-term composite section, where the modular ratio of 8 is used in the computations. Alternatively, dead loads are applied to the long-term composite section. The long-term composite section accounts for the reduction in strength that may occur in the deck over time due to creep effects. This is reflected in the section property calculations through use of a modular ratio equal to 3 times the typical modular ratio (3n), or in this example, 24. The effective width of the deck is divided by the appropriate modular ratio for each case in the determination of the composite section properties. The section properties for the short-term and long-term composite sections are computed below, in Tables 12 and 13. Recall that the section properties for the steel section (girder alone) were previously computed for the purpose of determining live load distribution factors.

Table 12 Section 1 Short Term Composite (n) Section Properties (Exterior Girder)

		<u>`</u>	<u>, </u>			
Component	A	d	Ad	Ad^2	Ιο	I
Steel Section	48.88		-208.0			16,855
Concrete Slab (8"x 102"/8)	102.0	27.00	2,754	74,358	544	74,902
	150.88		2,546			91,757
				-16.87(2	2,546)=	<u>-42,951</u>
						48,806 in ⁴
$d_{5} = \frac{2,546}{150.88} = 16.87 \text{in}.$						
$\underline{d}_{\text{TOP OF STEEL}} = 21.75 - 16.87 = 4.88$	3 in.	STOP OF STE	$EL = \frac{48,806}{4.88}$	= 10,00	1 in. ³	
d_{BOT} of STEEL = 22.25 + 16.87 = 39.	12 in.		S _{BOT} of ste	$EEL = \frac{48,806}{39.12}$	= 1,248	in. ³

Table 13 Section 1 Long Term Composite (3n) Section Properties (Exterior Girder)

Component	A	d	Ad	Ad ²	Io	I				
Steel Section	48.88		-208.0			16,855				
Concrete Slab (8"x 102"/24)	34.00	27.00	918.0	24,786	181.3	24,967				
	82.88		710.0			41,822				
				-8.57	(710.0) =	<u>-6,085</u>				
						35,737 in ⁴				
$d_{5} = \frac{710}{82.88} = 8.57 \text{in}.$										
$d_{\text{TOP OF STEEL}} = 21.75 - 8.57 = 13.18 \text{ in.}$ $S_{\text{TOP OF STEEL}} = \frac{35,737}{13.18} = 2,711 \text{ in.}^3$										
d _{BOT OF STEEL} = $22.25 + 8.57 = 30.82 \text{ in.}$ S _{BOT OF STEEL} = $\frac{35,737}{30.82} = 1,159 \text{ in.}^3$										

8.1.1.3 Plastic Moment: Section 1

The plastic moment M_p is the resisting moment of an assumed fully-yielded cross-section and may be determined for sections in positive flexure using the procedure outlined in Table D6.1-1 as demonstrated below. The longitudinal deck reinforcement is conservatively neglected in these computations. The plastic forces acting in the slab (P_s) , compression flange (P_c) , web (P_w) , and tension flange (P_t) are first computed.

$$\begin{split} P_s &= 0.85 f^* c b_s t_s &= 0.85 (4.0) (102) (8) &= 2,774 \text{ kips} \\ P_c &= F_{yc} b_c t_c &= (50) (14) (0.75) &= 525 \text{ kips} \\ P_w &= F_{yw} D t_w &= (50) (42) (0.4375) &= 919 \text{ kips} \\ P_t &= F_{yt} b_t t_t &= (50) (16) (1.25) &= 1,000 \text{ kips} \end{split}$$

The plastic forces for each element of the girder are then compared to determine the location of the plastic neutral axis (PNA). The position of the PNA is determined by equilibrium; i.e., no net axial force when considering the summation of plastic forces. Table D.6.1-1 provides seven cases, with accompanying conditions for use, to determine the location of the PNA and subsequently calculate the plastic moment.

Following the conditions set forth in Table D6.1-1, the PNA is generally located as follows:

CASE I
$$P_t + P_w \ge P_c + P_s$$

$$1,000 + 919 \ge 525 + 2,774$$

$$1,919 < 3,299 \quad \text{Therefore, PNA is not in the web}$$

$$\text{CASE II}$$

$$P_t + P_w + P_c \ge P_s$$

$$1,000 + 919 + 525 \ge 2,774$$

$$2,774 \text{ kips} < 2,611 \text{ kips} \quad \text{Therefore, PNA is not in the top flange}$$

Therefore, the plastic neutral axis is in the concrete deck and \bar{y} is computed using the following equation derived from that provided in Table D6.1-1 when deck reinforcement is ignored:

$$\overline{y} = (t_s) \left[\frac{P_c + P_w + P_t}{P_s} \right]$$

$$\overline{y} = (8.0) \left[\frac{525 + 919 + 1000}{2774} \right] = 7.05$$
 inches from the top of the concrete slab

The plastic moment M_p is then calculated using the following equation derived from that provided in Table D6.1-1 when deck reinforcement is ignored.

$$\mathbf{M}_{p} = \left(\frac{y^{2} P_{s}}{2t_{s}}\right) + \left[P_{c} d_{c} + P_{w} d_{w} + P_{t} d_{t}\right]$$

The distance from the PNA to the centroid of the compression flange, web, and tension flange (respectively) is as follows:

$$\begin{aligned} &d_c = 8.0 + 2.0 - 0.5(0.75) - 7.05 = 2.575 \text{ in.} \\ &d_w = 8.0 + 2.0 + 0.5(42.0) - 7.05 = 23.95 \text{ in.} \\ &d_t = 8.0 + 2.0 + 42.0 + 0.5(1.25) - 7.05 = 45.013 \text{ in.} \end{aligned}$$

Substitution of these distances and the above computed plastic forces, into the preceding equation, gives the following:

$$\mathbf{M}_{p} = \left(\frac{(7.05)^{2}(2774)}{2(8.0)}\right) + \left[(525)(2.575) + (919)(23.95) + (1000)(45.013)\right]$$

$$M_p = 76,992 \text{ k-in} = 6,416 \text{ k-ft}.$$

8.1.1.4 Yield Moment: Section 1

The yield moment, which is the moment causing first yield in either flange (neglecting flange lateral bending), is determined according to the provisions specified in Article D6.2.2 of the specifications. This computation method for the yield moment recognizes that different stages of loading (e.g. composite dead load, non-composite dead load, and live load) act on the girder when different cross-sectional properties are applicable. The yield moment is determined by solving for M_{AD} using Equation D6.2.2-1 (given below) and then summing M_{D1} , M_{D2} , and M_{AD} , where, M_{D1} , M_{D2} , and M_{AD} are the factored moments applied to the noncomposite, long-term composite, and short-term composite section, respectively.

$$F_{yt} = \frac{M_{D1}}{S_{NC}} + \frac{M_{D2}}{S_{LT}} + \frac{M_{AD}}{S_{ST}}$$
 Eq. (D6.2.2-1)

Due to the significantly higher section modulus of the short-term composite section about the top flange, compared to the short-term composite section modulus taken about the bottom flange, the minimum yield moment results when using the bottom flange section moduli.

Computation of the yield moment for the bottom flange is thus demonstrated below. First the known quantities are substituted into Equation D6.2.2-1 to solve for M_{AD} .

$$50 = 1.0 \left[\frac{1.25(738)(12)}{887.7} + \frac{1.25(147)(12) + 1.50(120)(12)}{1,159} + \frac{M_{AD}}{1,248} \right]$$

$$M_{AD} = 42,136 \text{ k-in.} = 3,511 \text{ k-ft.}$$

 M_y is then determined by applying the applicable load factors and summing the dead loads and M_{AD} .

$$M_v = 1.25(738) + 1.25(147) + 1.50(120) + 3,511 = 4,797 \text{ k-ft}$$
 Eq. (D6.2.2-2)

8.1.2 Section 2 – Negative Bending Region

This section details the calculations to determine the section properties of the composite girder in the negative bending region, which was previously shown in Figure 7.

8.1.2.1 Effective Flange Width (Article 4.6.2.6)

As discussed previously, the effective flange width for interior girders is computed as one-half the distance to the adjacent girder one each side of the girder being analyzed.

$$b_{\text{eff}} = \frac{120}{2} + \frac{120}{2} = 120.0 \text{in}.$$

For an exterior girder, b_{eff} is determined as one-half the distance to the adjacent girder plus the full overhang width.

$$b_{\text{eff}} = \frac{120}{2} + 42 = 102.0 \text{in}.$$

8.1.2.2 Minimum Negative Flexure Concrete Deck Reinforcement (Article 6.10.1.7)

The total area of the longitudinal reinforcement, provided in negative bending regions, is not to be less than one percent of the total cross-sectional area of the concrete deck. This provision is intended to control cracking of the concrete deck in regions where the tensile stress due to the factored construction loads or the Service II load exceeds ϕf_r , which is often the case in negative bending regions. (f_r is the modulus of rupture of the concrete and is to be taken equal to 0.24(f_r)^{0.5} for normal weight concrete, with ϕ taken equal to 0.90).

The total area of the concrete deck in this example is computed as follows.

$$A_{\text{deck}} = \frac{8.0}{12} (37.0) + 2 \left[\left(\frac{1}{2} \right) \left(\frac{1}{12} \right) (2.0 - 0.75) \left(3.5 - \frac{14/2}{12} \right) \right] = 24.97 \text{ ft}^2 = 3,596 \text{ in.}^2$$

The minimum area of reinforcing steel required is taken as:

$$0.01(3,596) = 35.96 \text{ in.}^2$$

Reinforcement is to be distributed uniformly across the deck width. The area of reinforcement required within the effective width (102 inches) of an exterior girder is determined as shown below.

$$\frac{35.96 \,\text{in.}^2}{37.0 \,\text{ft}} = 0.97 \,\text{in.}^2/\text{ft}$$

$$0.97(102 / 12) = 8.25 \text{ in.}^2$$

8.32 in² of longitudinal reinforcement is provided. This reinforcement should be placed in two layers with two-thirds of the reinforcement in the top layer and the remaining one-third placed in the bottom layer. Therefore, the area of the top reinforcement is 5.55 in² and the area of the bottom reinforcement is 2.77 in². Additionally, the reinforcement should not use bar sizes exceeding No. 6 bars or bar spacings exceeding 12.0 inches. The reinforcement must have a specified minimum yield strength not less than 60 ksi.

8.1.2.3 Elastic Section Properties: Section 2

Similar to the computation of section properties presented above for Section 1, section properties for the short-term and long-term composite sections in Section 2 are presented below. Section properties are computed assuming the concrete is effective in tension (for potential use at the fatigue and service limit states), and also for the section consisting of the girder and reinforcing steel only assuming that the concrete is not effective in tension (for use at the strength limit state).

Table 14 Section 2 Short Term Composite (n) Section Properties

Component	Α	d	Ad	Ad ²	Io	I							
Steel Section	56.75		-92.5			19,767							
Concrete Slab (8"x 102"/8)	102.0	27.00	2,754	74,358	544	74,902							
	158.75		2,662	•		94,669							
				-16.77(2	2,662)=	<u>-44,642</u>							
						50,027 in ⁴							
$d_{5} = \frac{2,662}{158.75} = 16.77 \text{ in.}$	•												
dtop of steel = 22.125 - 16.	.3												
d BOT OF STEEL = 22.25 + 16.	$d_{BOT \text{ of STEEL}} = 22.25 + 16.77 = 39.02 \text{ in.} $ $S_{BOT \text{ of STEEL}} = \frac{50,027}{39.02} = 1,282 \text{ in.}^3$												

Table 15 Section 2 Long Term Composite (3n) Section Properties

Component	A	d	Ad	Ad^2	I _o	I						
Steel Section	56.75		-92.5			19,767						
Concrete Slab (8"x 102"/24)	34.0	27.00	918	24,786	181.3	24,967						
	90.75		825.5			44,734						
				-9.1	0(825.5) =	<u>-7,512</u>						
						37,222 in ⁴						
$d_5 = \frac{825.5}{90.75} = 9.10 \text{ in.}$	•											
$d_{\text{TOP OF STEEL}} = 22.125 - 9.10 = 13.03 \text{ in.}$ $S_{\text{TOP OF STEEL}} = \frac{37,222}{13.03} = 2,857 \text{ in.}^3$												
$d_{\text{BOT OF STEEL}} = 22.25 + 9.1$	10=31.	35 in.	$S_{BOT OF STEEL} = \frac{37}{31}$	$\frac{222}{35} = 1,187$	in. ³							

Table 16 Section 2 Steel Section and Longitudinal Reinforcement Section Properties

Component	A	d	Ad	Ad ²	Io	I
Steel Section	56.75		-92.5			19,767
Top Long. Reinforcement	5.09	28.75	146.3	4,207		4,207
Bot. Long. Reinforcement	2.54	24.25	61.6	1,494		1,494
	64.38		115.4			25,468

$$-1.79(115.4) = \frac{-207}{25,261 \text{ in}^4}$$

$$d_{5} = \frac{115.4}{64.83} = 1.79 \text{ in.}$$

$$d_{\text{TOP OF STEEL}} = 22.125 - 1.79 = 20.34 \text{ in.}$$

$$d_{\text{TOP OF REIN.}} = 29.00 - 1.79 = 27.21 \text{ in}$$

$$d_{BOT OF STEEL} = 22.25 + 1.79 = 24.04 in$$

Furthermore, the steel section plus longitudinal reinforcement section moduli are computed as follows,

$$S_{TOP OF STEEL} = 25,261 / 20.34 = 1,242 in.^3$$

$$S_{BOT OF STEEL} = 25,261 / 24.04 = 1,051 \text{ in.}^3$$

$$S_{REIN} = 25,261 / 27.21 = 928 \text{ in.}^3$$

8.1.2.4 Plastic Moment: Section 2

Similar to the calculation of the plastic moment for Section 1, Table D6.1-2 is used to determine the plastic moment (M_p) for the negative bending section as demonstrated below. The concrete slab is assumed to crack and is neglected in the computation of M_p . The plastic force acting in each element of the girder is first computed.

$$\begin{split} P_c &= F_{yc} b_c t_c &= (50)(16)(1.25) &= 1,000 \text{ kips} \\ P_w &= F_{yw} D t_w = (50)(42)(0.50) &= 1,050 \text{ kips} \\ P_t &= F_{yt} b_t t_t &= (50)(14)(1.125) &= 788 \text{ kips} \\ P_{rb} &= F_{yrb} A_{rb} &= (60)(2.77) &= 166 \text{ kips} \end{split}$$

$$P_{rt} = F_{yrt}A_{rt} = (60)(5.55)$$
 = 333 kips

The plastic forces in each element are used to determine the general location of the plastic neutral axis as follows:

CASE I

$$P_c + P_w \ge P_t + P_{rb} + P_{rt}$$

$$1,000 + 1,050 \ge 788 + 166 + 333$$

 $2,050 \ge 1,287$ Therefore, the plastic neutral axis is in the web.

The location of plastic neutral axis (\bar{y}) is determined by the following equation:

$$rac{1}{y} = \left(\frac{D}{2}\right) \left[\frac{P_c - P_t - P_{rt} - P_{rb}}{P_w} + 1\right]$$

$$\overline{y} = \left(\frac{42}{2}\right) \left[\frac{1000 - 788 - 333 - 166}{1050} + 1\right] = 15.26in.$$

The plastic moment (M_p) is then computed as follows:

$$M_{p} = \frac{P_{w}}{2D} \left[\overline{y}^{2} + \left(D - \overline{y}^{2} \right) \right] + \left[P_{rt} d_{rt} + P_{rb} d_{rb} + P_{t} d_{t} + P_{c} d_{c} \right]$$

where,

$$d_{rt} = 15.26 + 2 + 8.0 - 2.25 = 23.01$$
 in.

$$d_{rb} = 15.26 + 2 + 1.25 = 18.51$$
 in.

$$d_t = 15.26 + 1.125/2 = 15.82$$
 in.

$$d_c = 42.0 - 15.26 + 1.25/2 = 27.37$$
 in.

$$\mathbf{M}_{p} = \left[\frac{1,050}{2(42.0)}\right] \left[(15.26)^{2} + (42.0 - 15.26)^{2} \right] + \left[(305)(23.01) + (152)(18.51) + (788)(15.82) + (1000)(27.37) \right]$$

$$M_p = 61,515 \text{ k-in.} = 5,126 \text{ k-ft.}$$

8.1.2.5 Yield Moment: Section 2

The process for determining the yield moment of the negative bending section is similar to the process for the positive bending section. The one difference, though, is that since the composite short-term and the composite long-term bending sections are both composed of the steel section and the reinforcing steel only at the strength limit state, the section modulus is the same for both the short-term and long-term composite sections.

The yield moment is the lesser of the moment which causes first yielding of the section, either yielding in the bottom flange or yielding in the tension flange or steel reinforcing. Because, for the negative bending region it is not clear which yield moment value will control, the moments causing first yield in both compression and tension are computed.

The moment causing yielding in compression flange is first computed based on Equation D6.2.2-1.

$$F_{yf} = \frac{M_{D1}}{S_{NC}} + \frac{M_{D2}}{S_{LT}} + \frac{M_{AD}}{S_{ST}}$$
 Eq. (D6.2.2-1)

$$50 = 1.0 \left[\frac{1.25(1,334)(12)}{951.3} + \frac{1.25(265)(12) + 1.50(217)(12)}{1,051} + \frac{M_{AD}}{1,057} 1 \right]$$

$$M_{AD} = 22,562 \text{ k-in.} = 1,880 \text{ k-ft}$$

$$M_{vc} = (1.25)(1,334) + (1.25)(265) + (1.50)(217) + 1,880 = 4,204 \text{ k-ft}$$

The specifications indicate that for regions in negative flexure, M_{yt} is to be taken with respect to either the tension flange or the longitudinal steel reinforcement, whichever yields first. Therefore, compute M_{yt} for both and use the smaller value.

The moment which causes yielding in the tension flange is computed as follows:

$$50 = 1.0 \left[\frac{1.25(1,334)(12)}{825.6} + \frac{1.25(265)(12) + 1.50(217)(12)}{1252} + \frac{M_{AD}}{1242} \right]$$

$$M_{AD} = 24,417 \text{ k-in.} = 2,010 \text{ k-ft}$$

$$M_{yt} = (1.25)(1,334) + (1.25)(265) + (1.50)(217) + 2,010 = 4,334 \text{ k-ft}$$

The moment which causes yielding in the longitudinal steel reinforcement is computed as follows. It is necessary to recognize that there is no noncomposite moment acting on the longitudinal steel reinforcement, and that F_y should be taken as 60 ksi.

$$F_{yf} = \frac{M_{D1}}{S_{NC}} + \frac{M_{D2}}{S_{LT}} + \frac{M_{AD}}{S_{ST}}$$
Eq. (D6.2.2-1)

$$F_{yf} = F_y = 60 \ ksi \qquad \qquad M_{D1} = 0 \ k\text{-ft} \label{eq:mass}$$

$$60 = 1.0 \left[0 + \frac{1.25(265)(12) + 1.50(217)(12)}{928} + \frac{M_{AD}}{928} \right]$$

$$M_{AD} = 47,799 \text{ k-in.} = 3,983 \text{ k-ft}$$

$$M_{vt} = (1.25)(265) + (1.50)(217) + 3,983 = 4,638 \text{ k-ft}$$

Therefore, the top flange yields before the longitudinal reinforcement, and $M_{yt} = 4,334$ k-ft.

