

**ENCE 353 Midterm 2, Open Notes and Open Book**

Name : \_\_\_\_\_

**Exam Format and Grading.** Attempt both questions 1 and 2. Partial credit will be given for partially correct answers, so please show all your working.

Question	Points	Score
1	20	
2	20	
Total	40	

**Question 1: 20 points**

**Moment-Area and Deflections.** Consider the cantilevered beam structure shown in Figure 1.

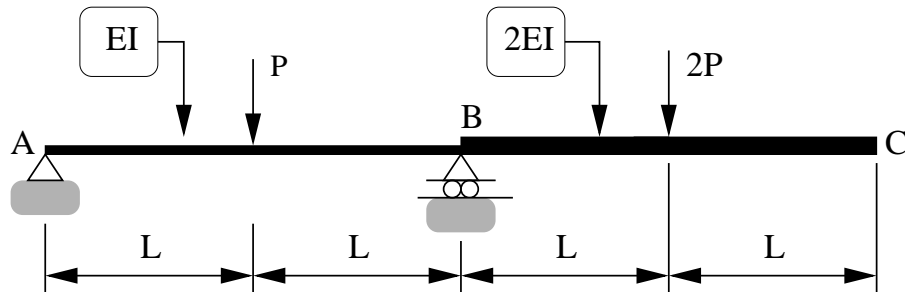


Figure 1: Front elevation view of a cantilevered beam structure.

Notice that segments A-B and B-C have cross-sectional properties EI and 2EI, respectively.

**[1a]** (4 pts) Compute and draw the  $M(x)/EI$  diagram for the complete beam A-B-C.

**[1b]** (4 pts) Draw and label a diagram of the deflected shape. Clearly indicate on your diagram regions of the beam having zero curvature.

**[1c]** (6 pts) Draw and label a diagram showing how the rotation at A is related to the beam deflections at points B and C.

**[1d]** (6 pts) Use the method of moment-area to compute the vertical deflection of the beam at point C.

**Question 2: 20 points**

**Virtual Forces.** Figure 2 is a front elevation view of a simple two-bar truss. A vertical load  $P$  is applied at node B.

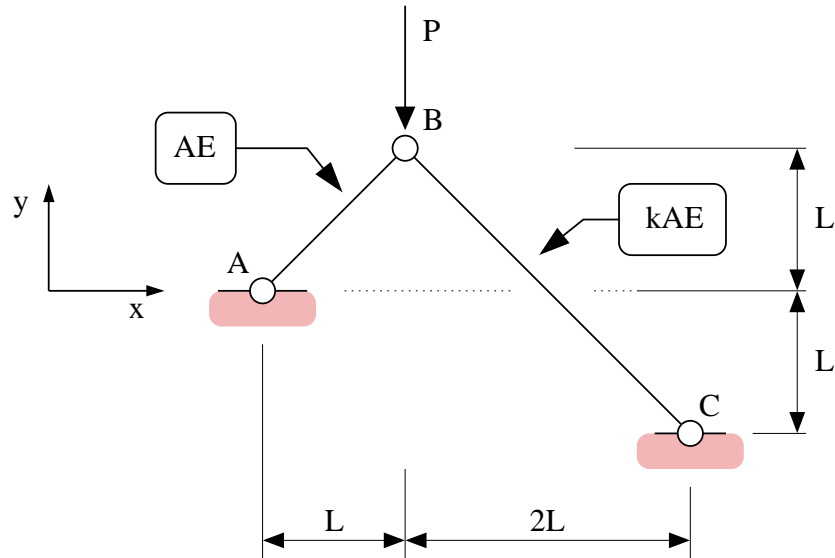


Figure 2: Front elevation view of a simple two-bar truss.

Notice that the left-hand bar has cross section properties  $AE$ , and the right-hand bar has cross section properties  $kAE$ , where  $k$  is a positive constant.

[2a] (6 pts) Use the method of virtual forces to show that the vertical displacement at node B is:

$$\Delta_y = \left[ \frac{\sqrt{2}}{k} + \frac{1}{\sqrt{2}} \right] \frac{PL}{AE}. \quad (1)$$

**[2b]** (6 pts) Show that the horizontal displacement at node B is:

$$\Delta_x = \left[ \frac{\sqrt{2}}{k} - \frac{1}{\sqrt{2}} \right] \frac{PL}{AE}. \quad (2)$$

**[2c]** (4 pts) Hence, show that:

$$\text{Total displacement at node B} = \sqrt{\left[ \frac{4}{k^2} + 1 \right]} \cdot \frac{PL}{AE}. \quad (3)$$

**[2d]** (4 pts) Determine the value of  $k$  that will cause node B to move downwards with zero horizontal displacement. This is a one-line computation.