

**ENCE 353 Homework 4**

**Question 1:** Figure 1 is an elevation view of a cantilever beam that carries a uniformly distributed load,  $w$  (N/m), over half of its length.

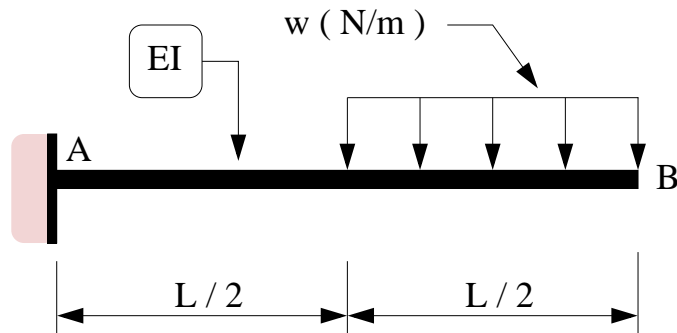


Figure 1: Elevation view of a cantilever beam that carries a uniformly distributed load,  $w$ , over half of its length.

Use the moment-area method to show that the vertical deflection at point B is:

$$\Delta_B = \left[ \frac{41wL^4}{384EI} \right]. \quad (1)$$

**Question 2:** Figure 2 is an elevation view of a cantilever beam of length  $L$  that is supported at its tip and carries a point load  $P$  at distance “ $a$ ” from the left-hand support.

Use the moment-area method and the principle of superposition to show that the vertical support reaction at point B is:

$$R = \frac{3P}{2} \left[ \frac{a}{L} \right]^2 \left[ 1 - \frac{1}{3} \frac{a}{L} \right]. \quad (2)$$

Notice that when  $a = 0$ ,  $R = 0$  and when  $a = L$ , the support reaction  $R = P$ .

Show that the maximum bending moment at A occurs when  $a = \left[ 1 - \frac{1}{\sqrt{3}} \right] L$ .

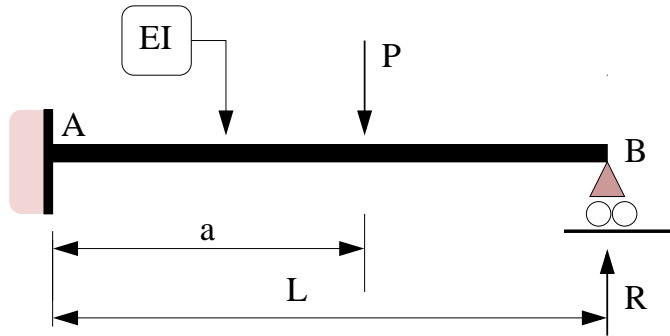


Figure 2: Elevation view of a support cantilever beam that carries a point load P.

**Question 3:** Figure 3 is a front elevation view of a simple beam structure carrying two external loads P. The beam has section properties EI near the supports and 2EI in the center section.

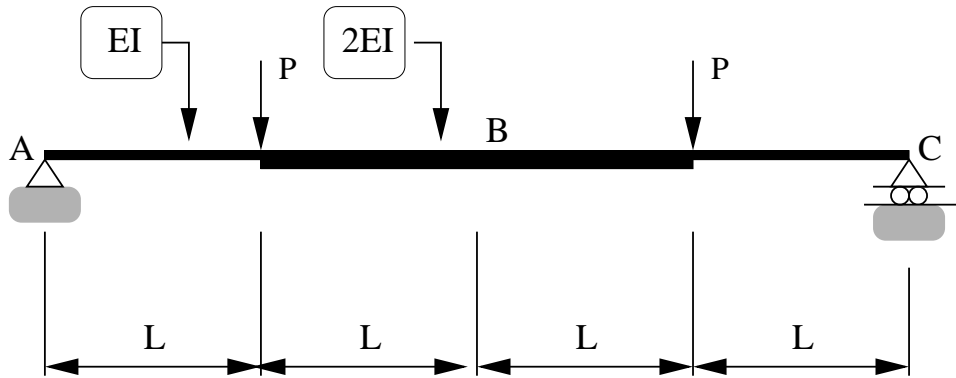


Figure 3: Simple beam structure (symmetric loads P).

Use the method of moment area to show that the end rotation at A (measured clockwise) is:

$$\theta_A = \frac{PL^2}{EI}. \quad (3)$$

Use the method of moment area to show that the vertical beam deflection at B is:

$$\Delta_B = \frac{13}{12} \frac{PL^3}{EI}. \quad (4)$$