For the whole section, the compression flange governs, thus $M_y = M_{yc} = 4,204$ k-ft.

8.2 **Exterior Girder Check: Section 2**

This design example illustrates the use of the optional moment redistribution procedures given in Appendix B6, where moment is redistributed from the negative bending region to the positive

bending region; therefore the negative bending region will be checked first in order to determine the amount of moment that must be redistributed to the positive bending region.

8.2.1 Strength Limit State (Article 6.10.6)

8.2.1.1 Flexure (Appendix A6)

For sections in negative flexure, the flexural capacity of the member can be determined for general steel I-girders using Article 6.10.8, which limits the maximum capacity to the yield moment of the section. Alternatively, Appendix A6 permits girder capacities up to M_p and may be used for girders: having a yield strength less than or equal to 70 ksi, with a compact or non-compact web (which is defined by Eq. A6.1-1), and satisfying Eq. A6.1-2 (given below). The applicability of Appendix A6 for this design example is evaluated below.

The first requirement that the nominal yield strength must be less than 70 ksi is easily evaluated.

$$F_{vf} = 50 \text{ ksi} \le 70 \text{ ksi}$$
 (satisfied)

The web slenderness requirement is evaluated using Eq. A6.1-1.

$$\frac{2D_c}{t_w} < 5.7 \sqrt{\frac{E}{F_{VC}}}$$
 Eq. (A6.1-1)

As computed above the elastic neutral axis is located 24.04 inches from the bottom of the composite negative bending section. Subtracting the bottom flange thickness gives the web depth in compression in the elastic range (D_c) as computed below.

$$D_c = 24.04 - 1.25 = 22.79$$
 in.

Substituting the applicable values into Eq. A6.1-1 shows that the equation is satisfied.

$$\frac{2(22.79)}{0.5} \le 5.7 \sqrt{\frac{29,000}{50}}$$

$$91.16 < 137.27$$
 (satisfied)

Equation A6.1-2 prevents the use of extremely mono-symmetric girders, which analytical studies indicate have significantly reduced torsional rigidity.

$$\frac{I_{yc}}{I_{yt}} \ge 0.3$$
 Eq. (A6.1-2)

$$\frac{(1/12)(1.25)(16)^3}{(1/12)(1.125)(14)^3} = 1.7 > 0.3$$
 (satisfied)

Thus, Appendix A6 is applicable.

The strength requirements specified by Appendix A6 are given in Section A6.1.1. Since the compression flange is discretely braced at Section 2, the flexural capacity of the compression flange must exceed the maximum negative moment plus one-third of the lateral bending stress due to the factored Strength I loading multiplied by the section modulus for the compression flange, see Eq. A6.1.1-1.

$$M_u + \frac{1}{3} f_l S_{xc} \le \phi_f M_{nc}$$
 Eq. (A6.1.1-1)

However, because the lateral bending forces are zero at the Strength I limit state for the straight girders considered in this example, the left side of the equation reduces to only the maximum moment. The tension flange at Section 2 is continuously braced by the concrete deck at the strength limit state, and must therefore satisfy the following, see Eq. A6.1.4-1.

$$M_u \le \phi_f R_{pt} M_{yt}$$
 Eq. (A6.1.4-1)

Use of Appendix A6 begins with the computation of the web plastification factors, as detailed in Article A6.2 and calculated below. If the section has a web which satisfies the compact web slenderness limit of Eq. A6.2.1-1, the section can reach M_p provided the flange slenderness and unbraced length requirements are satisfied.

$$\frac{2D_{cp}}{t_w} < \lambda_{PW(D_{CP})},$$
 Eq. (A6.2.1-1)

where:
$$\lambda_{pw(D_{qp})} = \frac{\sqrt{\frac{E}{F_{yc}}}}{\left(0.54 \frac{M_p}{R_h M_y} - 0.09\right)^2} \le \lambda_{rw} \left(\frac{D_{cp}}{D_c}\right)$$
 Eq. (A6.2.1-2)

The web depth in compression at M_p is computed by subtracting the previously determined distance between the top of the web and the plastic neutral axis from the total web depth.

$$D_{cp} = 42.0 - 15.26 = 26.74$$
 in.

The hybrid factor, R_h , is determined from Article 6.10.1.10.1, and is 1.0 for this example since the design has a homogeneous material configuration. Therefore, λ_{pw} is computed as follows.

$$\lambda_{\rm rw}=5.7\sqrt{\frac{E}{F_{\rm yc}}}=137.27$$

$$\lambda_{pw(D_{cp})} = \frac{\sqrt{\frac{29000}{50}}}{\left(0.54 \frac{61515}{(1.0)(4204)(12)} - 0.09\right)^{2}} \le 137.27 \left(\frac{26.74}{22.79}\right) = 161.1$$

$$\lambda_{pw(D_{cp})} = 74.5 < 161.1$$
 (satisfied)

The web slenderness classification is then determined as follows.

$$\frac{2(D_{cp})}{t_w} = \frac{2(26.74)}{0.5} = 107.0 > \lambda_{pw(D_c)} = 74.5$$
 (not compact)

As shown, the section does not qualify as compact. However, it was previously demonstrated when evaluating the Appendix A6 applicability that the web does qualify as non-compact. Therefore, the applicable web plastification factors for non-compact web sections are used and are determined as specified by Eqs. A6.2.2-4 and A6.2.2-5:.

$$R_{pc} = \left[1 - \left(1 - \frac{R_h M_{yc}}{M_p}\right) \left(\frac{\lambda_w - \lambda_{pw(D_c)}}{\lambda_{rw} - \lambda_{pw(D_c)}}\right)\right] \frac{M_p}{M_{yc}} \le \frac{M_p}{M_{yc}}$$
Eq. (A6.2.2-4)

where: $\lambda_{pw(D_c)}$ = limiting slenderness ratio for a compact web corresponding to $2D_c/t_w$

$$\lambda_{\text{pw}(D_c)} = \lambda_{\text{pw}(D_{cp})} \left(\frac{D_c}{D_{cp}} \right) = (74.51) \left(\frac{22.79}{26.74} \right) = 63.5 < \lambda_{\text{rw}} = 137.27 \text{ Eq. (A6.2.2-6)}$$

$$R_{pc} = \left[1 - \left(1 - \frac{(1.0)(4204)(12)}{61515}\right) \left(\frac{91.16 - 47.82}{137.27 - 47.82}\right)\right] \frac{61,515}{(4204)(12)} \le \frac{61515}{(4204)(12)}$$

$$R_{pc} = 1.113 \le 1.219 = 1.113$$

$$R_{pt} = \left[1 - \left(1 - \frac{R_h M_{yt}}{M_p} \right) \left(\frac{\lambda_w - \lambda_{pw}(D_c)}{\lambda_{rw} - \lambda_{pw}(D_c)} \right) \right] \frac{M_p}{M_{yt}} \le \frac{M_p}{M_{yt}}$$
 Eq. (A6.2.2-5)

$$R_{pt} = \left[1 - \left(1 - \frac{(1.0)(4334)(12)}{61515}\right) \left(\frac{91.16 - 47.82}{137.27 - 47.82}\right)\right] \frac{61,515}{(4334)(12)} \le \frac{61515}{(4334)(12)}$$

$$R_{pt} = 1.094 \le 1.183 = 1.094$$

The flexural resistance based on the compression flange is determined from Article A6.3 and is taken as the minimum of the local buckling resistance from Article A6.3.2 and the lateral torsional buckling resistance from Article A6.3.3.

To evaluate the local buckling resistance, the flange slenderness classification is first determined, where the flange is considered compact if the following equation is satisfied:

$$\lambda_{f} \leq \lambda_{pf}$$
where: $\lambda_{f} = \frac{b_{fc}}{2t_{fc}}$
Eq. (A6.3.2-3)
$$\lambda_{pf} = 0.38 \sqrt{\frac{E}{f_{yc}}}$$

$$\lambda_{f} = \frac{b_{fc}}{2t_{fc}} \leq \lambda_{pf} = 0.38 \sqrt{\frac{E}{F_{yc}}}$$

$$\lambda_{f} = \frac{16.0}{2(1.25)} \leq \lambda_{pf} = 0.38 \sqrt{\frac{29,000}{50}}$$

Therefore, the compression flange is considered compact, and the flexural capacity based on local buckling of the compression flange is governed by Eq. A6.3.2-1.

$$M_{nc} = R_{pc} M_{vc} = (1.113)(4,204) = 4,679 \text{ k-ft}$$
 Eq. (A6.3.2-1)

Similarly, to evaluate the compressive flexural resistance based on lateral-torsional buckling, the unbraced length must be first classified. Unbraced lengths satisfying the following equation are classified as compact.

$$L_{\rm b} \leq L_{\rm p}$$

where: $L_b = (10.0)(12) = 120$ in.

 $\lambda_{\rm f} = 6.40 \le \lambda_{\rm pf} = 9.15$

120 in.
$$\leq L_p = r_t \sqrt{\frac{E}{F_{yc}}}$$
 Eq. (A6.3.3-4)

where: r_t = effective radius of gyration for lateral torsional buckling (in.)

$$\mathbf{r}_{t} = \frac{b_{fc}}{\sqrt{12\left(1 + \frac{1}{3}\frac{D_{c} t_{w}}{b_{fc} t_{fc}}\right)}} = \frac{16.0}{\sqrt{12\left(1 + \frac{1}{3}\frac{(22.79)(0.5)}{(16.0)(1.25)}\right)}}$$
Eq. (A6.3.3-10)

$$r_t = 4.234$$
 in.

(satisfied)

$$\therefore L_{b} > L_{p} = 4.234 \sqrt{\frac{29,000}{50}} = 102.0$$
 (not compact)

Because the lateral bracing distance does not satisfy the compact limit, the non-compact limit is next evaluated.

$$L_p < L_b \le L_r$$

where: L_r = limiting unbraced length to achieve the nominal onset of yielding in either flange under uniform bending with consideration of compression flange residual stress effects (in.)

$$L_{r} = 1.95r_{t} \frac{E}{F_{yr}} \sqrt{\frac{J}{S_{xc}h}} \sqrt{1 + \sqrt{1 + 6.76 \left(\frac{F_{yr}S_{xc}h}{EJ}\right)^{2}}}$$
 Eq. (A6.3.3-5)

F_{yr} = smaller of the compression flange stress at the nominal onset of yielding of either flange, with consideration of compression-flange residual stress effects but without consideration of flange lateral bending, or the specified minimum yield strength of the web (ksi)

$$F_{yr} = \min \left(0.7F_{yc}, R_h F_{yt} \frac{S_{xt}}{S}, F_{yw} \right)$$
 Article A6.3.3

$$S_{xt} = (4334)(12) / 50 = 1040.1 \text{ in.}^3$$

$$S_{xc} = (4204) (12) / 50 = 1009.0 \text{ in.}^3$$

$$F_{yr} = \min\left(0.7(50), (1.0)(50)\frac{1040.1}{1009.0}, 50\right)$$

$$F_{vr} = min(35,51.5,50)$$

$$F_{yr} = 35.0 \, \text{ksi} > 0.5 \, F_{yc} = 25 \text{ksi}$$
 (satisfied)

J = St. Venant torsional constant

$$J = \frac{1}{3} \left(D t_w^3 + b_{fc} t_{fc}^3 \left(1 - 0.63 \frac{t_{fc}}{b_{fc}} \right) + b_{ft} t_{ft}^3 \left(1 - 0.63 \frac{t_{ft}}{b_{ft}} \right) \right) \quad \text{Eq. (A6.3.3-9)}$$

$$J = \frac{1}{3} ((42)(0.5)^3 + (16)(1.25)^3 (.95) + (14)(1.125)^3 (.95))$$

 $J = 17.96 \text{ in.}^3$

h = depth between the centerline of the flanges

$$h = 1.125/2 + 42 + 1.25/2 = 43.19 in.$$

$$L_{r} = 1.95(4.234) \frac{29000}{35} \sqrt{\frac{17.96}{(1009)(43.19)}} \sqrt{1 + \sqrt{1 + 6.76 \left(\frac{35(1009)(43.19)}{(29000)(18.81)}\right)^{2}}}$$

$$L_r = 401.0 \text{ in.}$$

$$L_B = 120 \le L_T = 401.0$$
 (satisfied)

Therefore, the unbraced length is classified as non-compact and the lateral torsional buckling resistance is controlled by Eq. A6.3.3-2 of the Specifications.

$$M_{nc} = C_b \left[1 - \left(1 - \frac{F_{yr} S_{xc}}{R_{pc} M_{yc}} \right) \left(\frac{L_b - L_p}{L_r - L_p} \right) \right] R_{pc} M_{yc} \le R_{pc} M_{yc}$$
 Eq. (A6.3.3-2)

where: $C_b = moment gradient modifier$

The moment gradient modifier is discussed in Article A6.3.3 and is calculated in the following manner.

$$C_b = 1.75 - 1.05 \left(\frac{M_1}{M_2}\right) + 0.3 \left(\frac{M_1}{M_2}\right)^2 \le 2.3$$
 Eq. (A6.3.3-7)

where: $M_1 = M_0$ when the variation in moment between brace points is concave

Otherwise:

$$M_1 = 2M_{mid} - M_2 \ge M_0$$

 M_{mid} = major-axis bending moment at the middle of the unbraced length

 M_0 = moment at the brace point opposite to the one corresponding to M_2

M₂ = largest major-axis bending moment at either end of the unbraced length causing compression in the flange under consideration

For the critical moment location at the interior pier, the variation in moment is concave throughout the unbraced length and the applicable moment values are as follows:

$$M_2 = 5.365 \text{ k-ft}.$$

$$M_0 = 2,999 \text{ k-ft.}$$

$$M_1 = M_0 = 2,999 \text{ k-ft}$$
 Eq. (A6.3.3-11)

$$C_b = 1.75 - 1.05 \left(\frac{2,999}{5,365}\right) + 0.3 \left(\frac{2,999}{5,365}\right)^2 = 1.26 \le 2.3$$

$$C_b = 1.26$$

Therefore, M_{nc} is equal to the following.

$$\mathbf{M}_{nc} = (1.26) \left[1 - \left(\frac{(35.0)(1009)}{(1.113)(4204)(12)} \right) \left(\frac{120 - 102}{401.0 - 120} \right) \right] (1.113)(4204) \le 1.113(4204)$$

$$M_{nc} = 5,775 \le 4,679$$

$$M_{nc} = 4,679 \text{ k-ft}$$

If the computed M_{nc} had been less than $R_{pc}M_{yc}$ in this case, then the equations of Article D6.4.2 could have alternatively been used to potentially obtain a larger resistance. As previously stated, the flexural capacity based on the compression flange is the minimum of the local buckling resistance and the lateral torsional buckling resistance, which in this design example are equal.

$$M_{nc} = 4,679 \text{ k-ft}$$

Multiplying the nominal moment capacity by the applicable resistance factor gives the following.

$$\phi_f M_{nc} = (1.0)(4,679)$$

$$\phi_f M_{nc} = 4.679 \text{ k-ft}$$

The moment capacity is also evaluated in terms of the tensile moment capacity. For a continuously braced tension flange at the strength limit state, the section must satisfy the requirements of Article A6.1.4.

$$\begin{split} M_u & \leq \varphi_f R_{pt} M_{yt} \\ \varphi_f \ M_{nt} & = \varphi_f R_{pt} M_{yt} \\ \varphi_f \ M_{nt} & = (1.0)(1.094)(4,334) \\ \varphi_f \ M_{nt} & = 4,741 \text{ k-ft} \end{split}$$

This moment capacity is less than the applied Strength I factored moment of 5,365 k-ft, but is not less than the moment capacity determined based on the resistance of the section in compression. Thus, the compression moment capacity will govern the moment resistance for the negative bending region of the girder.

$$\phi_f M_{nt} = 4,741 \text{ k-ft} < M_u = 5,365 \text{ k-ft}$$

$$\phi_f M_{nt} = 4,741 \text{ k-ft} > \phi_f M_{nc} = 4,679 \text{ k-ft}$$

$$\phi_f M_n = 4,679 \text{ k-ft}$$

Comparing this moment resistance to the Strength I factored moment at the pier shows that the factored moment is greater than the moment resistance. Thus, moment redistribution may be considered.

$$M_u = 5,365 > \phi_f M_{nc} = 4,679 \text{ k-ft}$$

8.2.1.2 Moment Redistribution (Appendix B6, Articles B6.1 – B6.5)

Article B6.2 defines the applicability of the optional Appendix B6 provisions. Specifically, the provisions may only be applied to straight continuous span I-section members whose bearing lines are not skewed more than 10 degrees from normal and along which there are no staggered (or discontinuous) cross-frames. The specified minimum yield strength of the section must not exceed 70 ksi. In addition, the section must satisfy the web proportion (Article B6.2.1), compression flange proportion (Article B6.2.2), section transition (Article B6.2.3), compression flange bracing (Article B6.2.4), and shear (Article B6.2.5) requirements discussed below.

