## ENCE 353 Midterm 1, Open Notes and Open Book

## Name:

Exam Format and Grading. This exam has three questions. Partial credit will be given for partially correct answers, so please show all your working.

| Question | Points | Score |
| :---: | :---: | :---: |
| 1 | 15 |  |
| 2 | 15 |  |
| 3 | 10 |  |
| Total | 40 |  |

## Question 1 (15 points): Shear Forces and Bending Moments in a connected Beam Structure.

Consider the multi-span beam structure shown in Figure 1.


Figure 1: Multi-span beam structure.

The cantilever is fully-fixed to the wall at Point A. Points B, D and E are hinges. An external moment of $20 \mathrm{kN} . \mathrm{m}$ is applied at Point H.
[1a] (2 pts). Compute the degree of indeterminacy for the beam structure.
[1b] (4 pts). Compute the reactions at points A, C, F and G.
[1c] ( 7 pts ). Compute and draw the shear force and bending moment diagrams along the beam.
[1d] (2 pts). Indicate on Figure 1 where you believe the beam fibre will be in compression (C) and tension (T).

Question 2 (15 points): Tension, Compression and Zero-Force Members in a Truss Structure.

Consider the truss structure shown in Figure 2.


Figure 2: Nine-bar truss structure.

A horizontal load of P kN is applied at node D , and a vertical load of P kN is applied at node F .
[2a] (4 pts). Compute the support reactions at points A and C.
[2b] (4 pts). Identify the zero-force members.
[2c] (7 pts). Using the method of joints (or otherwise) show that: (1) The maximum tensile force in the structure is $P \mathrm{kN}$, and (2) The maximum compressive force in the structure is $\sqrt{2} P$ kN .

## Question 3 (10 points): Degree's of Indeterminacy.

[3a] (5 pts). Compute the degree of indeterminacy for the structure shown in Figure 3.


Figure 3: Simple portal frame.
[3b] (5 pts). Using the method of trees (or otherwise), compute the degree of indeterminacy for the moment-resistant frame shown in Figure 4.


Figure 4: Elevation view of a moment-resistant frame.