8.2.1.2.1 Web Proportions

Equations B6.2.1-1, B6.2.1-2, and B6.2.1-3 specify the web proportion limits that must be satisfied.

$$\frac{D}{t_{w}} \le 150$$
 Eq. (B6.2.1-1)

$$\frac{D}{t_{\rm m}} = \frac{42.0}{0.5} = 84.0 \le 150$$
 (satisfied)

$$\frac{2D_c}{t_w} \le 6.8 \sqrt{\frac{E}{F_{vc}}}$$
 Eq. (B6.2.1-2)

$$\frac{2(22.79)}{0.50} = 91.16 \le 6.8 \sqrt{\frac{29,000}{50}} = 163.8$$
 (satisfied)

$$D_{cp} \le 0.75D$$
 Eq. (B6.2.1-3)

$$D_{cp} = 26.74 \le 0.75(42.0) = 31.50$$
 (satisfied)

8.2.1.2.2 Compression Flange Proportions

Section B6.2.2 requires that the following two compression flange proportion limits be satisfied.

$$\frac{b_{fc}}{2t_{fc}} \le 0.38 \sqrt{\frac{E}{F_{yc}}}$$
 Eq. (B6.2.2-1)

$$\frac{16}{2(1.25)} = 6.40 \le 0.38 \sqrt{\frac{29,000}{50}} = 9.15$$
 (satisfied)

$$b_{fc} \ge \frac{D}{4.25}$$
 Eq. (B6.2.2-2)

$$b_{fc} = 16.0 \ge \frac{42}{4.25} = 9.88$$
 (satisfied)

8.2.1.2.3 Compression Flange Bracing Distance

The compression flange bracing distance must satisfy the following:

$$L_b \le \left[0.1 - 0.06 \left(\frac{M_1}{M_2} \right) \right] \frac{r_i E}{F_{\text{vc}}}$$
 Eq. (B6.2.4-1)

$$L_{b} = 120.0 \le \left[0.1 - 0.06 \left(\frac{2,999}{5,365} \right) \right] \frac{(4.234)(29,000)}{50} = 163.2$$
 (satisfied)

8.2.1.2.4 Shear

Additionally, the applied shear under the Strength I loading must be less than or equal to the shear buckling resistance of the girder as specified by the following:

$$V \le \phi_{v} V_{cr}$$
 Eq. (B6.2.5-1)

where: V_{cr} = shear buckling resistance (kip)

 $V_{cr} = CV_p$ (for unstiffened webs) Eq.(6.10.9.2-1)

 V_p = plastic shear force (kip)

$$V_p = 0.58 F_{yw}Dt_w$$
 Eq. (6.10.9.2-2)

C = ratio of the shear buckling resistance to the shear yield strength determined as specified in Article 6.10.9.3.2, with the shear buckling coefficient, k, taken equal to 5.0

Equations are provided for computing the value of C based on the web slenderness of the girder. First the web slenderness is evaluated using the following equation.

$$\frac{D}{t_{w}} \le 1.12 \sqrt{\frac{Ek}{F_{yw}}}$$

$$\frac{42.0}{0.50} = 84.0 > 1.12 \sqrt{\frac{(29,000)(5)}{50}} = 60.31$$
(not satisfied)

The web slenderness is next evaluated using the following equation.

$$1.12\sqrt{\frac{Ek}{F_{yw}}} \le \frac{D}{t_{w}} \le 1.40\sqrt{\frac{Ek}{F_{yw}}}$$

$$1.12\sqrt{\frac{Ek}{F_{yw}}} = 60.31 < \frac{D}{t_{w}} = 84.0 > 1.40\sqrt{\frac{Ek}{F_{yw}}} = 75.4$$
 (not satisfied)

Thus, the governing equation for computing the ratio C is given by Eq. 6.10.9.3.2-6, which is applicable when:

$$\frac{D}{t_{w}} = 84.0 > 1.40 \sqrt{\frac{Ek}{F_{yw}}} = 75.4$$
 (satisfied)

$$C = \frac{1.57}{\left(\frac{D}{t_w}\right)^2} \left(\frac{Ek}{F_{yc}}\right)$$
 Eq. (6.10.9.3.2-6)

$$C = \frac{1.57}{(84.0)^2} (2,900) = 0.645$$

The shear buckling resistance is then computed as follows.

$$V_{cr} = CV_{p} = (0.645)(0.58)(50)(42)(0.5) = 392.8 \text{ kips}$$

The shear requirement for Appendix B6 can then be evaluated.

$$V=337 \text{ kips} \le \varphi V_{cr} = (1.0)(392.8) = 392.8 \text{ kips}$$
 (satisfied)

The provisions of Article B6.2.1 through B6.2.6 are satisfied for this section. Therefore, moments may be redistributed in accordance with Appendix B6.

The effective plastic moment, determined from Article B6.5, is a function of the geometry and material properties of the section. Furthermore, alternative equations are provided for girders that satisfy the requirements for enhanced moment rotation characteristics, i.e., classification as ultracompact sections. To be classified as ultracompact, the girder must either: (1) contain transverse stiffeners at a location less than or equal to one-half the web depth from the pier, or (2) satisfy the web compactness limit given by Eq. B6.5.1-1.

$$\frac{2D_{cp}}{t_w} \le 2.3 \sqrt{\frac{E}{F_{yc}}}$$
 Eq. (B6.5.1-1)

$$\frac{2(26.74)}{0.50} = 107.0 > 2.3\sqrt{\frac{29,000}{50}} = 55.4$$
 (not satisfied)

Therefore, the section does not satisfy the web compactness limit and because the section uses an unstiffened web, the girder does not satisfy the transverse stiffener requirement. Thus, the girder is not considered to be ultracompact and the applicable M_{pe} equation at the strength limit state is thus Eq. B6.5.2-2.

$$\mathbf{M}_{pe} = \left[2.63 - 2.3 \frac{b_{fc}}{t_{fc}} \sqrt{\frac{F_{yc}}{E}} - 0.35 \frac{D}{b_{fc}} + 0.39 \frac{b_{fc}}{t_{fc}} \sqrt{\frac{F_{yc}}{E}} \frac{D}{b_{fc}} \right] M_n \le M_n \qquad \text{Eq. (B6.5.2-2)}$$

$$M_{pe} = \left[2.63 - 2.3 \frac{16}{1.25} \sqrt{\frac{50}{29000}} - 0.35 \frac{42}{16} + 0.39 \frac{16}{1.25} \sqrt{\frac{50}{29000}} \frac{42}{16} \right] 4679 \le 4679$$

$$M_{pe} = 4,832 \le 4,679 = 4,679 \text{ k-ft}$$

The redistribution moment, M_{rd} , for the strength limit state is taken as the larger of the values calculated from Eqs. B6.4.2.1-1 and B6.4.2.1-2.

$$M_{rd} = |M_e| + \frac{1}{3} f_l S_{xc} - \phi_f M_{pe}$$
 Eq. (B6.4.2.1-1)

$$M_{rd} = |M_e| + \frac{1}{3} f_l S_{xt} - \phi_f M_{pe}$$
 Eq. (B6.4.2.1-2)

where: M_e = critical elastic moment envelope value at the interior-pier section due to the factored loads

Since the lateral bending stresses are negligible for this example, the previous equations reduce to the following equation.

$$\boldsymbol{M}_{rd} = \left| \boldsymbol{M}_{e} \right| - \boldsymbol{\phi}_{f} \boldsymbol{M}_{pe}$$

In addition, the redistribution moment is limited to 20 percent of the elastic moment by Eq. B6.4.2.1-3.

$$0 \le M_{rd} \le 0.2 |M_e|$$
 Eq. (B6.4.2.1-3)

Therefore, the redistribution moment is computed as follows, which is shown to satisfy the 20% limit.

$$M_{rd} = |M_e| - \phi_f M_{pe} = 5,365 - (1.0)(4,679)$$

$$M_{rd} = 686 \text{ k-ft} = 12.8\% \ M_e \le 20\% \ M_e$$

Therefore, the negative bending region of the girder satisfies the strength limit state requirements when the effective plastic moment equations given in Appendix B6 are used to evaluate the girder capacity.

8.2.1.3 Moment Redistribution - Refined Method (Appendix B6, Article B6.6)

Article B6.6 of Appendix B6 contains specifications for computing redistribution moments using a direct method of analysis. Using this analysis procedure, the effective plastic moments are computed based on the rotation at which the continuity curve intersects the moment-rotation curve, as opposed to assuming that this intersection occurs at a plastic rotation of 30 mrads, as assumed in the effective plastic moment equations utilized above.

In cases such as this example, where the effective plastic moment is equal to the nominal moment capacity of the negative bending section, there is no advantage to be gained by using the refined method. This is because the peak value of the moment-rotation curve is equal to M_n , the maximum value of M_{pe} possible, irrespective of using the effective plastic moment equations from Article B6.5 or the refined method of Article B6.6. However, in other cases the use of the refined method may lead to higher values of M_{pe} , further increasing the economic benefits of using the moment redistribution procedures. For this reason, the use of the refined method for the present design is demonstrated below.

The first step in using the refined method for moment redistribution is to determine the moment-rotation curve for the negative bending section. This is done using Figure B6.6.2-1 from the AASHTO LRFD (7th Edition, 2014) Specifications, which is reproduced in Figure 12. From Figure 12 it is observed that the moment-rotation relationship is a function of the single parameter, θ_{RL} , which is the rotation at which the moment begins to decrease below the nominal moment capacity. Similar to the equations for M_{pe} given for the simplified method introduced above, alternative equations for θ_{RL} are given based on whether the negative bending section satisfies the criteria for enhanced moment rotation characteristics given by Section B6.5. It has been shown above that the negative bending section does not satisfy either of the requirements for sections with enhanced moment-rotation performance. Thus, θ_{RL} is given in radians by Eq. B6.6.2-2.

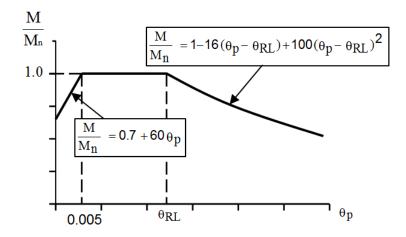


Figure 12 AASHTO LRFD Moment-Rotation Model

$$\theta_{RL} = 0.128 - 0.143 \frac{b_{fc}}{t_{fc}} \sqrt{\frac{F_{yc}}{E}} - 0.0216 \frac{D}{b_{fc}} + 0.0241 \frac{b_{fc}}{t_{fc}} \frac{D}{b_{fc}} \sqrt{\frac{F_{yc}}{E}}$$
Eq. (B6.6.2-2)

Substituting the applicable values into Eq. B6.6.2-2 gives the following.

$$\theta_{RL} = 0.128 - 0.143 \frac{16}{1.25} \sqrt{\frac{50}{29000}} - 0.0216 \frac{42}{16} + 0.0241 \frac{16(42)}{0.5(16)} \sqrt{\frac{50}{29000}} = 0.079$$

Thus, θ_{RL} is equal to 0.079 radians or 79 mrads. Recalling that the nominal moment capacity of the negative moment section of this girder is 4679 ft-kips, the predicted moment-rotation relationship of the example girder is as illustrated in Figure 13.

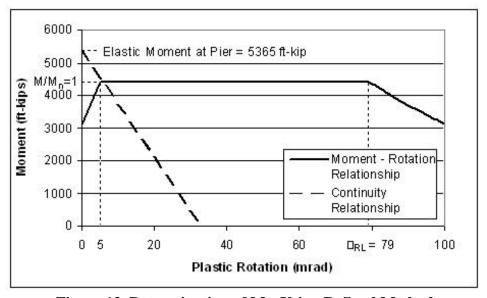


Figure 13 Determination of M_{pe} Using Refined Method

In addition to the moment-rotation relationship, the continuity relationship must also be determined. The continuity relationship is a linear relationship between the elastic moment at the pier (where no plastic rotation occurs) and the rotation assuming no continuity at the pier. The elastic moment at the pier has previously been determined to equal 5365 ft-kips, which is the y-intercept for the continuity relationship. To determine the x-intercept of the continuity relationship, the beam is analyzed assuming that a hinge exists at each pier, and rotations due to applied moments equal to the elastic moment are computed as shown in Figure 14. In this analysis, the *AASHTO LRFD (7th Edition, 2014)* Specifications stipulate that the section properties of the short-term composite section are to be used. Thus, the applicable moment of inertia of the positive bending section is 48,806 in⁴ and the moment of inertia value used for the negative bending section is 50,027 in⁴. From basic structural analysis, or the use of structural analysis software, the rotation at the pier for the situation depicted in Figure 14 is computed to be 32.88 mrads, which is the x-intercept for the continuity relationship. Based on the x- and y-intercepts of the continuity relationship, the continuity equation is thus expressed as

 $M = 5365 \text{ ft-kips} - 163.17 \text{ ft-kips} * \theta_p$

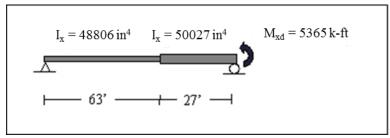


Figure 14 Determination of Rotation at Pier Assuming No Continuity

The moment at the intersection of the continuity relationship and the moment-rotation relationship is the effective plastic moment. From Figure 13 it is illustrated that this moment is equal to the nominal moment capacity of 4679 ft-kips. The effective plastic moment can also be determined mathematically by iteratively selecting θ_p values to be substituted into both the moment-rotation and continuity curves until the moment converges. Alternatively, for the present girder it is known that the moment is equal to M_n for θ_p values between 5 and 79 mrads. Solving the continuity equation for the value of θ_p at M_n gives a rotation of:

$$\theta_p = (5365 - 4679) / 163.17 = 5.8 \text{ mrads}.$$

Since this value is between 5 and 79 mrads, it is mathematically determined that the effective plastic moment is equal to M_n . Once M_{pe} is determined, the moment redistribution analysis proceeds in the same manner used in the simplified method outlined above, where the redistribution moments are computed as the difference between the elastic and the effective plastic moments as specified in Articles B6.3 and B6.4 and the girder is determined to satisfy the strength limit state requirements if the redistribution moment is less than 20% of the elastic moment.

8.2.1.4 Shear (6.10.6.3)

As computed above the shear resistance of the negative bending region is governed by Article 6.10.9.2 because the girder is comprised of an unstiffened web, i.e., no transverse stiffeners are provided. The shear resistance of the section was previously calculated to be:

$$V_p = V = CV_p = 392.8 \text{kips}$$
 Eq. (6.10.9.2-1)

The applied shear at the pier at the strength limit state is 337 kips. Thus, the shear requirements are satisfied.

$$V = 337 \text{ kips} \le \phi_V V_{cr} = (1.0)(392.8) = 392.8 \text{ kips}$$
 (satisfied)

8.2.2 Constructibility (Article 6.10.3)

Article 2.5.3 requires the engineer to design bridge systems such that the construction is not difficult and does not result in unacceptable locked-in forces. In addition, Article 6.10.3 states the main load-carrying members are not permitted to experience nominal yielding, or reliance on

post-buckling resistance during the construction phases. The sections must satisfy the requirements of Article 6.10.3 at each construction stage. The applied loads to be considered are specified in Table 3.4.1-1 and the applicable load factors are provided in Article 3.4.2.

The girders are considered to be non-composite during the initial construction phase. The influence of various segments of the girder becoming composite at various stages of the deck casting sequence is then considered. The effects of forces from deck overhang brackets acting on the fascia girders are to be included in the constructibility checks.

8.2.2.1 Flexure (Article 6.10.3.2)

In regions of negative flexure, Eqs. 6.10.3.2.1-1, 6.10.3.2.1-2 and 6.10.3.2.2-1 specified in Article 6.10.3.2, which are to be checked for critical stages of construction, generally do not control because the sizes of the flanges in these regions are normally governed by the design checks at the strength limit state. Also, the maximum accumulated negative moments from the deck-placement analysis in these regions, plus the negative moments due to the steel weight, typically do not differ significantly from (or may be smaller than) the calculated DC1 negative moments ignoring the effects of the sequential deck placement. The deck-overhang loads do introduce lateral bending stresses into the flanges in these regions, which can be calculated and used to check the above equations in a manner similar to that illustrated later on in this example for Section 1. Wind load, when considered for the construction case, also introduces lateral bending into the flanges.

When applying Eqs. 6.10.3.2.1-1, 6.10.3.2.1-2 and 6.10.3.2.2-1 in these regions, the bottom flange would be considered to be a discretely braced compression flange and the top flange would be considered to be a discretely braced tension flange for all constructibility checks to be made before the concrete deck has hardened or is made composite. The nominal flexural resistance of the bottom flange, F_{nc} , for checking Eq. 6.10.3.2.1-2 would be calculated in a manner similar to that demonstrated below for Section 1. For the sake of brevity, the application of Eqs. 6.10.3.2.1-1, 6.10.3.2.1-2 and 6.10.3.2.2-1 to the construction case for the unbraced lengths adjacent to Section 2 will not be shown in this example.

Note that for sections with slender webs, web bend-buckling should always be checked in regions of negative flexure according to Eq. 6.10.3.2.1-3 for critical stages of construction. In this example, however, Section 2 is not a slender-web section.

8.2.2.2 Shear (Article 6.10.3.3)

The required shear capacity during construction is specified by Eq. 6.10.3.3-1. Later in this design example, the unstiffened shear capacity of the girder is demonstrated to be sufficient to resist the applied shear at the strength limit state. Therefore, the section will have sufficient shear capacity for the constructibility check.

$$V_{u} \le \phi_{v} V_{cr}$$
 Eq. (6.10.3.3-1)

8.2.3 Service Limit State (Article 6.10.4)

Permanent deformations are controlled under the service limit state. Service limit state design checks for steel I-girder bridges are specified in Article 6.10.4.

8.2.3.1 Permanent Deformations (Article 6.10.4.2)

Permanent deformations that may negatively impact the rideability of the structure are controlled by limiting the stresses in the section under expected severe traffic loadings. Specifically, under the Service II load combination, the top flange of composite sections must satisfy:

$$f_f \le 0.95 R_h F_{yf}$$
 Eq. (6.10.4.2.2-1)

Because the bottom flange is discretely braced (as opposed to the top flange), Eq. 6.10.4.2.2-2 must be satisfied for the bottom flange of composite sections as follows:

$$f_f + \frac{f_I}{2} \le 0.95 R_h F_{yf}$$
 Eq. (6.10.4.2.2-2)

At the service limit state, the lateral force effects due to wind loads and deck overhang loads are not considered. Therefore, for bridges with straight, non-skewed girders such as the case in the present design example, the lateral bending stresses are taken equal to zero and Eq. 6.10.4.2.2-2 reduces to Eq. 6.10.4.2.2-1.

For sections satisfying the requirements of Article B6.2, Appendix B6 permits the redistribution of moment at the service limit state before evaluating the above equations. As demonstrated previously, Section 2 satisfies the requirements of Article B6.2. Article B6.5.2 specifies the effective plastic moment to be used at the service limit state as follows:

$$M_{pe} = \left[2.90 - 2.3 \frac{b_{fc}}{t_{fc}} \sqrt{\frac{F_{yc}}{E}} - 0.35 \frac{D}{b_{fc}} + 0.39 \frac{b_{fc}}{t_{fc}} \sqrt{\frac{F_{yc}}{E}} \frac{D}{b_{fc}} \right] M_n \le M_n \quad \text{Eq. (B6.5.2-1)}$$

$$M_{pe} = \left[2.90 - 2.3 \frac{16}{1.25} \sqrt{\frac{50}{29000}} - 0.35 \frac{42}{16} + 0.39 \frac{16}{1.25} \sqrt{\frac{50}{29000}} \frac{42}{16} \right] 4679 \le 4679$$

$$M_{pe} = 6,079 \text{ k-ft} \le 4,679 \text{ k-ft}$$

$$M_{pe} = 4,679 \text{ k-ft} > M_u = 4,075 \text{ k-ft}$$

Because the effective plastic moment is greater than the maximum factored moment for the Service II load combination, it is assumed that there is no moment redistribution at this limit state. The elastic stresses under the Service II load combination are therefore computed using the following equation assuming no moment redistribution:

$$f_f = \frac{M_{DC1}}{S_{nc}} + \frac{M_{DC2} + M_{DW}}{S_{lt}} + \frac{1.3M_{LL+IM}}{S_{st}}$$

For members with shear connectors provided throughout their entire length that also satisfy the provisions of Article 6.10.1.7, and where the maximum longitudinal tensile stresses in the concrete deck at the section under consideration caused by the Service II loads are smaller than $2f_r$, Article 6.10.4.2.1 permits the concrete deck to also be considered effective for negative flexure when computing flexural stresses acting on the composite section at the service limit state. f_r is the modulus of rupture of the concrete specified in Article 6.10.1.7.

Separate calculations (not shown) were made to ensure that the minimum longitudinal reinforcement (determined previously) satisfied the provisions of Article 6.10.1.7 for both the factored construction loads and the Service II loads. Check the maximum longitudinal tensile stresses in the concrete deck under the Service II loads at Section 2. The longitudinal concrete deck stress is to be determined as specified in Article 6.10.1.1.1d; that is, using the short-term modular ratio n = 8. Note that only DC2, DW and LL+IM are assumed to cause stress in the concrete deck.

$$f_r = 0.24\sqrt{f_c'} = 0.24\sqrt{4.0} = 0.48 \text{ ksi}$$

$$f_{deck} = \frac{1.0[1.0(-265) + 1.0(-217) + 1.3(-1,737)](14.235)(12)}{50,027(8)} = 1.17 \text{ ksi} > 2f_r = 2(0.48) = 0.96 \text{ ksi}$$

Therefore, since the concrete deck may not be considered effective in tension at Section 2, the Service II flexural stresses will be computed using the section consisting of the steel girder plus the longitudinal reinforcement only for loads applied to the composite section.

The stress in the compression flange is thus computed as follows.

$$f_f = \frac{(-1334)(12)}{951.3} + \frac{(-265-217)(12)}{1051} + \frac{1.3(-1737)(12)}{1051} = -48.11 \text{ksi}$$

Comparing this stress to the allowable stress shows that Eq. 6.10.4.2.2-1 is satisfied within an acceptable tolerance; the applied stress and the stress limit differ by approximately one percent.

$$f_f = |-48.11 \text{kst}| > 0.95 R_h F_{yf} = 0.95 (1.0) (50) = 47.50 \text{ksi} \ (\approx 1\% \text{ overstress} - \text{say satisfied})$$

Similarly, the computation of the stress in the tension flange is computed as follows.

$$f_f = \frac{(-1334)(12)}{825.6} + \frac{(-265-217)(12)}{1242} + \frac{1.3(-1737)(12)}{1242} = 45.86 \text{ ksi}$$

Thus, it is also demonstrated that Eq. 6.10.4.2.2-2 is satisfied for the tension flange.

$$f_f = 45.86 \text{ ksi} \le 0.95 R_h F_{vf} = 0.95 (1.0)(50) = 47.50 \text{ ksi}$$
 (satisfied)

The compression flange stress at service loads is also limited to the elastic bend-buckling resistance of the web by Eq. 6.10.4.2.2-4.

$$f_c \le F_{crw}$$
 Eq. (6.10.4.2.2-4)

where: f_c = compression flange stress at the section under consideration due to the Service II loads calculated without consideration of flange lateral bending

 F_{crw} = nominal elastic bend buckling resistance for webs with or without longitudinal stiffeners, as applicable, determined as specified in Article 6.10.1.9

From Article 6.10.1.9, the bend-buckling resistance for the web is determined using the following equation.

$$F_{crw} = \frac{0.9Ek}{\left(\frac{D}{t_w}\right)^2} \le min \left(R_h F_{yc}, \frac{F_{yw}}{0.7}\right)$$
 Eq. (6.10.1.9.1-1)

where: k = bend-buckling coefficient =
$$\frac{9}{\left(D_c/D\right)^2}$$
 Eq. (6.10.1.9.1-2)

As specified in Article D6.3.1, the depth of web in compression for composite sections in negative flexure where the concrete deck is not considered to be effective in tension at the service limit state is to be calculated for the section consisting of the steel girder plus the longitudinal reinforcement.

$$D_c = 24.04 - 1.25 = 22.79$$
 in.

Therefore, k and F_{crw} are computed as follows.

$$k = \frac{9}{\left(\frac{22.79}{42.0}\right)^2} = 30.57$$

$$F_{\text{CrW}} = \frac{0.9(29,000(30.57)}{\left(\frac{42}{0.50}\right)^2} = 113.08 \text{ ksi} > R_h F_{yc} = 50 \text{ ksi}$$

$$\therefore$$
 F_{crw} = 50 ksi

It can then be demonstrated that Eq. 6.10.4.2.2-4 is satisfied as shown below.

$$f_c = |-48.11 \text{ksi}| \le F_{crw} = 50 \text{ksi}$$
 (satisfied)

8.2.4 Fatigue and Fracture Limit State (Article 6.10.5)

The fatigue and fracture limit state incorporates three distinctive checks: fatigue resistance of details (Article 6.10.5.1), fracture toughness (Article 6.10.5.2), and a special fatigue requirement for webs (Article 6.10.5.3). The first requirement involves the assessment of the fatigue resistance of details as specified in Article 6.6.1 using the appropriate Fatigue load combination specified in Table 3.4.1-1 and the fatigue live load specified in Article 3.6.1.4. The fracture toughness requirements in Article 6.10.5.2 specify that the fracture toughness must satisfy the requirements of Article 6.6.2. The special fatigue requirement for the web controls the elastic flexing of the web to prevent fatigue cracking. The factored fatigue load for this check is to be taken as the Fatigue I load combination specified in Table 3.4.1-1.

8.2.4.1 Load Induced Fatigue (Article 6.6.1.2)

Article 6.10.5.1 requires that fatigue be investigated in accordance with Article 6.6.1. Article 6.6.1 requires that the live load stress range be less than the nominal fatigue resistance. The nominal fatigue resistance, $(\Delta F)_n$, varies based on the fatigue detail category and is computed using Eq. 6.6.1.2.5-1 for the Fatigue I load combination and infinite fatigue life; or Eq. 6.6.1.2.5-2 for Fatigue II load combination and finite fatigue life.

$$(\Delta F)_n = (\Delta F)_{TH}$$
 Eq. (6.6.1.2.5-1)

$$(\Delta F)_n = \left(\frac{A}{N}\right)^{\frac{1}{3}}$$
 Eq. (6.6.1.2.5-2)

where:
$$N = (365)(75)n(ADTT)_{SL}$$
 Eq. (6.6.1.2.5-3)

A = constant from Table 6.6.1.2.5-1

n = number of stress range cycles per truck passage taken from Table 6.6.1.2.5-2

(ADTT)_{SL}= single-lane ADTT as specified in Article 3.6.1.4

 $(\Delta F)_{TH}$ = constant-amplitude fatigue threshold taken from Table 6.6.1.2.5-3

The fatigue resistance of the base metal at the weld joining the cross-frame connection plate located 10 feet from the pier to the flanges is evaluated below. From Table 6.6.1.2.3-1, it is determined that this detail is classified as a fatigue Detail Category C'. The constant-amplitude fatigue threshold, $(\Delta F)_{TH}$, for a Category C' detail is 12.0 ksi (see Table 6.6.1.2.5-3).

For this example, an $(ADTT)_{SL}$ of 800 trucks per day is assumed. Since this $(ADTT)_{SL}$ exceeds the value of 745 trucks per day specified in Table 6.6.1.2.3-2 for a Category C' detail, the nominal fatigue resistance for this particular detail is to be determined for the Fatigue I load combination and infinite fatigue life using Eq. 6.6.1.2.5-1. Therefore:

$$(\Delta F)_n = (\Delta F)_{TH} = 12.00$$
ksi

The applied stress range is taken as the result of the fatigue loading with a dynamic load allowance of 15 percent applied and distributed laterally by the previously calculated distribution factor for fatigue.

According to Article 6.6.1.2.1, for flexural members with shear connectors provided throughout their entire length and with concrete deck reinforcement satisfying the provisions of Article 6.10.1.7, flexural stresses and stress ranges applied to the composite section at the fatigue limit state at all sections in the member may be computed assuming the concrete deck to be effective for both positive and negative flexure. Shear connectors are assumed provided along the entire length of the girder in this example. Separate computations (not shown) were made to ensure that the longitudinal concrete deck reinforcement satisfies the provisions of Article 6.10.1.7. Therefore, the concrete deck will be assumed effective in computing all dead load and live load stresses and live load stress ranges applied to the composite section in the subsequent fatigue calculations.

The provisions of Article 6.6.1.2 apply only to details subject to a net applied tensile stress. According to Article 6.6.1.2.1, in regions where the unfactored permanent loads produce compression, fatigue is to be considered only if this compressive stress is less than the maximum tensile stress resulting from the Fatigue I load combination specified in Table 3.4.1-1. Note that the live-load stress due to the passage of the fatigue load is considered to be that of the heaviest truck expected to cross the bridge in 75 years. At this location, the unfactored permanent loads produce tension at the top of the girder and compression at the bottom of the girder. In this example, the effect of the future wearing surface is conservatively ignored when determining if a detail is subject to a net applied tensile stress.

Bottom of Top Flange:

$$\gamma(\Delta f) = (1.50) \left[\frac{(104)(12)(4.24)}{50,027} + \frac{|-285|(12)(4.24)}{50,027} \right]$$
$$\gamma(\Delta f) = 0.59 \text{ ksi} \le (\Delta F)_n = 12.00 \text{ ksi}$$
 (satisfied)

Top of Bottom Flange:

$$f_{DC1} = \frac{(-674)(12)(19.37)}{19,616} = -7.99 \text{ ksi}$$

$$f_{DC2} = \frac{(-134)(12)(30.10)}{37,222} = -1.30 \text{ ksi}$$

$$\Sigma = -7.99 + -1.30 = -9.29 \text{ ksi}$$

$$f_{LL+IM} = \frac{1.5(104)(12)(37.77)}{50.027} = 1.41 \text{ ksi}$$

 $|-9.29 \, \mathrm{ksi}| > 1.41 \, \mathrm{ksi}$: fatigue does not need to be checked

8.2.4.2 Distortion Induced Fatigue (Article 6.6.1.3)

A positive connection is to be provided for all transverse connection-plate details to both the top and bottom flanges to prevent distortion induced fatigue.

8.2.4.3 Fracture (Article 6.6.2)

The appropriate Charpy V-notch fracture toughness, found in Table 6.6.2-2, must be specified for main load-carrying components subjected to tensile stress under the Strength I load combination.

8.2.4.4 Special Fatigue Requirement for Webs (Article 6.10.5.3)

Article 6.10.5.3 requires that the shear force applied due to the unfactored permanent loads plus the factored fatigue loading (i.e. the Fatigue I load combination) must be less than the shear-buckling resistance of interior panels of stiffened webs.

$$V_{u} \le V_{cr}$$
 Eq. (6.10.5.3-1)

However, designs utilizing unstiffened webs at the strength limit state, as is the case here, automatically satisfy this criterion. Thus, Eq. 6.10.5.3-1 is not explicitly evaluated herein.

8.3 Exterior Girder Check: Section 1

8.3.1 Constructibility (Article 6.10.3)

8.3.1.1 Deck Placement Analysis

In regions of positive flexure, temporary moments that the non-composite girders experience during the casting of the deck can sometimes be significantly higher than those which may be calculated based on the final conditions of the system. An analysis of the moments during each casting sequence must be conducted to determine the maximum moments in the structure acting on the non-composite girders in those regions. The potential for uplift during the deck casting should also be investigated.

Figure 15 depicts the casting sequence assumed in this design example. As required in Article 6.10.3.4, the loads are applied to the appropriate composite sections during each casting sequence. For example, it is assumed during Cast One that all sections of the girder are non-composite. Similarly, the dead load moments due to the steel components are also based on the non-composite section properties. However, to determine the distribution of moments due to Cast Two, the short-term composite section properties are used in the regions of the girders that were previously cast in Cast One, while the non-composite section properties are used in the region of the girder where concrete is cast in Cast Two. The moments used in the evaluation of the constructibility requirements are then taken as the maximum moments that occur on the non-composite girder during any stage of construction, i.e., the sum of the moments due to the steel

dead load and the first casting phase or the sum of the moments due to the steel dead load and both casting phases. Additionally, while not required, the dead load moment resulting from applying all dead load at once (i.e. without consideration of the sequential placement) to the non-composite section (DC1) is also considered.

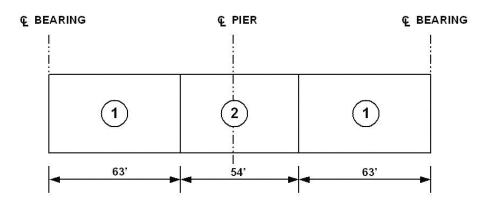


Figure 15 Deck Placement Sequence

The results of the deck placement analysis are shown in Table 17 where the maximum dead load moments in the positive bending region acting on the non-composite section is indicated by bold text. Note that because of the deck-casting sequence chosen for this particular example, the maximum positive bending moment acting on the non-composite section is not caused by the sequential deck placement (i.e. Cast One). Therefore, the DC1 moment of 738 kip-ft at Section 1, ignoring the effect of the sequential deck placement, will be used in the subsequent constructibility design checks.

x/L	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
Dist. (ft.)	0	9	18	27	36	45	54	63	72	81	90
Steel Wt.	0	49	82	101	106	96	71	31	-22	-90	-173
SIP Forms	0	27	46	56	58	53	39	16	-13	-50	-94
Cast 1	0	260	437	532	544	474	321	86	-181	-447	-714
Cast 2	0	301	518	654	707	677	565	370	105	-238	-656
Σ Cast 1	0	335	565	689	708	622	430	133	-216	-587	-981
Σ Cast 2	0	376	646	811	871	825	674	417	70	-377	-923
DC1	0	343	581	712	738	657	471	178	-220	-724	-1334

Table 17 Moments from Deck Placement Analysis (kip-ft)

Article 6.10.1.6 states that when checking the flexural resistance based on lateral torsional buckling, f_{bu} is to be taken as the largest compressive stress in the flange under consideration, without consideration of flange lateral bending, throughout the unbraced length. When checking the flexural resistance based on yielding, flange local buckling or web bend buckling, f_{bu} is to be taken as the stress at the section under consideration. The maximum factored flexural stresses due to the deck casting sequence are calculated below.

8.3.1.1.1 Strength I

Top Flange

$$f_{bu} = \frac{1.0(1.25)(738)(12)}{825.6} = -13.41 \,\text{ksi}$$

Bottom Flange

$$f_{bu} = \frac{1.0(1.25)(738)(12)}{958.6} = 11.55 \text{ ksi}$$

8.3.1.1.2 Special Load Combination (Article 3.4.2.1)

Top Flange

$$f_{bu} = \frac{1.0(1.4)(738)(12)}{825.6} = -15.02 \text{ ksi}$$

Bottom Flange

$$f_{bu} = \frac{1.0(1.4)(738)(12)}{958.6} = 12.93 \text{ ksi}$$

8.3.1.2 Deck Overhang Loads

The loads applied to the deck overhang brackets induce torsion on the fascia girders, which introduces flange lateral bending stresses. This section illustrates the recommended approach to estimate these lateral bending stresses.

The deck overhang bracket configuration assumed in this example is shown in Figure 16. Typically the brackets are spaced between 3 and 4 feet, but the assumption is made here that the loads are uniformly distributed, except for the finishing machine. Half of the overhang weight is assume to be carried by the exterior girder, and the remaining half is carried by the overhang brackets.

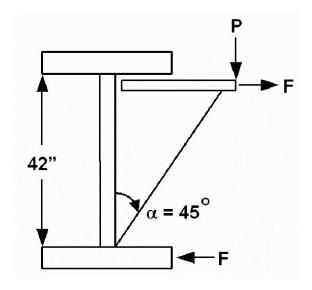


Figure 16 Deck Overhang Bracket Loads

The following calculation determines the weight of the deck overhang acting on the overhang brackets.

$$P = 0.5(150) \left[\frac{8.5}{12} (3.5) + \left[\frac{1}{12} \left(\frac{2.0}{2} \right) \left(3.5 - \frac{14/2}{12} \right) \right] + \frac{1.25}{12} \left(\frac{14/2}{12} \right) \right] = 208.7 \text{ lbs/ft}$$

The following is a list of typical construction loads assumed to act on the system before the concrete slab gains strength. The magnitudes of load listed are those that are applied to only the overhang brackets. Note that the finishing machine load shown represents one-half of the finishing machine truss weight.

Overhang Deck Forms: P = 40 lb/ft

Screed Rail: P = 85 lb/ft

Railing: P = 25 lb/ft

Walkway: P = 125 lb/ft

Finishing Machine: P = 3,000 lb

The lateral force acting on the girder section due to the vertical loading is computed as follows.

 $F = Ptan\alpha$

where: $\alpha = \tan^{-1} \left(\frac{42 \text{in.}}{42 \text{in.}} \right) = 45^{\circ}$

The equations provided in Article C6.10.3.4 to determine the lateral bending moment can be employed in the absence of a more refined method. From the article, the following equation determines the lateral bending moment for a uniformly distributed lateral bracket force:

$$M_l = \frac{F_l L_b^2}{12}$$

where: M_{ℓ} = lateral bending moment in the top flange due to the eccentric loadings from the form brackets

 F_{ℓ} = statically equivalent uniformly distributed lateral force due to the factored loads

The equation which estimates the lateral bending moment due to a concentrated lateral force at the middle of the unbraced length is as follows.

$$M_l = \frac{P_l L_b}{8}$$

where: P_{ℓ} = statically equivalent concentrated force placed at the middle of the unbraced length

For simplicity, the largest value of f_{ℓ} within the unbraced length is conservatively used in the design checks, i.e., the maximum value of f_{ℓ} within the unbraced length is the assumed stress level throughout the unbraced length. The unbraced length for the section under consideration is 20 feet.

Article 6.10.1.6 specifies the process for determining the lateral bending stress. The first-order lateral bending stress may be used if the following limit is satisfied.

$$L_b \le 1.2 L_p \sqrt{\frac{C_b R_b}{f_{bm}/F_{yc}}}$$
 Eq. (6.10.1.6-2)

where: L_p = limiting unbraced length from Article 6.10.8.2.3 of the Specifications

 $C_b \ = \ moment \ gradient \ modifier$

 $R_b \ = \ web \ load\text{-shedding factor}$

 F_{yc} = yield strength of the compression flange

 C_b is the moment gradient modifier specified in Article 6.10.8.2.3. Separate calculations show that $f_{mid}/f_2 > 1$ in the unbraced length under consideration. Therefore, C_b must be taken equal to 1.0.

According to Article 6.10.1.10.2, the web load-shedding factor, R_b , is to be taken as 1.0 when checking constructibility.

Calculate L_p:

$$\begin{split} &D_c = 26.01 - 0.75 = 25.26 \text{ in.} \\ &r_t = \frac{b_{fc}}{\sqrt{12 \left(1 + \frac{1}{3} \frac{D_c t_w}{b_{fc} t_{fc}}\right)}} = \frac{14}{\sqrt{12 \left(1 + \frac{1}{3} \frac{(25.26)(0.4375)}{14(0.75)}\right)}} = 3.48 \text{ in.} \\ &L_p = 1.0 \\ &r_t \sqrt{\frac{E}{F_{yc}}} = 1.0(3.48) \sqrt{\frac{29,000}{50}} = 83.8 \text{ in.} \end{split}$$
 Eq. (6.10.8.2.3-4)

Thus, Eq. 6.10.1.6-2 is evaluated as follows.

$$L_b = 240 \text{ in.} > 1.2(83.8) \sqrt{\frac{(1.0)(1.0)}{|-15.02|/50}} = 183.5 \text{ in.}$$

Because Eq. 6.10.1.6-2 is not satisfied, Article 6.10.1.6 requires that second-order elastic compression-flange lateral bending stresses be determined. The second-order compression-flange lateral bending stresses may be determined by amplifying first-order values (i.e. $f_{\ell 1}$) as follows:

$$f_{\ell} = \left(\frac{0.85}{1 - \frac{f_{bu}}{F_{cr}}}\right) f_{\ell 1} \ge f_{\ell 1}$$
 Eq. (6.10.1.6-4)

or: $f_{\ell} =$

$$f_{\ell} = (AF)f_{\ell_1} \ge f_{\ell_1}$$

where AF is the amplification factor and F_{cr} is the elastic lateral torsional buckling stress for the flange under consideration specified in Article 6.10.8.2.3 determined as:

$$F_{cr} = \frac{C_b R_b \pi^2 E}{\left(\frac{L_b}{r_t}\right)^2}$$
 Eq. (6.10.8.2.3-8)
$$F_{cr} = \frac{1.0(1.0)\pi^2 (29,000)}{\left(\frac{20(12)}{3.48}\right)^2} = 60.18 \text{ ksi}$$

Note that the calculated value of F_{cr} for use in Eq. 6.10.1.6-4 is not limited to $R_b R_h F_{yc}$.

The amplification factor is then determined as follows:

For Strength I:

$$AF = \frac{0.85}{\left(1 - \frac{\left|-13.41\right|}{60.18}\right)} = 1.09 > 1.0 \text{ ok}$$

For the Special Load Combination specified in Article 3.4.2.1:

$$AF = \frac{0.85}{\left(1 - \frac{\left| -15.02 \right|}{60.18}\right)} = 1.13 > 1.0 \text{ ok}$$

AF is taken equal to 1.0 for tension flanges.

8.3.1.2.1 Strength I

The lateral bending stresses for the Strength I load combination are computed as follows. As specified in Article 3.4.2.1, the load factor for construction loads and any associated dynamic effects is not to be taken less than 1.5 for the Strength I load combination.

Dead loads:

$$P = [1.25(209) + 1.5(40 + 85 + 25 + 125)] = 673.8 \text{ lbs/ft.}$$

$$F = F_{\ell} = P \tan \alpha = 673.8 \tan (45^{\circ}) = 673.8 \text{ lbs/ft.}$$

$$M_{\ell} = \frac{F_{\ell}L_{b}^{2}}{12} = \frac{(0.6738)(20)^{2}}{12} = 22.46 \text{ kip} - \text{ft}$$

Top Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{22.46(12)}{0.75(14)^2/6} = 11.00 \text{ ksi}$$

Bottom Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{22.46(12)}{1.25(16)^2/6} = 5.05 \text{ ksi}$$

Finishing machine load:

$$P = [1.5(3,000)] = 4,500 \text{ lbs.}$$

$$F = P_{\ell} = P \tan \alpha = 4,500 \tan (45^{\circ}) = 4,500 \text{ lbs.}$$

$$M_{\ell} = \frac{P_{\ell}L_b}{8} = \frac{(4.5)(20)}{8} = 11.25 \text{ kip} - \text{ft}$$

Top Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{11.25(12)}{0.75(14)^2/6} = 5.51 \text{ ksi}$$

Bottom Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{11.25(12)}{1.25(16)^2/6} = 2.53 \text{ ksi}$$

Total:

Top flange:
$$f_{\ell} = (11.00 + 5.51)AF = (11.00 + 5.51)(1.09) = 17.99 \text{ ksi}$$

Bot. flange:
$$f_{\ell} = (5.05 + 2.53)AF = (5.05 + 2.53)(1.0) = 7.58 \text{ ksi}$$

8.3.1.2.2 Special Load Combination (Article 3.4.2.1)

The computation of the lateral bending stresses for the special load combination specified in Article 3.4.2.1 is demonstrated below.

Dead loads:

$$P = [1.4(209+40+85+25+125)] = 677.6$$
 lbs/ft

$$F = F_{\ell} = P \tan \alpha = 677.6 \tan(45^{\circ}) = 677.6 \text{ lbs/ft}$$

$$M_{\ell} = \frac{F_{\ell}L_b^2}{12} = \frac{(0.6776)(20)^2}{12} = 22.59 \text{ k} - \text{ft}$$

Top Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{22.59(12)}{0.75(14)^2/6} = 11.06 \text{ ksi}$$

Bottom Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{22.59(12)}{1.25(16)^2/6} = 5.08 \text{ ksi}$$

Finishing machine load:

$$P = [1.4(3,000)] = 4,200$$
 lbs.

$$F=P_{\boldsymbol{\ell}}=P$$
 tan $\alpha=4{,}200$ tan (45°) = 4,200 lbs.

$$M_{\ell} = \frac{P_{\ell}L_b}{8} = \frac{(4.2)(20)}{8} = 10.50 \text{ kip} - \text{ft}$$

Top Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{10.50(12)}{0.75(14)^2/6} = 5.14 \text{ ksi}$$

Bottom Flange:
$$f_{\ell} = \frac{M_{\ell}}{S_{\ell}} = \frac{10.50(12)}{1.25(16)^2/6} = 2.36 \text{ ksi}$$

Total:

Top flange:
$$f_{\ell} = (11.06 + 5.14)(AF) = (11.06 + 5.14)(1.13) = 18.31 \text{ ksi}$$

Bot. flange:
$$f_{\ell} = (5.08 + 2.36)(AF) = (5.08 + 2.36)(1.0) = 7.44 \text{ ksi}$$

According to Article 6.10.1.6, the lateral bending stresses (after amplification) must be less than 60 percent of the yield stress of the flange under consideration. It is shown above that the lateral bending stresses are highest in the top flange under the Special Load Combination, and highest in the bottom flange under the Strength I load combination. Thus, evaluation of Eq. 6.10.1.6-1 for the Special Load Combination combination is shown below.

$$f_l \le 0.6F_{v} \tag{6.10.1.6-1}$$

Top flange:
$$f_{\ell} = 18.31 \text{ ksi} < 0.6F_{\text{vf}} = 30 \text{ ksi}$$
 (satisfied)

Bot. flange:
$$f_{\ell} = 7.58 \text{ ksi} < 0.6F_{\text{yf}} = 30 \text{ ksi}$$
 (satisfied)

8.3.1.3 Flexure (Article 6.10.3.2)

During construction, both the compression and tension flanges are discretely braced. Therefore, Article 6.10.3.2 requires the non-composite section to satisfy Eqs. 6.10.3.2.1-1, 6.10.3.2.1-2, and 6.10.3.2.1-3, which ensure the flange stress is limited to the yield stress, the section has sufficient strength under the lateral torsional and flange local buckling limit states, and web bend buckling does not occur during construction, respectively.

First, determine if the non-composite section satisfies the noncompact slenderness limit as follows:

$$\frac{2D_c}{t_w} < 5.7 \sqrt{\frac{E}{F_{yc}}}$$
 Eq. (6.10.6.2.3-1)
$$\frac{2(25.26)}{0.4375} < 5.7 \sqrt{\frac{29,000}{50}}$$

$$0.4375$$
 V 50 (satisfied)

The section is nonslender (i.e. the section has a compact or noncompact web). Therefore, Eq. 6.10.3.2.1-3 (web bend-buckling) need not be checked.

8.3.1.3.1 Compression Flange:

Flange nominal yielding:

$$f_{bu} + f_1 \le \phi_f R_b F_{vc}$$
 Eq. (6.10.3.2.1-1)

Since the section under consideration is homogeneous, the hybrid factor, R_h , is 1.0, as stated in Article 6.10.1.10.1. Thus, Eq. 6.10.3.2.1-1 is evaluated as follows:

For Strength I:

$$13.41 + 17.99 \le (1.0)(1.0)(50)$$

$$31.40 \,\mathrm{ksi} \le 50 \,\mathrm{ksi}$$
 (satisfied)

For the Special Load Combination (Article 3.4.2.1):

$$15.02+18.31 \le (1.0)(1.0)(50)$$

$$33.33 \,\mathrm{ksi} \le 50 \,\mathrm{ksi}$$
 (satisfied)

Flexural Resistance:

$$f_{bu} + \frac{1}{3} f_l \le \phi_f F_{nc}$$
 Eq. (6.10.3.2.1-2)

As specified in Article 6.10.3.2.1, the nominal flexural resistance of the compression flange, F_{nc} , is to be determined as specified in Article 6.10.8.2. For sections in straight I-girder bridges with compact or noncompact webs, the lateral torsional buckling resistance may be taken as M_{nc} determined as specified in Article A6.3.3 (Appendix A6) divided by the elastic section modulus about the major axis of the section to the compression flange, S_{xc} . As mentioned in Article C6.10.3.2.1, this may be useful for sections in bridges with compact or noncompact webs having larger unbraced lengths, if additional lateral torsional buckling resistance is required beyond that calculated based on the provisions of Article 6.10.8.2. However, for this particular example, the increased lateral torsional buckling resistance obtained by using the provisions of Article A6.3.3 is not deemed to be necessary. Thus, the provisions of Article 6.10.8.2.3 will be used to compute the lateral torsional buckling resistance for this check.

First, calculate the local buckling resistance of the top (compression) flange. Determine the slenderness ratio of the top flange:

$$\lambda_{f} = \frac{b_{fc}}{2t_{fc}}$$
 Eq. (6.10.8.2.2-3)

$$\lambda_{f} = \frac{14}{2(0.75)} = 9.3$$

Determine the limiting slenderness ratio for a compact flange (alternatively, see Table C6.10.8.2.2-1):

$$\lambda_{\rm pf} = 0.38 \sqrt{\frac{\rm E}{\rm F_{yc}}}$$
 Eq. (6.10.8.2.2-4)
$$\lambda_{\rm pf} = 0.38 \sqrt{\frac{29,000}{50}} = 9.2$$

Since $\lambda_f > \lambda_{pf}$,

$$F_{nc} = \left[1 - \left(1 - \frac{F_{yr}}{R_h F_{yc}}\right) \left(\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}\right)\right] R_b R_h F_{yc}$$
 Eq. (6.10.8.2.2-2)

where: $F_{yr} = 0.7F_{yc} \le F_{yw}$

$$F_{Vr} = 0.7(50) = 35.0 \text{ ksi} < 50 \text{ ksi}$$
 ok

 F_{yr} must also not be less than $0.5F_{yc} = 0.5(50) = 25.0$ ksi ok.

$$\lambda_{\text{rf}} = 0.56 \sqrt{\frac{E}{F_{\text{yr}}}}$$
 Eq. (6.10.8.2.2-5)
$$\lambda_{\text{rf}} = 0.56 \sqrt{\frac{29,000}{35.0}} = 16.1$$

As specified in Article 6.10.3.2.1, in computing F_{nc} for constructibility, the web load-shedding factor R_b is to be taken equal to 1.0 because the flange stress is always limited to the web bendbuckling stress according to Eq. 6.10.3.2.1-3. Therefore,

$$\left(F_{nc}\right)_{FLB} = \left[1 - \left(1 - \frac{35.0}{(1.0)(50)}\right)\left(\frac{9.3 - 9.2}{16.1 - 9.2}\right)\right](1.0)(1.0)(50) = 49.78 \text{ ksi}$$

For Strength I:

$$f_{bu} + \frac{1}{3} f_{\ell} \le \phi_f (F_{nc})_{FLB}$$

$$f_{bu} + \frac{1}{3} f_{\ell} = |-13.41| \text{ ksi} + \frac{17.99}{3} \text{ ksi} = 19.41 \text{ ksi}$$

$$\phi_f (F_{nc})_{FLB} = 1.0(49.78) = 49.78 \text{ ksi}$$

$$19.41 \text{ ksi} < 49.78 \text{ ksi} \quad \text{(satisfied)}$$

For the Special Load Combination specified in Article 3.4.2.1:

$$\begin{split} f_{bu} + & \frac{1}{3} f_{\ell} \le \phi_{f} \left(F_{nc} \right)_{FLB} \\ f_{bu} + & \frac{1}{3} f_{\ell} = \left| -15.02 \right| \text{ksi} + \frac{18.31}{3} \text{ksi} = 21.12 \text{ksi} \\ \phi_{f} \left(F_{nc} \right)_{FLB} = 1.0(49.78) = 49.78 \text{ksi} \\ 21.12 \text{ ksi} < 49.78 \text{ksi} \quad \text{(satisfied)} \end{split}$$

Next, determine the lateral torsional buckling resistance of the top (compression) flange within the unbraced length under consideration. The limiting unbraced length, L_p, was computed earlier to be 83.8 in. or 6.98 ft. The effective radius of gyration for lateral torsional buckling, r_t, for the non-composite section was also computed earlier to be 3.48 inches.

Determine the limiting unbraced length, L_r:

$$L_r = \pi r_t \sqrt{\frac{E}{F_{yr}}}$$
 Eq. (6.10.8.2.3-5)

where: $F_{yr} = 0.7F_{yc} \le F_{yw}$

$$F_{Vr} = 0.7(50) = 35.0 \text{ ksi} < 50 \text{ ksi}$$
 ok

 F_{yr} must also not be less than $0.5F_{yc} = 0.5(50) = 25.0$ ksi ok.

Therefore: $L_r = \frac{\pi(3.48)}{12} \sqrt{\frac{29,000}{35.0}} = 26.22 \text{ ft}$

Since $L_p = 6.98$ feet $< L_b = 20.0$ feet $< L_r = 26.22$ feet,

$$F_{nc} = C_b \left[1 - \left(1 - \frac{F_{yr}}{R_h F_{yc}} \right) \left(\frac{L_b - L_p}{L_r - L_p} \right) \right] R_b R_h F_{yc} \le R_b R_h F_{yc}$$
 Eq. (6.10.8.2.3-2)

As discussed previously, since $f_{mid}/f_2 > 1$ in the unbraced length under consideration, the moment-gradient modifier, C_b , must be taken equal to 1.0. Therefore,

$$F_{nc} = 1.0 \left[1 - \left(1 - \frac{35.0}{1.0(50)} \right) \left(\frac{20.0 - 6.98}{26.22 - 6.98} \right) \right] (1.0)(1.0)(50) = 39.85 \text{ ksi} < 1.0(1.0)(50) = 50 \text{ ksi} \text{ ok}$$

For Strength I:

$$\begin{split} f_{bu} + & \frac{1}{3} f_{\ell} \le \phi_{f} (F_{nc})_{LTB} \\ f_{bu} + & \frac{1}{3} f_{\ell} = \left| -13.41 \right| \text{ksi} + \frac{17.99}{3} \text{ksi} = 19.41 \text{ksi} \\ \phi_{f} (F_{nc})_{LTB} = & 1.0(39.85) = 39.85 \text{ksi} \\ 19.41 \text{ksi} < & 39.85 \text{ksi} \quad \text{(satisfied)} \end{split}$$

For the Special Load Combination specified in Article 3.4.2.1:

$$\begin{split} f_{bu} + & \frac{1}{3} f_{\ell} \le \phi_f \left(F_{nc} \right)_{LTB} \\ f_{bu} + & \frac{1}{3} f_{\ell} = \left| -15.02 \right| \text{ksi} + \frac{18.31}{3} \text{ksi} = 21.12 \text{ksi} \\ \phi_f \left(F_{nc} \right)_{LTB} = & 1.0(39.85) = 39.85 \text{ksi} \\ 21.12 \text{ksi} < & 39.85 \text{ksi} \quad \text{(satisfied)} \end{split}$$

8.3.1.3.2 Tension Flange:

Flange Nominal Yielding:

$$f_{bu} + f_l \le \phi_f R_b F_{vt}$$
 Eq. (6.10.3.2.2-1)

For Strength I:

$$11.55 + 7.58 \le (1.0)(1.0)(50)$$

 $19.13 \text{ ksi} \le 50 \text{ ksi}$ (satisfied)

For the Special Load Combination (Article 3.4.2.1):

$$12.93 + 7.44 \le (1.0)(1.0)(50)$$

 $20.37 \text{ ksi} \le 50 \text{ ksi}$ (satisfied)

8.3.1.4 Shear (Article 6.10.3.3)

As previously stated, since the design does not require any transverse stiffeners, the shear check under the construction loading is automatically satisfied.

8.3.2 Service Limit State (Article 6.10.4)

Service limit state requirements for steel I-girder bridges are specified in Article 6.10.4. The evaluation of the positive bending region based on these requirements follows.

8.3.2.1 Elastic Deformations (Article 6.10.4.1)

Since the bridge is not designed to permit pedestrian traffic, the live load deflection will be limited to L/800. It is shown below that the maximum deflection along the span length using the service loads and a line girder approach is less than the L/800 limit. It is noted, however, that the application of this requirement is optional.

$$\delta = 0.610 \text{ in.} < L/800 = (90 \text{ x } 12) / 800 = 1.35 \text{ in.}$$

8.3.2.2 Permanent Deformations (Article 6.10.4.2)

To control permanent deformations, flange stresses are limited according to Eq. 6.10.4.2.2-1 as follows:

$$f_f \le 0.95 R_h F_{vf}$$
 Eq. (6.10.4.2.2-1)

where:
$$f_f = \frac{M_{DC1}}{S_{nc}} + \frac{M_{DC2} + M_{DW}}{S_{lt}} + \frac{1.3M_{LL+IM}}{S_{st}}$$

It is noted that the moment values in the above equation represent the moments resulting from elastic analysis since it has previously been determined that moment redistribution is not applicable at the service limit state.

The stress in the compression flange is shown below to equal 18.97 ksi, which satisfies the requirements of Eq. 6.10.4.2.2-1.

$$f_f = \frac{(738)(12)}{614} + \frac{(147 + 120)(12)}{2,711} + \frac{1.3(2160)(12)}{10,001} = 18.97 \text{ ksi}$$

$$f_f = 18.97 \text{ ksi} \le 0.95 R_h F_{yf} = 0.95(1.0)(50) = 47.5 \text{ ksi}$$
 (satisfied)

Similarly, the stress in the tension flange is computed to equal 39.74 ksi, also satisfying Eq. 6.10.4.2.2-1 (f_{ℓ} is equal to zero in this case).

$$f_f = \frac{(738)(12)}{887.7} + \frac{(147 + 120)(12)}{1,159} + \frac{1.3(2160)(12)}{1,248} = 39.74 \text{ ksi}$$

$$f_f = 39.74 \text{ ksi} \le 0.95 R_h F_{yf} = 0.95(1.0)(50) = 47.5 \text{ ksi}$$
 (satisfied)

For composite sections in positive flexure, since the web satisfies the requirement of Article 6.10.2.1.1 (i.e. $D/t_w \le 150$) such that longitudinal stiffeners are not required, web bend-buckling under the Service II load combination need not be checked at Section 1. Thus, all service limit state requirements are satisfied.

8.3.3 Fatigue and Fracture Limit State (Article 6.10.5)

8.3.3.1 Load Induced Fatigue (Article 6.6.1.2)

The fatigue calculation procedures in the positive bending region are similar to those previously presented for the negative bending region. In this section the fatigue requirements are evaluated for the flange welds of a cross-frame connection plate located 40 feet from the abutment.

From Table 6.6.1.2.3-1, it is determined that this detail is classified as a fatigue Detail Category C'. The constant-amplitude fatigue threshold, $(\Delta F)_{TH}$, for a Category C' detail is 12 ksi (see Table 6.6.1.2.5-3).

For this example, an $(ADTT)_{SL}$ of 800 trucks per day is assumed. Since this $(ADTT)_{SL}$ exceeds the value of 745 trucks per day specified in Table 6.6.1.2.3-2 for a Category C' detail, the nominal fatigue resistance for this particular detail is to be determined for the Fatigue I load combination and infinite fatigue life using Eq. 6.6.1.2.5-1. Therefore:

$$(\Delta F)_{n} = (\Delta F)_{TH}$$
 Eq. (6.6.1.2.5-1)
 $(\Delta F)_{n} = (\Delta F)_{TH} = 12.00 \text{ksi}$

Again, as discussed previously, the concrete deck will be assumed effective in computing all dead load and live load stresses and live load stress ranges applied to the composite section in the subsequent fatigue calculations.

At this location, the unfactored permanent loads produce compression at the top of the girder and tension at the bottom of the girder. In this example, the effect of the future wearing surface is conservatively ignored when determining if a detail is subject to a net applied tensile stress.

Bottom of Top Flange:

$$f_{DC1} = \frac{(702)(12)(25.26)}{15,969} = -13.32 \text{ ksi}$$

$$f_{DC2} = \frac{(140)(12)(12.43)}{35,737} = -0.58 \text{ ksi}$$

$$\Sigma = -13.32 + -0.58 = -13.90 \text{ ksi}$$

$$f_{LL+IM} = \frac{1.5 |-143|(12)(4.13)}{48.806} = 0.22 \text{ ksi}$$

 $|-13.90 \, \text{ksi}| > 0.22 \, \text{ksi}$: fatigue does not need to be checked

Top of Bottom Flange:

$$\gamma(\Delta f) = (1.50) \left[\frac{(528)(12)(37.87)}{48,806} + \frac{|-143(12)(37.87)}{48,806} \right]$$

$$\gamma(\Delta f) = 9.37 \text{ ksi} \le (\Delta F)_n = 12.00 \text{ ksi}$$
 (satisfied)

8.3.3.2 Special Fatigue Requirement for Webs (Article 6.10.5.3)

As discussed previously, the following shear requirement must be satisfied at the fatigue limit state:

$$V \le \phi_v V_{cr}$$
 Eq. (6.10.5.3-1)

However this is an unstiffened web. Therefore, this limit does not control and is not explicitly evaluated.

8.3.4 Strength Limit State (Article 6.10.6)

8.3.4.1 Flexure (Article 6.10.6.2)

For compact sections in positive bending, Equation 6.10.7.1.1-1 must be satisfied at the strength limit state.

$$M_u + \frac{1}{3} f_l S_{xt} \le \phi_f M_n$$
 Eq. (6.10.7.1.1-1)

The lateral bending stresses are negligible for the straight, composite girder considered herein. The following requirements must be satisfied for a section to qualify as compact:

$$F_v = 50 \text{ ksi} \le 70 \text{ ksi}$$
 (satisfied)

$$\frac{D}{t_{\text{m}}} = \frac{42.0}{0.4375} = 96.0 \le 150$$
 (satisfied)

$$\frac{2D_{cp}}{t_w} = \frac{2(0)}{0.4375} = 0 \le 3.76 \sqrt{\frac{E}{F_{yc}}}$$
 (satisfied)

Therefore, the section is compact, and the nominal flexural resistance is based on Article 6.10.7.1.2. The following requirement must be evaluated.

$$D_p \le 0.1D_t$$

The plastic neutral axis was determined previously to be located 7.05 in. from the top of the concrete deck. Therefore, the depth of the composite section in compression at the plastic moment, D_p , is

$$D_p = 7.05 \text{ in.}$$

 D_t = total depth of the composite section

$$D_t = 8 + 2 + 42 + 1.25 = 53.25$$
 in.

$$D_p = 7.05 > 0.1D_t = 0.1(53.25) = 5.33$$
 (not satisfied)

Therefore, the nominal flexural capacity is determined from.

$$M_n = M_p \left(1.07 - 0.7 \frac{D_p}{D_c} \right)$$
 Eq. (6.10.7.1.2-2)

$$M_n = 6,416 \left(1.07 - 0.7 \frac{7.05}{53.25} \right) = 6,270k - ft$$

Since the span under consideration and all adjacent interior-pier sections satisfy the requirements of Article B6.2 (as determined previously), M_n is not limited to $1.3R_hM_y$ according to Eq. 6.10.7.1.2-3 in this case.

From elastic analysis procedures, the maximum positive moment under the Strength I load combination is 4,192 k-ft., which is at a distance of 36 feet from the left support. The redistribution moment must then be added to this moment to determine the total applied moment. The redistribution moment varies linearly from zero at the end supports to a maximum at the interior pier of 936 k-ft. Thus, the redistribution moment at 36' from the abutment is computed as follows.

$$M_{rd}$$
= 36/90*(936) = 0.4(936) = 374 k-ft

The total design moment is then the sum of the redistribution moment and the elastic moment.

$$M_n = 4{,}192 + 374 = 4{,}566 \text{ k-ft}$$

The bending strength of the positive bending region is then shown to be sufficient.

$$M_{ij} \leq \phi_{f} M_{ij}$$

$$4,566 \text{ k-ft.} \le (1.0)(6,270) = 6,270 \text{ k-ft}$$
 (satisfied)

8.3.4.2 Ductility Requirement (6.10.7.3)

Sections in positive bending are also required to satisfy Eq. 6.10.7.3-1, which is a ductility requirement intended to prevent premature crushing of the concrete slab.

$$D_n \le 0.42D_t$$
 Eq. (6.10.7.3-1)

$$D_p = 7.05 \text{ in.} \le 0.42(53.25) = 22.37 \text{ in.}$$
 (satisfied)

8.3.4.3 Shear (6.10.6.3)

The shear requirements at the strength limit state are expressed by:

$$V_u \le \phi_v V_n$$
 Eq. (6.10.9.1-1)

where: $V_n = V_{cr}$

 V_{cr} = shear buckling resistance (kip)

 $V_{cr} = CV_p$ (for unstiffened webs) Eq. (6.10.9.2-1)

 V_p = plastic shear force (kip)

 $V_p = 0.58 F_{vw}Dt_w$ Eq. (6.10.9.2-2)

C = ratio of the shear buckling resistance to the shear yield strength determined as specified in Article 6.10.9.3.2, with the shear buckling coefficient, k, taken equal to 5.0

The computation of C is based on the web slenderness classification. Thus, the web slenderness is first evaluated in terms of the following equation.

$$\frac{D}{t_{w}} \le 1.12 \sqrt{\frac{Ek}{F_{yw}}}$$

$$\frac{D}{t_{w}} = \frac{42.0}{0.4375} = 96.0 > 1.12 \sqrt{\frac{Ek}{F_{yw}}} = 1.12 \sqrt{\frac{(29,000)(5)}{50}} = 60.31 \qquad \text{(not satisfied)}$$

The web slenderness is next evaluated in terms of the following equation.

$$1.12\sqrt{\frac{Ek}{F_{yw}}} < \frac{D}{t_w} = 96.0 \le 1.40\sqrt{\frac{Ek}{F_{yw}}}$$

$$1.12\sqrt{\frac{Ek}{F_{yw}}} = 60.31 < \frac{D}{t_w} = 96.0 > 1.40\sqrt{\frac{Ek}{F_{yw}}} = 75.4$$
 (not satisfied)

Lastly, the web slenderness is evaluated as follows.

$$\frac{D}{t_w} = 96.0 > 1.40 \sqrt{\frac{Ek}{F_{yw}}} = 75.4$$
 (satisfied)

Thus, C is calculated according to Eq. 6.10.9.3.2-6.

$$C = \frac{1.57}{\left(\frac{D}{t_{w}}\right)^{2}} \left(\frac{Ek}{F_{yw}}\right) = \frac{1.57}{(96.0)^{2}} (2,900) = 0.494$$
 Eq. (6.10.9.3.2-6)

Therefore, the shear capacity is equal to:

$$V_{cr} = CV_p = (0.494)(0.58)(50)(42) (0.4375) = 263.2 \text{ kips}$$

 $V = 257 \text{ kips} \le \phi_v V_{cr} = (1.0)(263.2) = 263.2 \text{ kips}$ (satisfied)

Thus, the shear requirements at the strength limit state (and consequently all other limit states as previously discussed) are satisfied.

8.4 Cross-frame Design

The cross-frames alone provide restoring forces during construction to enable the girders to deflect equally. Once the system acts compositely, the concrete slab also contributes to providing restoring forces and continuously braces the top flanges at the girder. Although several styles of cross-frames may be used (refer to Chapter 8 for a more complete discussion), a typical K-shaped cross-frame (as shown in Figure 17) is used for this example. The design of the intermediate and end cross-frames is demonstrated in the sections that follow.

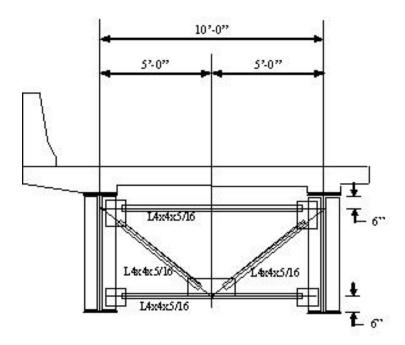


Figure 17 Intermediate Cross Frame

8.4.1 Intermediate Cross-frame Design

This section describes the design process for an intermediate cross-frame. The cross-frames are most critical while the system is in the non-composite stage under wind loading. The wind load per unit length on the bottom flange is given by Article 4.6.2.7.

$$w = \frac{P_D d}{2} = \frac{(0.050)(44.25/12)}{2} = 0.092 \,\text{k/ft}.$$

8.4.1.1 Bottom Strut

The bottom strut is in compression under the wind loading; therefore, the limiting slenderness ratio for bracing members in compression must be satisfied as specified in Article 6.9.3.

A L 4x4x 5/16 single angle is selected for the bottom strut. Section properties are calculated below and depicted in Figure 18. In these computations it is assumed that the connection plate is ½-inch thick.

$$\begin{split} A &= 2.40 \text{ in.}^2 \\ r_z &= 0.781 \text{ in.} \\ I_z &= A r_z^2 = (2.40)(0.781)^2 = 1.46 \text{ in.}^4 \\ I_w &= I_x + I_y - I_z = 3.67 + 3.67 - 1.46 = 5.88 \text{ in.}^4 \\ r_w &= \sqrt{\frac{I_w}{A}} = \sqrt{\frac{5.88}{2.40}} = 1.57 \text{ in.} \end{split}$$

$$r_x = r_v = 1.24 \text{ in.}$$

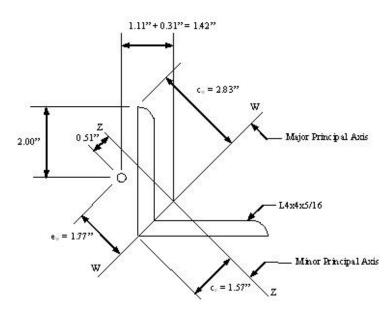


Figure 18 Single Angle for Intermediate Cross Frame

The horizontal wind force applied to the brace point can be calculated in the following manner, where L_b is taken as the maximum cross frame spacing and the wind load per unit length (w) is 0.092 k/ft, as previously determined:

$$P_w = wL_b = (0.092)(20.0) = 1.84 \text{ kips}$$

The bottom struts in the exterior bays of the system must carry the entire wind force $P_{\rm w}$; therefore, all of the bottom struts will be conservatively designed to satisfy the requirements of the exterior bay struts.

The Strength III load combination controls the cross-frame design for wind due to having the largest load factor for wind, which is specified to be 1.40. The following calculation determines the factored axial wind force in the bottom strut, including the η factor.

$$P_u = 1.00(1.40)(1.84) = 2.58 \text{ kips}$$

Connected through one leg only, the strut is eccentrically loaded. The member then experiences both flexure and axial compression.

Check the slenderness provision of Article 6.9.4.2.1 for the cross frame bottom strut member:

$$\frac{b}{t} \le k \sqrt{\frac{E}{F_y}}$$
 Eq. (6.9.4.2.1-1)

where: k = plate buckling coefficient, 0.45 for outstanding legs of single angles from Table 6.9.4.2.1-1

b = the full width of the outstanding leg for a single angle (in.)

t = plate thickness (in.)

$$\frac{b}{t} = \frac{4}{0.5625} = 7.1 < 0.45 \sqrt{\frac{29000}{50}} = 10.8$$
 OK. Member is nonslender.

Check the limiting slenderness ratio of Article 6.9.3. As a secondary compression member, the angle must satisfy the following:

$$\frac{K\ell}{r}$$
 < 140

where: K =effective length factor specified in Article 4.6.2.5 taken as 1.0 for single angles regardless of end connection (in.)

 ℓ = unbraced length (in.)

r = minimum radius of gyration (in.)

$$\frac{K\ell}{r} = \frac{1.0(9)(12)}{0.781} = 138 < 140 \text{ OK}$$

8.4.1.1.1 Combined Axial Compression and Bending

Having satisfied the basic slenderness provisions, the angle is then checked for the strength limit state in accordance with Article 6.9.4.4 regarding single-angle members.

Single angles are commonly used as members in cross frames of steel girder bridges. Since the angle is typically connected through one leg only, the member is subjected to combined axial load and flexure. In other words, the eccentricity of the applied axial load induces moments about both principal axes of the angle. As a result, it is difficult to predict the nominal compressive resistance of these members. The provisions of Article 6.9.4.4 provide a simplified approach by permitting the effect of the eccentricities to be neglected when the single angles are evaluated as axially loaded compression members for flexural buckling only using an appropriate specified effective slenderness ratio, $(K\ell/r)_{eff}$, in place of $(K\ell/r_s)$ in Eq. 6.9.4.1.2-1. By following this approach, the single angles may be designed as axially loaded compression members for flexural buckling only according to the provisions of Articles 6.9.2.1, 6.9.4.1.1, and 6.9.4.1.2. It should be noted that according to Article 6.9.4.4, the actual maximum slenderness ratio of the angle, not the effective slenderness ratio, is not to exceed the limiting slenderness ratio specified in Article 6.9.3, as checked above. Also, per Article 6.9.4.4, single angles designed using $(K\ell/r)_{eff}$ need not be checked for flexural-torsional buckling.

Compute the effective slenderness ratio per Article 6.9.4.4 based on the criteria for equal-leg angles. First, check the ℓ/r_x limit of 80:

$$\frac{\ell}{r_{r}} = \frac{(9)(12)}{1.24} = 87.1 > 80$$

where: r_x = radius of gyration about the geometric axis of the angle parallel to the connected leg (Although not relevant for equal-leg angles, the term r_x may actually equal r_y when unequal-leg angles are used.)

Therefore, compute the effective slenderness ratio as follows:

$$\left(\frac{K\ell}{r}\right)_{\text{eff}} = 32 + 1.25 \frac{\ell}{r_x}$$
 Eq. (6.9.4.4-2)
$$\left(\frac{K\ell}{r}\right)_{\text{eff}} = 32 + 1.25 \frac{(9)(12)}{1.24} = 141$$

In accordance with the provisions for single-angle members in Article 6.9.4.4 and using the effective slenderness ratio, $(K\ell/r)_{eff}$, the factored resistance of the angle in compression is taken as:

$$P_r = \phi_c P_n$$
 Eq. (6.9.2.1-1)

where: P_n = nominal compressive resistance determined using the provisions of Article 6.9.4.1.1 ϕ_c = resistance factor for compression as specified in Article 6.5.4.2

To compute P_n , first compute P_e and P_o . P_e is the elastic critical buckling resistance determined as specified in Article 6.9.4.1.2 for flexural buckling, which is the applicable buckling mode for single angles. P_o is the equivalent nominal yield resistance equal to QF_yA_g , where Q is the slender element reduction factor determined as specified in Article 6.9.4.2. Q is taken as 1.0 in this case according to Article 6.9.4.2.1 since the angle member is nonslender per Eq. 6.9.4.2.1-1.

$$P_{e} = \frac{\pi^{2}E}{\left(\frac{K\ell}{r_{s}}\right)^{2}} A_{g}$$
 Eq. (6.9.4.1.2-1)

where $(K\ell/r)_{eff}$ is used in place of $(K\ell/r_s)$ in the denominator.

$$P_e = \frac{\pi^2 E}{\left(\frac{K\ell}{r}\right)_{eff}^2} A_g = \frac{\pi^2 (29000)}{(141)^2} (2.40) = 34.6 \text{kips}$$

$$P_o = QF_yA_g = (1.0)(50)(2.4) = 120 \text{ kips}$$

Since

$$\frac{P_e}{P_o} = \frac{34.6}{120} = 0.288 < 0.44$$
,

the nominal axial resistance in compression is computed as:

$$P_n = 0.877P_e$$
 Eq. (6.9.4.1.1-2)

$$P_n = 0.877(34.6) = 30.3 \text{ kips}$$

Compute the factored axial resistance of the angle in compression as follows:

$$P_r = \phi_c P_n = 0.95(30.3) = 28.8 \text{ kips}$$

$$P_u = |-2.58 \text{kips}| < P_r = 28.8 \text{ kips OK}$$

8.4.1.2 Diagonals

The diagonals carry a compressive force that is the result of wind loads and reactions from the loads carried in the top strut. It is assumed that each bay carries a portion of P_w , and the two diagonals carry equal loads. From statics the following equation can be derived to determine the axial force in the diagonals.

$$(P_w)_{diag.} = \sqrt{a^2 + b^2} \left(\frac{P_w}{2na}\right)$$

where:

a = one-half the transverse girder spacing

b = vertical distance between working points for the diagonals

 $P_w = \text{total applied wind-load force}$

n = number of bays

$$(P_w)_{diag.} = \sqrt{\frac{(10.0)(12)}{2}^2 + (30)^2} \left(\frac{1.84}{2(3)(10.0(12)/2)}\right) = 0.34 \text{ kips}$$

The axial force in each diagonal due to the wind loading under the Strength III load combination is as follows:

$$P_u = 1.00(1.40)(0.34) = 0.48 \text{ kips}$$

The unbraced length of the diagonal in compression, taken as the distance between the working points, is calculated below:

$$l = \sqrt{\left(\frac{10.0(12)}{2}\right)^2 + (30.0)^2} = 67.08$$
in.

A similar analysis was conducted for the diagonals as was conducted for the bottom strut, and the L4x4x5/16 member was determined to be adequate for the design wind loading.

8.4.2 End Cross-frame Design

The lateral wind forces are transmitted from the deck to the substructure by the end cross-frames. The following section describes the design of end cross-frames (see Figure 19).

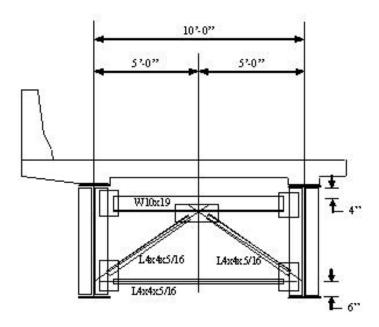


Figure 19 End Cross Frame

8.4.2.1 Top Strut

The top strut of the end cross-frames carries the compressive forces that are a result of the wind load on the structure and vehicles, dead load of the slab, including the haunch, and the wheel loads, including the dynamic load allowance. The total wind pressure P_D , calculated previously, is 0.050 ksf. The total height of the structure is as follows:

Barrier = 42.00 in.

Deck = 8.50 in.

Haunch = 2.00 in.

Girder - top flange = 43.25 in.
= 93.75 in. = 7.98 ft

The wind load per unit length on the structure is computed as follows:

$$w_s = (7.98)(0.050) = 0.40 \text{ kips/ft}$$

From Article 3.8.1.3, the wind load per unit length acting normal to the vehicles at a distance of 6.0 feet above the roadway is:

$$w_L = 0.10 \text{ kips/ft}$$

The wind load on the end cross-frames is assumed to be half of the total wind load and is computed below.

$$P_{WL} = 0.40 \left(\frac{90.0}{2} \right) = 18.0 \text{ kips}$$

$$P_{WL} = 0.10 \left(\frac{90.0}{2} \right) = 4.5 \,\text{kips}$$

Each bay is assumed to carry an equal portion of the wind load; therefore, the axial force in the top strut is calculated as follows:

$$(P_{WS})_{top strut} = 18.00/3 = 6.00 \text{ kips}$$

$$(P_{WL})_{top \ strut} = 4.50/3 = 1.50 \ kips$$

The dead load from the slab, concrete haunch, and steel girder acting on the top strut is computed below:

Slab =
$$8.50 (14.00 + 12.00 + 7.50)(1/144)(0.150) = 0.30$$

Concrete Haunch = $7.50 (14.00 + 12.00 + 7.50/2)(1/144)(0.150) = 0.23$
Steel Girder = 0.03
= 0.56 kip/ft .

As specified in Article 3.6.1.2.4, the design lane is a 0.64 kips/ft. load distributed over a 10.0 foot width.

$$W_{LL} = \frac{0.64}{10.0(12)} \left(14.0 + 12.0 + \frac{7.50}{2} \right) = 0.16 \text{ kips/ft}$$

The design truck wheel load plus the dynamic load allowance is discussed in Article 3.6.1.2.2 and is as follows.

$$P_{LL} = \frac{32.0}{2}(1.33) = 21.28 \text{ kips}$$

Figure 20 illustrates the position of the above computed live loads that produce the maximum moment and shear in the strut. The maximum moments and reactions in the top strut are given as follows.

$$M_{DC} = 1.75 \text{ k-ft}$$

$$M_{LL+IM} = 18.30 \text{ k-ft}$$

$$R_{DC} = 3.50 \text{ kips}$$

$$R_{LL+IM} = 25.1 \text{ kips}$$

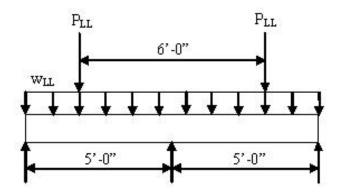


Figure 20 Live load on Top Strut

The Strength I load combination governs the design of the top strut of the end cross-frame design. Thus, the controlling moments and shears are computed as follows.

8.4.2.1.1 Strength I:

$$M_u = 1.00[1.25(1.75) + 1.75(18.30)] = 34.21 \text{ k-ft}$$

$$V_u = 1.0 \left[1.25 \left(\frac{3.5}{2} \right) + 1.75 \left(\frac{25.1}{2} \right) \right] = 24.15 \text{ kips}$$

To choose a preliminary member for the top strut, the required section modulus assuming the moment capacity of the member is M_p is computed.

$$M_r = \phi_f M_n = \phi_f M_p = \phi_f F_y Z$$

$$Z = \frac{34.2(12)}{1.0(50)} = 8.21$$
in.

In addition to meeting the flexural requirements, the minimum material thickness requirements must also be considered when selecting the member. Therefore, a W10 x 19 is selected as a trial member.

To determine the flexural capacity of the W10x19 section, the applicability of Appendix A6 is first evaluated.

$$F_v = 50 \text{ ksi} \le 70 \text{ ksi}$$

$$\frac{2D_c}{t_{vc}} = \frac{2(9.41/2)}{0.25} = 37.64 \le 5.7 \sqrt{\frac{E}{F_{yc}}} = 137.3$$
 Eq. (A6.1-1)

Therefore, Appendix A6 is applicable. The web slenderness is then evaluated based on Eq. A6.2.1-1.

$$\frac{2D_{cp}}{t_{w}} \le \lambda_{pw(D_{Cp})}$$
 Eq. (A6.2.1-1)

$$\lambda_{pw(D_{cp})} = \frac{\sqrt{\frac{E}{F_{yc}}}}{\left(0.54 \frac{M_p}{R_h M_y} - 0.09\right)^2} \le \lambda_{rw} \left(\frac{D_{cp}}{D_c}\right)$$
 Eq. (A6.2.1-2)

$$\lambda_{\text{pw}(D_{\text{cp}})} = \frac{\sqrt{\frac{29000}{50}}}{\left(0.54 \frac{(21.6)(50)}{(1.0)(18.8(50)} - 0.09\right)^2} = 88.92 \le 137.3 \left(\frac{9.41/2}{9.41/2}\right) = 137.3$$

$$\frac{2D_{cp}}{t_w} = \frac{2(9.41/2)}{0.25} = 37.64 < 88.92$$
 (satisfied)

Therefore, the web is compact and the web plastification factors are thus computed as follows.

$$R_{pc} = \frac{M_p}{M_{yc}} = \frac{(21.6)(50)}{(18.8)(50)} = 1.149$$
 Eq. (A6.2.1-3)

$$R_{pt} = \frac{M_p}{M_{vt}} = \frac{(21.6)(50)}{(18.8)(50)} = 1.149$$
 Eq. (A6.2.1-4)

The flange slenderness must also be evaluated. The following calculations show that the compression flange is compact.

$$\lambda_{pf} = 0.38 \sqrt{\frac{E}/F_{yc}} = 9.15$$

$$\lambda_{f} = \frac{b_{fc}}{2t_{fc}} = \frac{4.02}{2(0.395)} = 5.09 \le 9.15$$
(satisfied)

Therefore, the flexural capacity of the section based on local buckling is equal to the product of the web plastification factor and the yield moment, as specified in Eq. A6.3.2-1.

$$M_{nc(FLB)} = R_{pc}M_{yc} = 1.149(50)(18.8)/12 = 90.0 \text{ k-ft.}$$

The flexural capacity based on lateral torsional buckling must also be investigated. Alternative equations are used to compute the lateral torsional buckling capacity based on the unbraced length. The unbraced length classifications are based on the value of r_t .

$$r_{t} = \frac{b_{fc}}{\sqrt{12\left(1 + \frac{1}{3}\left(\frac{D_{c}t_{w}}{b_{fc}t_{fc}}\right)\right)}} = \frac{4.02}{\sqrt{12\left(\frac{1}{3}\left(\frac{(9.41/2)(0.25)}{(4.02)(0.395)}\right)\right)}} = 1.039 \text{in.}$$
 Eq. (A6.3.3-10)

The lateral bracing distance is classified as compact if Eq. A6.3.3-4 is satisfied.

$$L_p = r_t \sqrt{\frac{E_{f_{yc}}}{F_{yc}}} = 25.03 \text{ in.}$$
 Eq. (A6.3.3-4)

$$L_b = (5.0)(12) = 60 \text{ in.} > 25.03 \text{ in.}$$
 (not satisfied)

Therefore, the lateral bracing distance is next evaluated compared to the non-compact lateral bracing limit.

$$L_b = 60 \le L_r = 1.95 r_t \frac{E}{F_{yr}} \sqrt{\frac{J}{S_{xc}h}} \sqrt{1 + \sqrt{1 + 6.76 \left(\frac{F_{yr}S_{xc}h}{EJ}\right)^2}}$$
 Eq. (A6.3.3-5)

where:
$$F_{yr} = \min \left(0.7 F_{yc}, R_h F_{yt} \frac{S_{xt}}{S_{xc}}, F_{yw} \right)$$

$$F_{yr} = \min\left(0.7(50), (1.0)(50)\frac{18.8}{18.8}, 50\right) = \min\left(35, 50, 50\right) = 35.0 \text{ ksi}$$

$$J = \frac{1}{3} \left(Dt_{w}^{3} + b_{fc} t_{fc}^{3} \left(1 - 0.63 \frac{t_{fc}}{b_{fc}} \right) + b_{ft} t_{ft}^{3} \left(1 - 0.63 \frac{t_{ft}}{b_{ft}} \right) \right)$$
Eq. (A6.3.3-9)

$$J = \frac{1}{3} ((9.41)(0.25)^3 + 2(4.02)(.395)^3 (.938)) = 0.204 \text{ in.}^3$$

$$h = 9.81$$
in.

$$L_r = 1.95(1.039) \frac{29,000}{35} \sqrt{\frac{0.204}{(18.8)(9.81)}} \sqrt{1 + \sqrt{1 + 6.76 \left(\frac{35}{29,000} \frac{(18.8)(9.81)}{0.204}\right)^2}} = 110 \text{ in.}$$

$$L_b = 60 \text{in.} < L_r = 110 \text{in.}$$

Therefore, the lateral torsional buckling resistance is controlled by Eq. A6.3.3-2.

$$M_{nc} = C_b \left[1 - \left(1 - \frac{F_{yr} S_{xc}}{R_{pc} M_{yc}} \right) \left(\frac{L_b - L_p}{L_r - L_p} \right) \right] R_{pc} M_{yc} \le R_{pc} M_{yc}$$

$$R_{pc}M_{vc} = (1.149)(50)(18.8) = 1,080 \text{ k-ft}.$$

$$M_{nc} = \left[1 - \left(\frac{(35)(18.8)}{(1.149)(50)(18.8)}\right) \left(\frac{60 - 25.03}{112.7 - 25.03}\right)\right] = 911.7 \text{ k-ft.}$$

$$M_{nc(LTR)} = 911.7 \text{ k-in.} = 75.9 \text{ k-ft.}$$

Comparing the flange local buckling and lateral torsional buckling capacities, it is determined that the lateral torsional buckling capacity controls the design of the top strut.

$$M_{nc} = \min(90.0, 75.9)$$

$$\phi_f M_{nc} = (1.0)(75.9) = 75.9 \text{ k-ft.}$$

Thus, the moment capacity is sufficient.

$$\phi_f M_{nc} = 75.9 \text{ k-ft.} > M_u = 34.21 \text{ k-ft.}$$
 (satisfied)

In addition to the flexural capacity, the shear capacity must be evaluated to ensure the member is acceptable. The shear capacity of the member is computed below:

$$V_n = V_{cr} = CV_p$$
 Eq. (6.10.9.2-1)

where:
$$V_p = 0.58 F_{ww} Dt_w = 0.58(50)(9.41)(0.25) = 68.22 \text{ kips}$$
 Eq. (6.10.9.2-2)

The formula used to compute C varies depending on the web slenderness as shown below.

$$1.12\sqrt{\frac{Ek}{F_{yw}}} = 1.12\sqrt{\frac{(29,000)(5.0)}{50}} = 60.31$$

$$\frac{D}{t_{-}} = \frac{9.41}{0.25} = 37.64 < 60.31$$

Therefore, C = 1.0

$$\phi_{\nu}V_{\nu} = (1.0)(68.22) = 68.22 \text{ kips} \ge V_{\nu} = 24.15 \text{ kips}$$
 (satisfied)

Thus, the shear requirements are satisfied.

The member must also be evaluated for combined axial compression and flexure, for which the Strength III and Strength V load combinations are most likely to govern.

8.4.2.1.2 Strength III:

$$P_{\rm u} = 1.00[1.25(0.00) + 1.40(6.00)] = 8.40 \text{ kips}$$

$$M_{ux} = 1.00[1.25(1.75) + 1.40(0.00)] = 2.19 \text{ k-ft}.$$

Article 6.9.2.1 specifies the axial capacity as follows.

$$P_r = \phi_c P_n$$
 Eq. (6.9.2.1-1)

where: $\phi_c = 0.95$

Check the slenderness provision of Article 6.9.4.2.1 for the cross-frame top strut member:

$$\frac{b}{t} \le k \sqrt{\frac{E}{F_y}}$$
 Eq. (6.9.4.2.1-1)

where: k = plate buckling coefficient, 0.56 for flanges of rolled sections and 1.49 for webs of rolled sections from Table 6.9.4.2.1-1

b = half flange width for flanges and clear distance between flanges minus the corner radius for webs (in.)

t = plate thickness (in.)

$$\frac{b}{t} = \frac{4.02/2}{0.395} = 5.09 < 0.56 \sqrt{\frac{29000}{50}} = 13.5$$
 OK. Flanges are nonslender.

$$\frac{b}{t} = \frac{(10.2 - 2(0.695))}{0.250} = 35.24 < 1.49 \sqrt{\frac{29000}{50}} = 35.88 \text{ OK. Web is nonslender.}$$

$$...$$
 O = 1.0

$$P_{e} = \frac{\pi^{2}E}{\left(\frac{K\ell}{r_{s}}\right)^{2}} A_{g} = \frac{\pi^{2}(29000)}{\left(\frac{0.75(9.5)(2)}{0.874}\right)^{2}} (5.62) = 168 \text{ kips}$$

$$P_o = QF_yA_g = (1.0)(50)(5.62) = 281 \text{ kips}$$

Since

$$\frac{P_e}{P_o} = \frac{168}{281} = 0.60 > 0.44,$$

the nominal axial resistance in compression is computed as:

$$P_{n} = \begin{bmatrix} 0.658 \\ P_{e} \end{bmatrix} P_{o} = \begin{bmatrix} 0.658 \\ 168 \end{bmatrix} (281) = 139.5 \text{ kips}$$
 Eq. (6.9.4.1.1-1)

Compute the factored axial resistance of the top strut in compression as follows:

$$P_r = \phi_c P_n = 0.95(139.5) = 132.5 \text{ kips}$$

The factored moment resistance, M_{rx} , was computed previously to be:

$$M_{rx} = \phi 75.9 \text{ k-ft.}$$

The combined influence of axial force and moment must then satisfy the following equation.

$$\frac{P_{\rm u}}{P_{\rm r}} = \frac{8.4}{132.5} = 0.06 < 0.2$$

$$\frac{P_{\rm u}}{2P_{\rm r}} + \frac{M_{\rm ux}}{M_{\rm rx}} \le 1.0$$
Eq. (6.9.2.2-1)
$$\frac{8.4}{2(132.5)} + \frac{2.19}{75.9} = 0.06 < 1.0$$
(satisfied)

8.4.2.1.3 Strength V:

Similarly, the applied axial force and moment due to the Strength V load combination are computed below.

$$\begin{split} P_u &= 1.00[1.25(0.00) + 1.35(0.00) + 1.40(6.00) + 0.40(1.50)] = 9.00 \; kips \\ M_{ux} &= 1.00[1.25(1.75) + 1.35(18.30) + 0.40(0.00) + 1.40(0.00)] = 26.89 \; k\text{-ft}. \end{split}$$

The axial load and moment interaction equation 6.9.2.2-1 is also shown to be satisfied for this load combination below.

$$\frac{9.0}{2(132.5)} + \frac{26.89}{75.9} = 0.39 < 1.0$$
 (satisfied)

8.4.2.2 Diagonals

The diagonals carry a compressive force that is the result of wind loads and reactions from the loads carried in the top strut. The geometry of the end cross-frames was previously illustrated in Figure 19. As previously discussed, the design of the cross-frame is based on the assumption that each bay carries an equal portion of the total wind forces. The axial force is computed below using the same process used earlier in this cross-frame design example.

$$P_{WS} = 18.0 \text{kips}$$

$$P_{WL} = 4.5 \,\mathrm{kips}$$

$$(P_{WS})_{\text{diag.}} = \sqrt{a^2 + b^2} \left(\frac{P_{W}}{2na}\right)$$

$$(P_{WS})_{\text{diag.}} = \sqrt{\left(\frac{10.0(12)}{2}\right)^2 + 30^2} \left(\frac{18.0}{2(3)(10.0(12)/2)}\right) = 3.35 \text{ kips}$$

$$(P_{WL})_{\text{diag.}} = \sqrt{\left(\frac{10.0(12)}{2}\right)^2 + 30^2} \left(\frac{4.5}{2(3)(10.0(12)/2)}\right) = 0.84 \text{ kips}$$

The axial force in the diagonal as a result of the dead-load reaction R_{DC} on the top strut is computed below.

$$(P_{DC})_{\text{diag.}} = \sqrt{\left(\frac{10.0(12)}{2}\right)^2 + 30^2} \left(\frac{3.5}{2(30)}\right) = 3.91 \text{kips}$$

The axial force in the diagonal as a result of the live-load reaction R_{LL+IM} on the top strut is computed as follows.

$$(P_{LL+IM})_{\text{diag.}} = \sqrt{\frac{10.0(12)}{2}^2 + 30^2} \left(\frac{25.1}{2(30)}\right) = 28.06 \text{ kips}$$

The following calculations determine the controlling load combination.

8.4.2.2.1 Strength I:

$$P_u = 1.00[1.25(3.91) + 1.75(28.06)] = 54.0 \text{ kips (governs)}$$

8.4.2.2.2 Strength III:

$$P_u = 1.00[1.25(3.91) + 1.40(3.35)] = 9.58 \text{ kips}$$

8.4.2.2.3 Strength V:

$$P_u = 1.00[1.25(3.91) + 1.35(28.06) + 0.40(3.35) + 0.40(0.84)] = 44.4 \text{ kips}$$

The initial member selection will be based on the compressive strength slenderness requirements of the member and minimum material thickness requirements. The distance between the working points will be taken as the unbraced length ℓ .

$$\frac{\mathrm{K}\ell}{\mathrm{r}}$$
 < 140

where: K =effective length factor specified in Article 4.6.2.5 as 1.0 for single angles regardless of end connection (in.)

 $\rho = \text{unbraced length (in.)}$

r = minimum radius of gyration (in.)

$$l = \sqrt{\left(\frac{10.0(12)}{2}\right)^2 + 30^2} = 67.08$$
in.

$$r_{min} = \frac{1.0(67.08)}{140} = 0.479 \text{ in.}$$

Thus an L4 x 4 x 5/8 is selected as the trial member, assuming a $\frac{1}{2}$ -inch connection plate. Similarly to the bottom strut of the intermediate cross frames, the member must be evaluated for the combined influences of flexure and axial compression as detailed below. The necessary cross sectional properties for the L4 x 4 x 5/8 are listed below:

$$r_x = r_y = 1.20 \text{ in.}$$

$$r_z = 0.774$$
 in.

$$A_s = 4.61 \text{ in.}^2$$

Check the slenderness provision of Article 6.9.4.2.1 for the cross frame diagonal member:

$$\frac{b}{t} \le k \sqrt{\frac{E}{F_y}}$$
 Eq. (6.9.4.2.1-1)

where: k = plate buckling coefficient, 0.45 for outstanding legs of single angles, from

Table 6.9.4.2.1-1

b = the full width of the outstanding leg for a single angle (in.)

t = plate thickness (in.)

$$\frac{b}{t} = \frac{4}{0.625} = 6.4 < 0.45 \sqrt{\frac{29000}{50}} = 10.8$$
 OK. Member is nonslender.

8.4.2.2.4 **Combined Axial Compression and Flexure**

Compute the effective slenderness ratio per Article 6.9.4.4 based on the criteria for equal-leg angles. First, check the ℓ/r_x limit of 80:

$$\frac{\ell}{r_x} = \frac{(67.08)}{1.20} = 55.96 < 80$$

where: r_x = radius of gyration about the geometric axis of the angle parallel to the connected leg (Although not relevant for equal-leg angles, the term r_x may actually equal r_y when unequal-leg angles are used.)

Therefore, compute the effective slenderness ratio as follows:

$$\left(\frac{K\ell}{r}\right)_{\text{eff}} = 72 + 0.75 \frac{\ell}{r_{x}}$$
 Eq. (6.9.4.4-1)

$$\left(\frac{K\ell}{r}\right)_{\text{eff}} = 72 + 0.75 \frac{(67.08)}{1.20} = 114$$

In accordance with the provisions for single-angle members in Article 6.9.4.4 and using the effective slenderness ratio, $(k\ell/r)_{eff}$, the factored resistance of the angle in compression is taken as:

$$P_r = \phi_c P_n$$
 Eq. (6.9.2.1-1)

where: P_n = nominal compressive resistance determined using the provisions of Article 6.9.4.1.1 ϕ_c = resistance factor for compression as specified in Article 6.5.4.2

To compute P_n , first compute P_e and P_o . P_e is the elastic critical buckling resistance determined as specified in Article 6.9.4.1.2 for flexural buckling, which is the applicable buckling mode for single angles. P_o is the equivalent nominal yield resistance equal to QF_yA_g , where Q is the slender element reduction factor determined as specified in Article 6.9.4.2. Q is taken as 1.0 in this case according to Article 6.9.4.2.1 since the angle member is nonslender per Eq. 6.9.4.2.1-1.

$$P_{e} = \frac{\pi^{2}E}{\left(\frac{K\ell}{r_{s}}\right)^{2}} A_{g}$$
 Eq. (6.9.4.1.2-1)

where $(K\ell/r)_{eff}$ is used in place of $(K\ell/r_s)$ in the denominator.

$$P_{e} = \frac{\pi^{2}E}{\left(\frac{K\ell}{r}\right)_{eff}^{2}} A_{g} = \frac{\pi^{2}(29000)}{(114)^{2}} (4.61) = 101.5 \text{ kips}$$

$$P_o = QF_yA_g = (1.0)(50)(4.61) = 230.5 \text{ kips}$$

Since

$$\frac{P_e}{P_o} = \frac{101.5}{230.5} = 0.44 \ge 0.44$$
,

the nominal axial resistance in compression is computed as:

$$P_{n} = \left[0.658^{\left(\frac{P_{o}}{P_{e}}\right)}\right] P_{o}$$
 Eq. (6.9.4.1.1-1)

$$P_{n} = \left[0.658^{\left(\frac{230.5}{101.5}\right)}\right] (230.5) = 89.1 \,\text{kips}$$

Compute the factored axial resistance of the angle in compression as follows:

$$Pr = \phi_c P_n = 0.95(89.1) = 84.6 \text{ kips}$$

$$P_u = |-54 \text{ kips}| < P_r = 84.6 \text{ kips OK}$$

Therefore, the end cross frame diagonal member is acceptable.

8.5 Stiffener Design

8.5.1 Bearing Stiffener Design

Bearing stiffeners must be provided at locations of concentrated loads for the webs of sections that do not satisfy the provisions of Article D6.5. Specifically, Article D6.5 specifies the web strength of steel I-girders with respect to the limit states of web local yielding and web crippling. Both of these limit states are evaluated below for the abutment and pier locations, assuming a 10 in. bearing length at each location.

The requirement to prevent web local yielding is expressed by Eq. D6.5.2-1.

$$R_u < \phi_b R_n$$

For interior-pier reactions, the web local yielding capacity, R_n , is given by Eq. D6.5.2-2 as follows:

$$R_n = (5k + N)F_{vw}t_w$$

where:

k = distance from the outer face of the flange resisting the bearing force to the web toe of the fillet

$$= 1.25 + 0.3125 = 1.5625$$
 in

N = bearing length = 10 in.

$$F_{yw} = 50 \text{ ksi}$$

$$t_{\rm w} = 0.5 \, {\rm in}.$$

Substituting the above values into Eq. D6.5.2-2 gives the following.

$$R_n = [(5)(1.5625) + 10](50)(0.5)$$

$$R_n = 445 \text{ kips}$$

Then evaluating Eq. D6.5.2-1, where ϕ_b is equal to 1.00 and R_u at the pier is equal to 337 kips, shows that the web yielding requirements are satisfied at the pier.

$$337 \text{ kips} < (1.00)(445) = 445 \text{ kips}$$
 (satisfied)

For evaluating the web yielding capacity at the abutments, Equation D6.5.2-3 is used as follows:

$$R_n = (2.5k + N)F_{yw}t_w$$
 (D6.5.2-2)

$$R_n = [(2.5)(1.5625) + 10](50)(0.4375)$$

$$R_n = 304 \text{ kips}$$

Again evaluating Eq. D6.5.2-1, where R_u at the pier is equal to 258 kips, shows that the web yielding requirements are also satisfied at the abutments.

$$258 \text{ kips} \le (1.00)(304) = 304 \text{ kips}$$
 (satisfied)

The requirements to prevent web crippling are expressed by Eq. D6.5.3-1.

$$R_u \leq \phi_w R_n$$

For interior pier reactions, the web crippling capacity, R_n , is given by Eq. D6.5.3-2 as follows:

$$R_n = 0.8t_w^2 \left[1 + 3\left(\frac{N}{d}\right) \left(\frac{t_w}{t_f}\right)^{1.5} \right] \sqrt{\frac{EF_{yw}t_f}{t_w}}$$

where: d = depth of the steel section = 44.375 in.

 t_f = thickness of the flange resisting the concentrated load = 1.25 in.

$$R_n = 0.8(0.5)^2 \left[1 + 3 \left(\frac{10}{44.375} \right) \left(\frac{0.5}{1.25} \right)^{1.5} \right] \sqrt{\frac{(29,000)(50)(1.25)}{0.5}} = 446 \text{ kips}$$

Evaluation of Eq. D6.5.3-1 where ϕ_w is equal to 0.80 then shows that the pier section has sufficient web crippling resistance.

$$337 \text{ kips} < (0.80)(446) = 356 \text{ kips}$$
 (satisfied)

For abutment reactions, R_n is expressed by either Eq. D6.5.3-3 or D6.5.3-4 depending on the ratio between the bearing length and the steel section depth. For the present example with N/d = 10/44 = 0.23 at the abutments, Eq. D6.5.3-4 applies as follows:

$$R_n = 0.4t_w^2 \left[1 + 3\left(\frac{4N}{d} - 0.2\right) \left(\frac{t_w}{t_f}\right)^{1.5} \right] \sqrt{\frac{EF_{yw}t_f}{t_w}}$$
 Eq. (D6.5.3-4)

$$R_n = 0.4(0.4375)^2 \left[1 + 3 \left(\frac{(4)(10)}{44} - 2 \right) \left(\frac{0.4375}{1.25} \right)^{1.5} \right] \sqrt{\frac{(29,000)(50)(1.25)}{0.4375}} = 179 \text{ kips}$$

Evaluating Eq. D6.5.3-1 at the abutments thus shows that bearing stiffeners must be provided to prevent web crippling.

$$258 \text{ kips} > (0.80)(179) = 143 \text{ kips}$$
 (not satisfied)

The bearing stiffeners are typically plates welded to both sides of the web that extend the full depth of the web, and are as close to the outer edges of the flanges as practical. The plates are to bear against or to be welded to the flange that the load is transmitted through. This example illustrates the design of bearing stiffeners at Abutment 1.

8.5.1.1 Projecting Width (Article 6.10.11.2.2)

The width, b_t, of projecting stiffener elements must satisfy the following:

$$b_t \le 0.48t_p \sqrt{\frac{E}{F_{ys}}}$$
 Eq. (6.10.11.2.2-1)

It will be assumed that 6 inches wide plates are welded to each side of the web. Eq. 6.10.11.2.2-1 is then rearranged to determine the minimum allowable thickness of the stiffener.

$$(t_p)_{\text{min.}} = \frac{b_t}{0.48 \sqrt{\frac{E}{F_{ys}}}} = \frac{6.0}{0.48 \sqrt{\frac{29,000}{50}}} = 0.52 \text{ in.}$$

Thus, a 6 inch by 5/8 inch plate will be used to evaluate the bearing stiffener requirements.

8.5.1.2 Bearing Resistance (Article **6.10.11.2.3**)

The factored resistance for the bearing stiffeners is to be taken as:

$$(R_{sb})_r = \phi_b (R_{sb})_n$$
 Eq. (6.10.11.2.3-1)

where: ϕ_b = resistance factor for bearing =1.0 (Article 6.5.4.2)

 $(R_{sb})_n$ = nominal bearing resistance for bearing stiffeners

$$= 1.4A_{pn}F_{ys}$$
 Eq. (6.10.11.2.3-2)

 A_{pn} = area of the projecting elements for the stiffener outside of the web-to-flange fillet welds but not beyond the edge of the flange

In this design example, it is assumed the clip provided at the base of the stiffener to clear the web-to-flange weld is 1.5 inches in length.

$$A_{pn} = 2(6.0 - 1.5)(0.625) = 5.63 \text{ in.}^2$$

 $(R_{sb})_n = 1.4(5.63)(50) = 394 \text{ kips}$
 $(R_{sb})_r = (1.00)(394) = 394 \text{ kips} > R_u = 258 \text{ kips}$ (satisfied)

The 6 inch by 5/8 inch bearing stiffeners have adequate bearing resistance.

8.5.1.3 Axial Resistance of Bearing Stiffeners (Article 6.10.11.2.4)

The factored axial resistance is calculated from Article 6.9.2.1 of the specifications, where the radius of gyration is computed about the mid-thickness of the web, and the effective length is taken as 0.75D. For stiffeners welded to the web, part of the web is considered in the effective column section. The strip of web included in the effective column is not more than $9t_w$ on each side of the stiffeners. Therefore, the area of the effective column section is computed below:

$$A_s = 2[(6.0)(0.625) + 9(0.4375)(0.4375)] = 10.95 \text{ in.}^2$$

The moment of inertia of the effective column section is computed as follows:

$$I_s = \frac{0.625(6.0 + 0.4375 + 6.0)^3}{12} = 100.2 \text{ in.}^4$$

The radius of gyration computed about the mid-thickness of the web is computed as:

$$r_{_{\!S}} = \sqrt{\frac{I_{_{\!S}}}{A_{_{\!S}}}} = \sqrt{\frac{100.2}{10.95}} = 3.03 \, \text{in}.$$

The effective length is computed as follows:

$$Kl = 0.75D = 0.75(42.0) = 31.50 \text{ in.}$$

The bearing stiffeners must satisfy the limiting slenderness ratio, stated in Article 6.9.3, which is 120 for main members in compression.

$$\frac{Kl}{r_s} = \frac{31.5}{3.03} = 10.40 \le 120$$
 (satisfied)

As previously mentioned, the factored axial resistance of the effective column section is calculated from Article 6.9.2.1 using the specified minimum yield strength of the stiffener.

$$P_r = \phi_c P_n$$
 Eq. (6.9.2.1-1)

where:

 ϕ_c = resistance factor for axial compression = 0.95 (Article 6.5.4.2)

 P_n = nominal compressive resistance from Article 6.9.4.1

Determine P_n using Article 6.9.4.1. First, determine the elastic critical buckling load, P_e , per Article 6.9.4.1.2 as follows:

$$P_{e} = \frac{\pi^{2}E}{\left(\frac{K\ell}{r_{s}}\right)^{2}} A_{g}$$
 Eq. (6.9.4.1.2-1)

$$P_e = \frac{\pi^2 (29000)}{(10.40)^2} (10.95) = 2,646 \text{kips}$$

$$P_o = QF_vA_g$$
 Article 6.9.4.1.1

where,

 $P_o =$ Equivalent nominal yield resistance

Q = Slender Element Reduction factor, taken as 1.0 for bearing stiffeners

$$P_o = QF_yA_g = (1.0)(50)(10.95) = 547.5 \text{ kips}$$

$$P_e / P_o = 2646 / 547.5 = 4.83 > 0.44$$

Therefore, Eq. 6.9.4.1.1-1 applies.

$$P_{n} = \left[0.658^{\left(\frac{P_{o}}{P_{e}}\right)}\right] P_{o}$$
 Eq. (6.9.4.1.1-1)

$$P_e = \left[0.658^{547.5/2646}\right] (547.5) = 502.1 \,\text{kip}$$

$$P_r = 0.95(502.1) = 477 \text{ kips} > R_u = 258 \text{ kips}$$
 (satisfied)

8.5.1.4 Bearing Stiffener-to-Web Welds

Adequate shear strength of the welds joining the bearing stiffener to the web must also be verified. First the weld shear strength, which is the area of the weld multiplied by 60 percent of the yield strength of the weld metal, is determined.

$$R_r = 0.6\phi_{e2}F_{exx}$$
 Eq. (6.13.3.2.4b-1)

where:

 ϕ_{e2} = resistance factor for shear in the throat of the weld metal = 0.80

 F_{exx} = classification strength of the weld metal = 70 ksi for this example

$$R_r = 0.6(0.80)(70) = 33.6 \text{ ksi}$$

The minimum size fillet weld permissible in this situation is 0.25 inches, according to Table 6.13.3.4-1. Using this weld size the shear strength per unit length of weld is as follows.

$$V = 33.6(0.707)(0.25) = 5.94 \text{ k/in}.$$

The length of the weld, allowing 2.5 inches for clips at both the top and bottom of the stiffener, is:

$$L = 42.0 - 2(2.5) = 37.0 \text{ in.}$$

The total factored resistance of the weld connecting the stiffener to the web of the section is then 879 kips which is greater than the required shear strength of 258 kips.

$$4(37.0)(5.94) = 879.1 \text{ kips} > 258 \text{ kips}$$
 (satisfied)

8.6 Flange-to-Web Weld Design

This section outlines the weld design for the web-to-flange junction. The weld design resistance is checked against the factored shear flow associated with the design loads. The horizontal shear flow at the end bearing is computed from the following equation:

$$s = \frac{VQ}{I}$$

where:

V = shear force (kips)

Q = statical moment of the area about the neutral axis (in.³)

I = moment of inertia (in.⁴)

Similar to previous calculations, the shear flow will be computed by considering the cross sectional properties applicable to various applied forces. Thus, the statical moment of the area about the neutral axis will be computed for each applicable section.

8.6.1 Steel Section:

Top Flange: $Q = (10.50)(25.63) = 269.1 \text{ in.}^3$

Bottom Flange: $Q = (20.0)(17.37) = 347.4 \text{ in.}^3$

8.6.2 Long-term Section:

Top Flange: $Q = (10.50)(12.81) = 134.5 \text{ in.}^3$

Slab: $Q = (34.0)(18.43) = \underline{626.6 \text{ in.}^3}$ 761.1 in.³

Bottom Flange: $Q = (20.0)(30.20) = 604.0 \text{ in.}^3$

8.6.3 Short-term Section:

Top Flange: $Q = (10.50)(4.51) = 47.4 \text{ in.}^3$

Slab: $Q = (102)(10.13) = \frac{1033.3 \text{ in.}^3}{1080.7 \text{ in.}^3}$

Bottom Flange: $Q = (20.0)(38.50) = 770.0 \text{ in.}^3$

The shear flow under each loading is thus computed as follows, where it is determined that the top flange experiences the highest level of shear flow.

Top Flange:

DC1: s = (1.25)(44)(269.1)/15,969 = 0.93

DC2: s = (1.25)(7)(761.1)/35,737 = 0.19

DW: s = (1.5)(9)(761.1)/35,737 = 0.29

LL+IM s = (1.75)(103)(1080.7)/48,806 = 4.00

= 5.41 kip/in

Bottom Flange:

DC1:
$$s = (1.25)(44)(347.4)/15,969 = 1.20$$

DC2:
$$s = (1.25)(7)(604.0)/35,737 = 0.15$$

DW:
$$s = (1.5)(9)(604.0)/35,737 = 0.23$$

$$LL+IM$$
 $s = (1.75)(103)(770.0)/48,806 = 2.84$

= 4.42 kip/in

Thus, the applied shear flow of 5.41 k/in., must be evaluated in comparison to the shear resistance of the fillet welds and the shear rupture resistance of the base metal. The specifications limit the minimum size of a fillet weld in which the base metal is thicker than 0.75" to 5/16." Therefore, a 5/16" fillet weld is assumed on each side of the plate. The factored shear resistance of the weld metal is determined as follows:

$$R_r = 0.6\phi_{e2}F_{exx}$$
 Eq. (6.13.3.2.4b-1)

where:

$$\phi_{e2}$$
 = resistance factor for shear on the throat of the weld metal

$$= 0.80$$
 (Article 6.5.4.2)

 F_{exx} = classification strength of the weld metal= 70 ksi

$$R_r = 0.6(0.80)(70) = 33.6 \text{ ksi}$$

The allowable shear flow for the 5/16 inch welds is:

$$v = 33.6(0.707)(0.3125)(2) = 14.85 \text{ k/in}.$$

From Article 6.13.5.3, the factored shear rupture resistance of the connected material is computed as follows:

$$R_r = \phi_{vu} 0.58 R_p F_u A_{vn}$$
 Eq. (6.13.5.3-2)

where:

 A_{vn} = net area of the connection element subject to shear (equal to the gross area for welded connections)

 $F_u =$ tensile strength of the connection element specified in Table 6.4.1-1

 ϕ_{vu} resistance factor for shear rupture of connection elements = 0.80

Rp = reduction factor for holes taken equal to 0.90 for bolt holes punched full size and 1.0 for bolt holes drilled full size or subpunched and reamed to size (equal to 1.0 for welded connections)

The factored shear rupture resistance of the connected material is therefore:

$$v = (0.80)(0.58)(1.0)(70)(0.4375) = 14.21 \text{ k/in.}$$
 (governs)

Since, $v = 14.21 \ k/in. > v_u = 5.41 \ k/in.$, the 5/16" fillet weld is adequate for the web-to-flange welds.

9.0 REFERENCES

1. AASHTO (2014). *AASHTO LRFD Bridge Design Specifications*, 7th Edition, American Association of State Highway and Transportation Officials, Washington, DC.